## MEDICAL STATISTICS

Physiology
Anatomy
Chemistry
...

No any doubt
Statistics


Theory: matematics


Practice: applied statistics (examples)


Example: body temperature$36.7^{\circ} \mathrm{C}$

$36.9^{\circ} \mathrm{C}$
$36.6^{\circ} \mathrm{C}$

1. Inaccuracy of the measurement.
2. Daily fluctuation!!!

The measured value is not constant!
3. Biological variability!!!


Measured value: $37.0^{\circ} \mathrm{C}$. Is it healthy or not?

## Medical statistics




## Description of a variable

- Type
- Possible values
- Occurrence of the values


## Numerical variables

| Name | Continuous | Discrete |
| :--- | :---: | :---: |
| Definition | Infinitely large no. of <br> values in a certain range | Only finite number of <br> values |
| Example | Height, temperature, <br> pressure.. | No. of teeth, no. of <br> children.. |



## Determination of the possible values

- Continuous: giving a possible range.
» e.g.: height from $\sim 50 \mathrm{~cm}-$ to $\sim 250 \mathrm{~cm}$
- Another : listing the values, if it is possible » E.g.: blood type: A, B, AB, 0


## Occurence

## Population

How many people? are not the same!


Trial: experiment, observation, data collection. Deal with only the case, when the trial may be repeated!

Outcome: result of one trial. (e.g.: height of a student)


## Selection of the sample

## Main principle: Random sample

Medical statistics: if there is no any reason to exclude,
must be random!

## Occurrence

## Frequency distribution

Frequency as the function of the possible values.

| Blood-type | $\mathbf{0}$ | $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{A B}$ | total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| frequency | 17 | 21 | 10 | 2 | 50 |

$$
n=\sum_{i} k_{i}
$$



## Relative frequency, proportion

The ratio of the frequency and the total no. of the elements.

$$
\sum_{i} \frac{k_{i}}{n}=\frac{1}{n} \sum_{i} k_{i}=\frac{1}{n} \times n=1
$$

Frequently it is given as percentage:

$$
\frac{k_{i}}{n} \times 100 \%
$$



Properties of the probability

$$
\mathrm{O} \leq P \leq 1 \quad \longrightarrow \quad \begin{aligned}
& \mathrm{P}=0-\text { never occur } \\
& \mathrm{P}=1-\text { always occur }
\end{aligned}
$$

$\begin{aligned} & \text { Example: blood- type } \\ & P_{A}+P_{B}+P_{A B}+P_{0}=1\end{aligned} \longrightarrow \sum_{i} P_{i}=1$
(exclusive events)


## Continuous quantity

Infinite no. of possible values!!!

Class: a short interval in the whole range.
Class-width: the length of the class
Frequency: no. of elements in the given class.

## Example

| 1 | 160 cm |
| :---: | :---: |
| 2 | 181 cm |
| 3 | 175 cm |
| 4 | 163 cm |
| 5 | 165 cm |
| 6 | 179 cm |
| 7 | 164 cm |
| 8 | 185 cm |
| 9 | 177 cm |
| 10 | 168 cm |


| class | $k_{\mathrm{i}}$ |
| :---: | :---: |
| $160-164$ | 3 |
| $165-169$ | 2 |
| $170-174$ | 0 |
| $175-179$ | 3 |
| $180-184$ | 1 |
| $185-189$ | 1 |

## Decrease the width!

## Presentation

Frequency distribution (class width $=5 \mathrm{~cm}$ )


5 cm is too large!


## Consequence

## Normal distribution

Class-width


No. of classes


We must increase the no. of the elements!

## Theoretical description

Normal or Gauss-distribution

$$
g(x)=\frac{1}{\sigma \sqrt{2 \pi}} e^{-\frac{(x-\mu)^{2}}{2 \sigma^{2}}}
$$

Parameters:
$\mu$ - expected value or mean
$\sigma-$ theoretical standard deviation


If $n$ and no. of classes are infinite!

Normal distribution ( $\mu=170, \sigma=8$ )


## Meaning of the parameters

$\mu \quad$ (mean):
the value belonging to the maximum of the curve.
$\sigma$ (theoretical standard deviation):
the average deviation of the data from the $\mu$.


## Standard deviation

$$
\begin{aligned}
& (\mu \pm \sigma) \sim 68 \% \text { of data } \\
& (\mu \pm 2 \sigma) \sim 95 \% \text { of data } \\
& (\mu \pm 3 \sigma) \sim 99.5 \% \text { of data }
\end{aligned}
$$



## Normal distribution

## Estimation of the $\mu$


average: must be in the center of the data range.

$$
\sum_{i}\left(x_{i}-\bar{x}\right)=0 \quad \bar{x}=\frac{\sum_{i} x_{i}}{n}
$$

## Estimation of the $\sigma$

$\sigma=$ average deviation of the data from the $\mu$.
$\mathbf{s}$ (standard deviation) = average deviation of the elements from the average.


$$
Q_{x}=\sum_{i}\left(x_{i}-\bar{x}\right)^{2} \geq 0
$$

## Relation of parameters

$$
\begin{aligned}
& (\bar{x} \pm s) \sim 68 \% \\
& (\bar{x} \pm 2 s) \sim 95 \% \\
& (\bar{x} \pm 3 s) \sim 99.5 \%
\end{aligned}
$$

## Standard deviation

$s=\sqrt{\frac{Q_{x}}{n-1}}$
$s$ : the average deviation of the elements from the average.

## Question of the week!

How can we estimate the $\mu$ and the $\sigma$ ?
$\sigma$

