

Sedimentation and electrophoresis methods

Schay G.

Physical basis of sedimentation methods

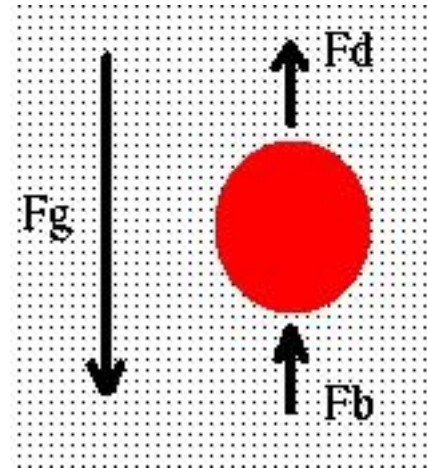
Goal: we would like to measure the mass of tiny particles

(this method originates long before the AFM or resonance methods, but is still in use)

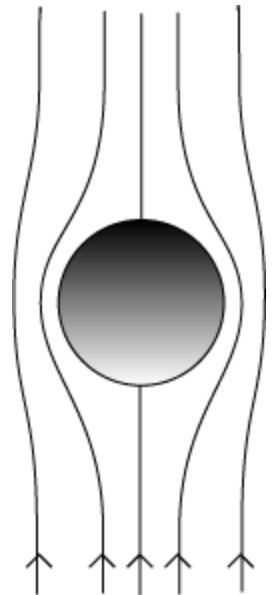
Put the particle into a solvent/liquid, and see what happens:

If it's density is higher than that of the liquid, it will sink, or settle down.

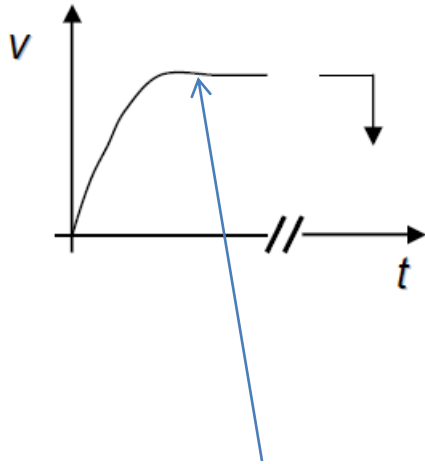
This is called **sedimentation**.



F_g : gravity force, F_d : drag force, F_b : buoyant force.



Drag: a force (F_d) acting on a moving object (usually in a fluid of given viscosity) , working against the movement.
 $F_d \sim v, \eta, \text{size}$



The particle will accelerate until the force equilibrium is reached.

(or until the bottom of the holder tube is reached)

Here we have the force equilibrium

Newton-II. Law : $\Sigma F = m \cdot a$

and

$$\frac{\Delta v}{\Delta t} = a$$

At force equilibrium $a=0$.

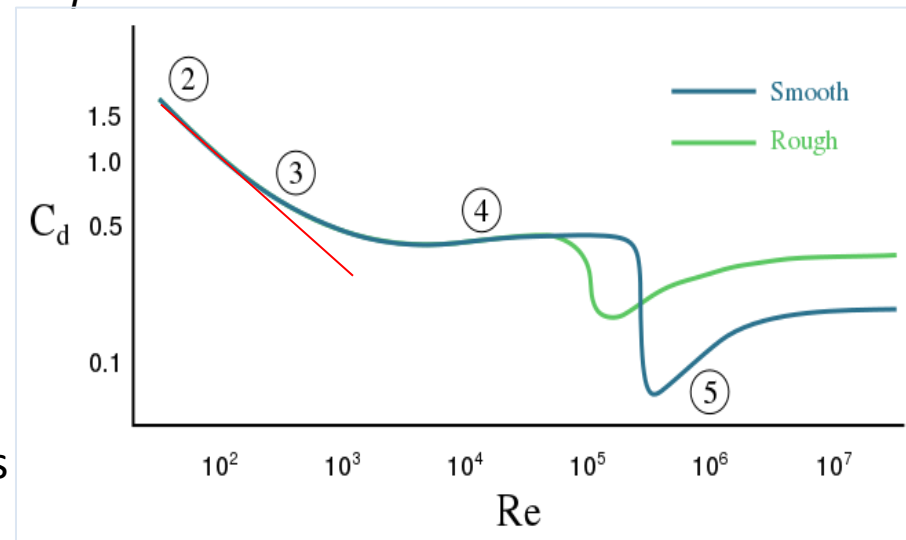
The drag force:

General equation: $F_d = \frac{1}{2} \rho v^2 \cdot C_d \cdot A$, where A is the cross-sectional area, and C_d is the **drag coefficient**.

At low speeds $C_d \sim 1/Re$, which means F_d is linearly proportional to the speed.

$$Re = \frac{v \cdot L}{\eta / \rho} = \frac{v \cdot L \cdot \rho}{\eta}$$

If we substitute this into the Eq. of F_d , then one can see that F_d at low speeds depends on the viscosity, and the diameter. (L is the characteristic length, in case of a sphere it is the diameter, but A also depends on L)



Double-log, and slope=-1

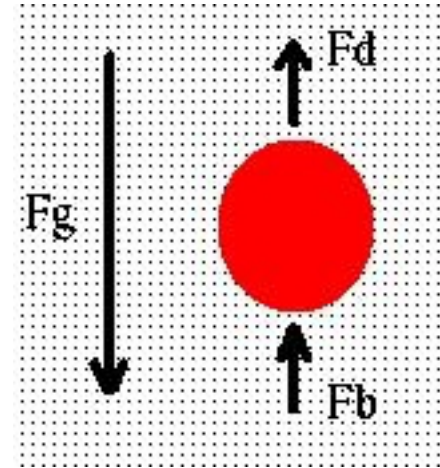
N.B.: Re is the Reynolds number

F_g : gravity force, F_d : drag force, F_b : buoyant force.

Newton-II. Law : $\Sigma F = m \cdot a$

and

$$\frac{\Delta v}{\Delta t} = a$$



$$F_g = m \cdot g$$

$$F_d = f \cdot v \quad (Re < 0.1)$$

where f is the shape constant, embedding C_d .

From Archimedes's law we get: $F_b = g \cdot \rho_{\text{fluid}} \cdot V_{\text{particle}}$, but $V_{\text{particle}} = m / \rho_{\text{particle}}$

$$\text{so } F_b = m \frac{\rho_{\text{fluid}}}{\rho_{\text{particle}}}$$

From the force equilibrium we get:

$$\Sigma F = 0, \text{ which means } F_g - F_b - F_d = 0,$$

(or $F_d = F_g - F_b$) thus

$$f \cdot v = m \cdot g \cdot \left(1 - \frac{\rho_{\text{fluid}}}{\rho_{\text{particle}}} \right)$$

$V \neq v$ (Volume, velocity)

There is one problem with this:

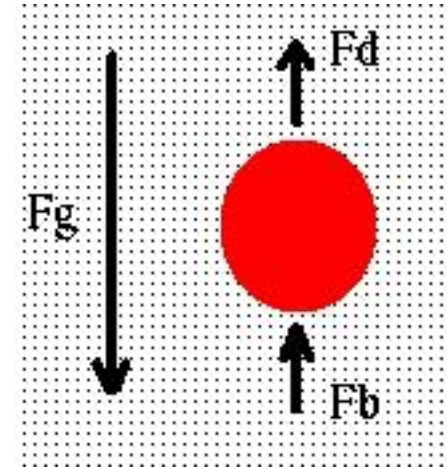
If the particles are really small, then the **Brownian motion** will prohibit settling, and thus the method will not work.

Solution: Centrifuge!



Let's centrifuge the fluid+particles:

Fg : gravity force, Fd: drag force, Fb: buoyant force.



$g = 9.8 \text{ m/s}^2$ would be the gravity force, but in the centrifuge
 $a = r\omega^2$ is the acceleration felt by the particle. (ω is the angular velocity)

$$f \cdot v = m \cdot \mathbf{g} \cdot \left(1 - \frac{\rho_{fluid}}{\rho_{particle}}\right)$$



$$f \cdot v = m \cdot r \cdot \omega^2 \cdot \left(1 - \frac{\rho_{fluid}}{\rho_{particle}}\right)$$

We can rearrange such as:

$$S \equiv \frac{v}{r \cdot \omega^2} = \frac{m}{f} \cdot \left(1 - \frac{\rho_{fluid}}{\rho_{particle}}\right)$$

here S is the sedimentation coefficient. Unit is Svedberg, 1Sv = 10^{-13} s

(Theodor Svedberg , Nobel prize 1926)

This shows, that mass and density play a crucial role.
If the density is identical, then the bigger particle will sediment faster.

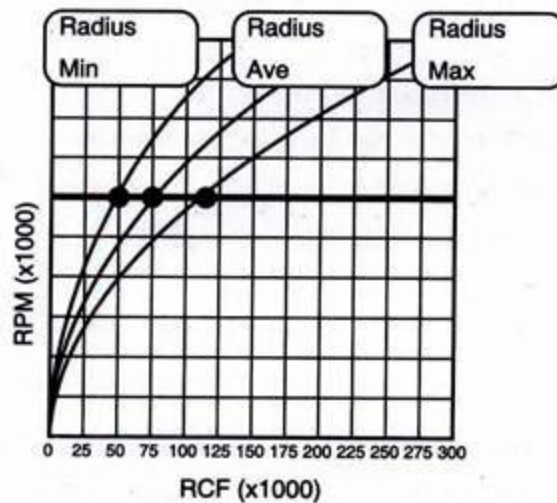


Useful equations

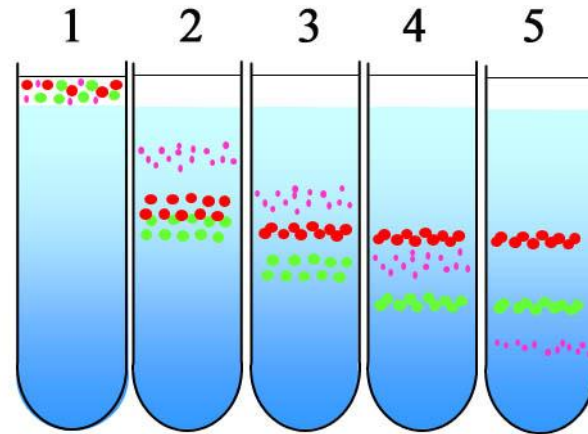
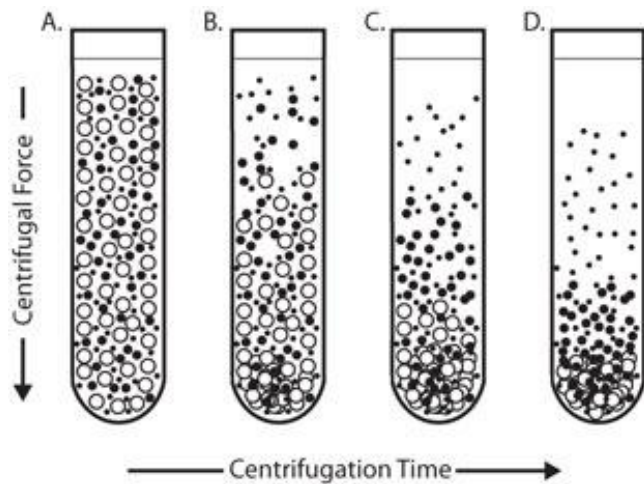
$$\omega = 2\pi \left(\frac{rpm}{60} \right), \text{ rpm} = \text{revolutions per minute}$$

RCF: relative centrifugal field

$$RCF = a = r\omega^2 = 4\pi^2 \text{ rpm}^2 / 3600$$



Since the terminal velocities are different, the particles segregate/separate by mass during the process

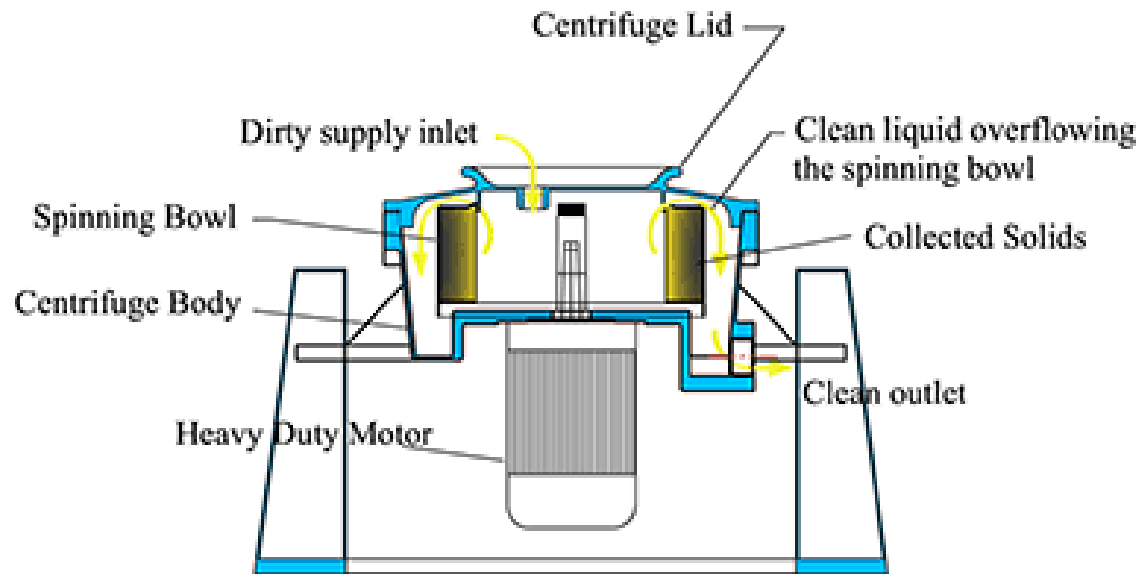


There is always an optimal centrifugation time!

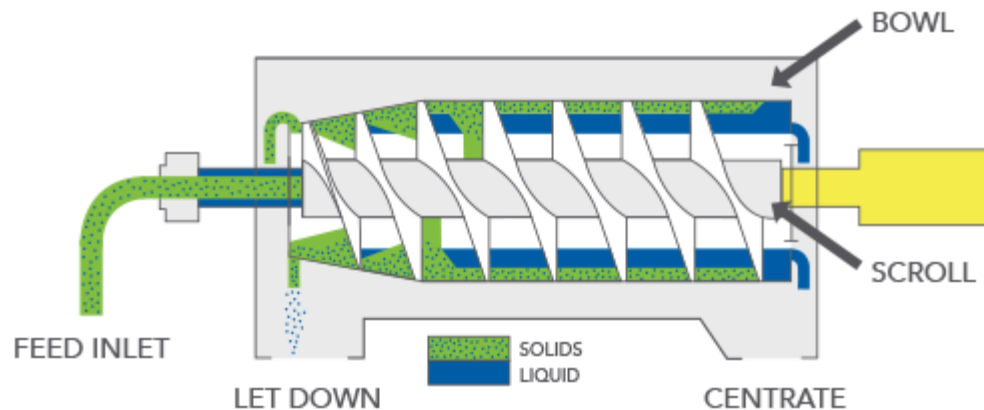
Too short: no separation

Too long: every size reaches the bottom, also no separation.

The centrifugal separator



The centrifugal force can be generated by many ways.



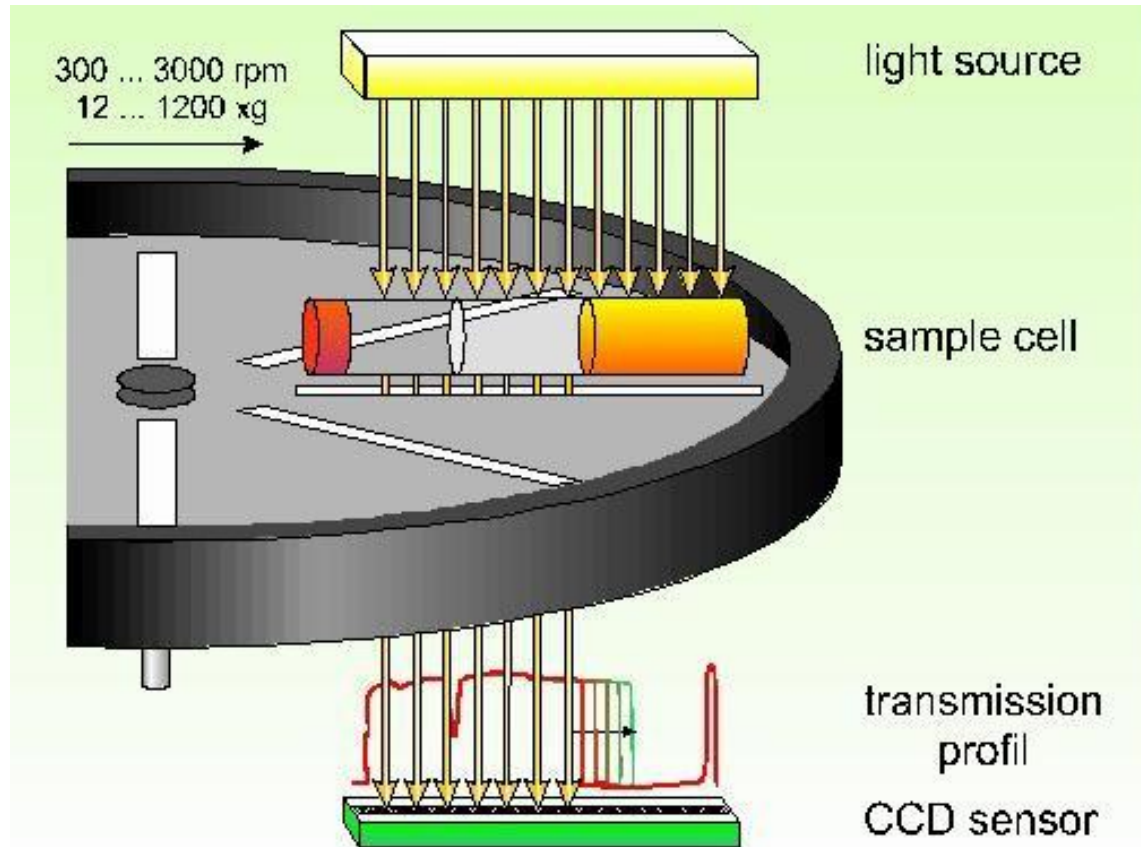
Rotating the mixture, or rotating the container, both, etc..

Everyday life:
Fruit centrifuge.

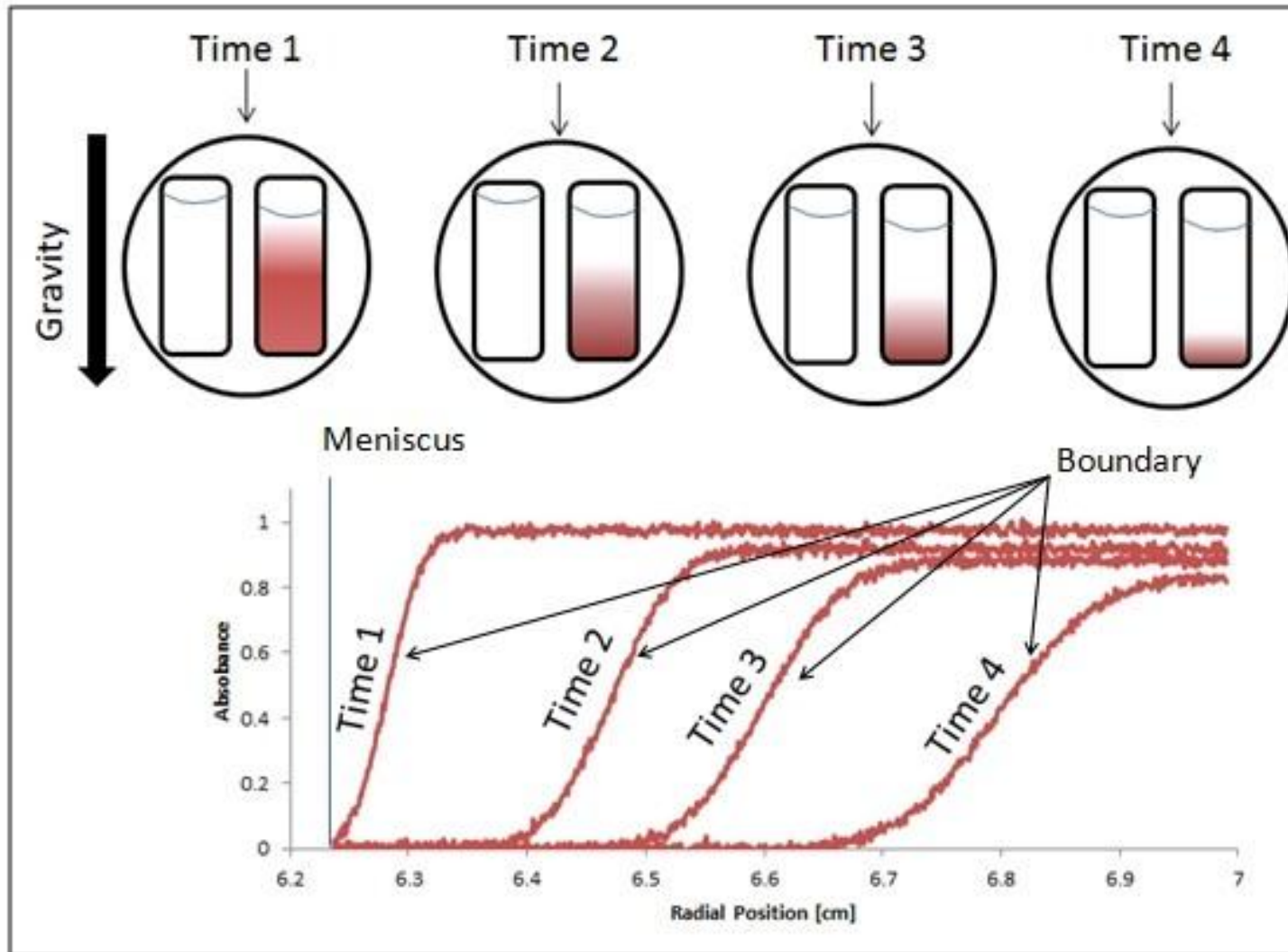


Quantitative methods

We want to measure during centrifugation



Centrifuging a mono-component system +fluid

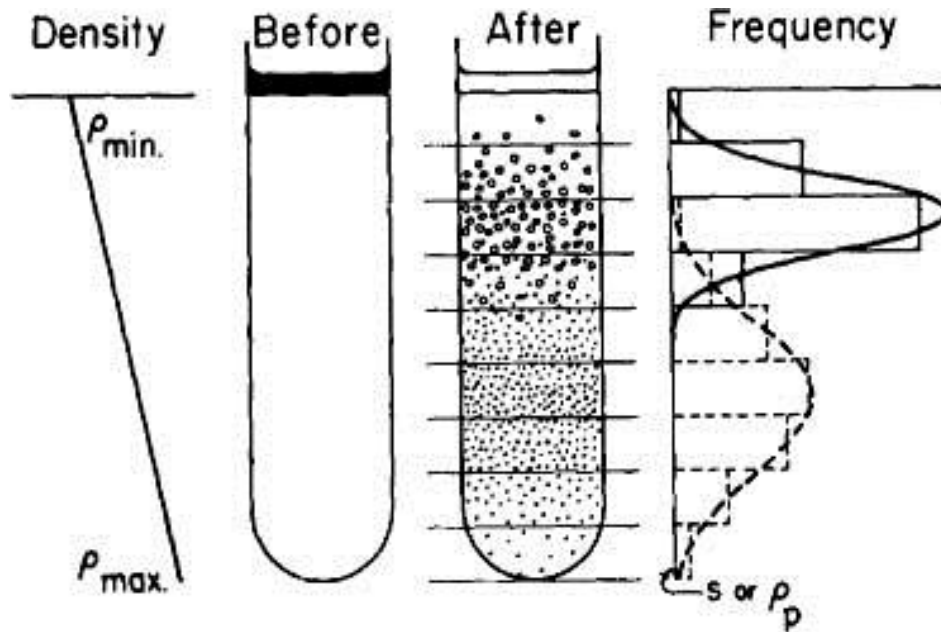


The only remaining unknown is the f : **form-factor**

But this is also in the diffusion:

$$f = \frac{kT}{D} \text{ where } D \text{ is the diffusion coefficient.}$$

So we need to measure diffusion, in order to get the particle size.



It is possible to use a density gradient in the sedimentation medium.

In this case during centrifugation different density particles will stop settling at different positions.

This can be used also for separation:

Preparative or analytical ultracentrifugation methods.

1. Differential sedimentation

Gradient: *Shallow stabilizing, $\rho_{\max.} < \rho_{p \max.}$*

Centrifugation: \rightarrow *Incomplete sedimentation*

Abscissa of frequency distribution: *Sedimentation coefficient*

2. Density equilibration

Gradient: *Steep, $\rho_{\max.} > \rho_{p \max.}$*

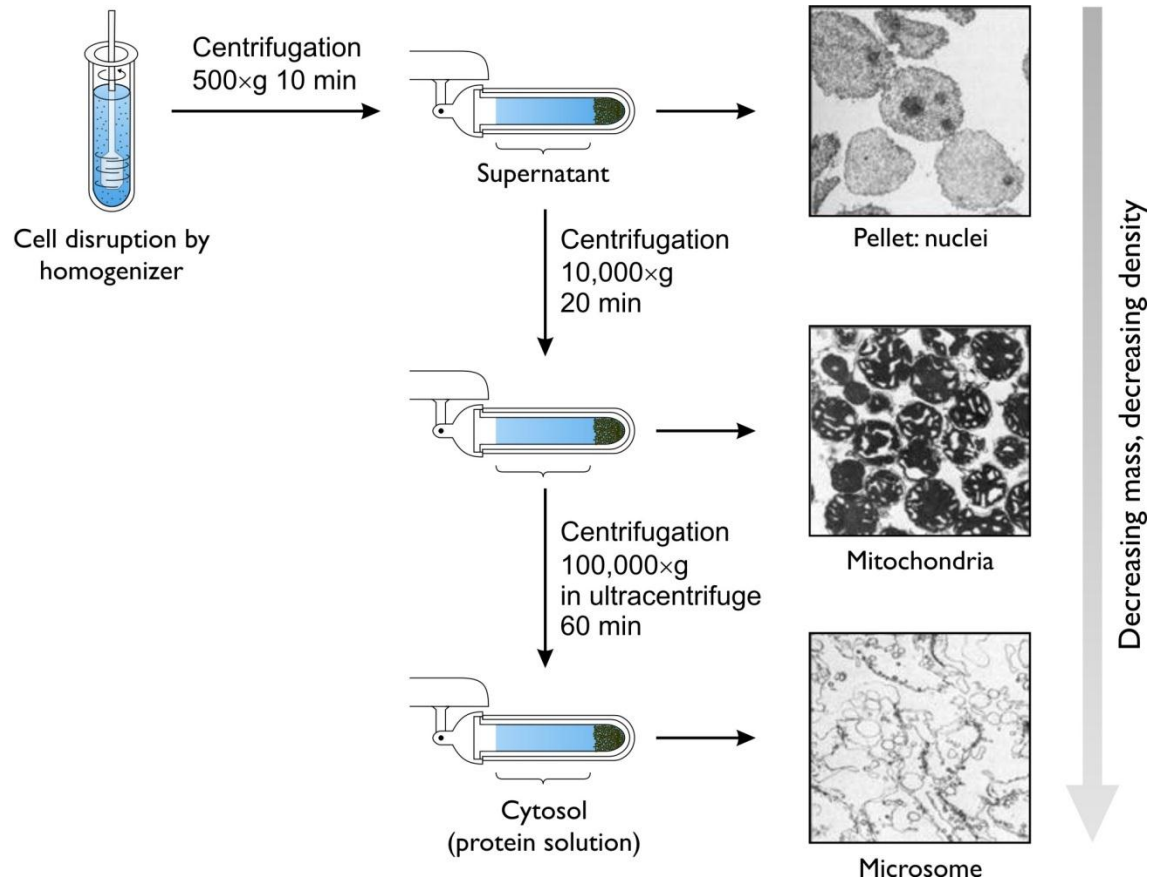
Centrifugation: *Prolonged, high speed*

Abscissa of frequency distribution: *Equilibrium density*

Differential centrifugation:

Separation based on the size of the particles.

This is not an equilibrium method.



Sedimentation equilibrium method

Here we wait, until the sedimentation and the Brownian motion reach an equilibrium. (so there will be a concentration profile in the tube)
We spin with medium speed, so there is a sedimentation, but not a complete pellet formation

This means, in equilibrium the net drag force is 0.

In thermal equilibrium, the **Boltzmann distribution** will describe the position of the particles in any force field:

$$\frac{n_1}{n_2} = e^{-\frac{\Delta E}{kT}}$$

In the energy term, we take into account the work of the forces.
If 1 and 2 denote distances r_1 and r_2 from the center of rotation, then

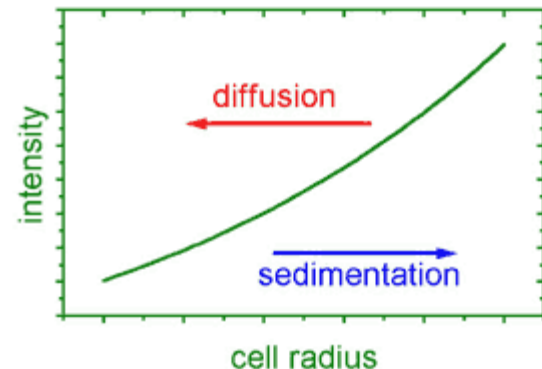
$$\Delta E = \frac{m}{2} (r_1^2 - r_2^2) \omega^2 \left(1 - \frac{\rho_{fluid}}{\rho_{particle}} \right)$$

Substituting into the Boltzmann formula and taking the logarithm yields:

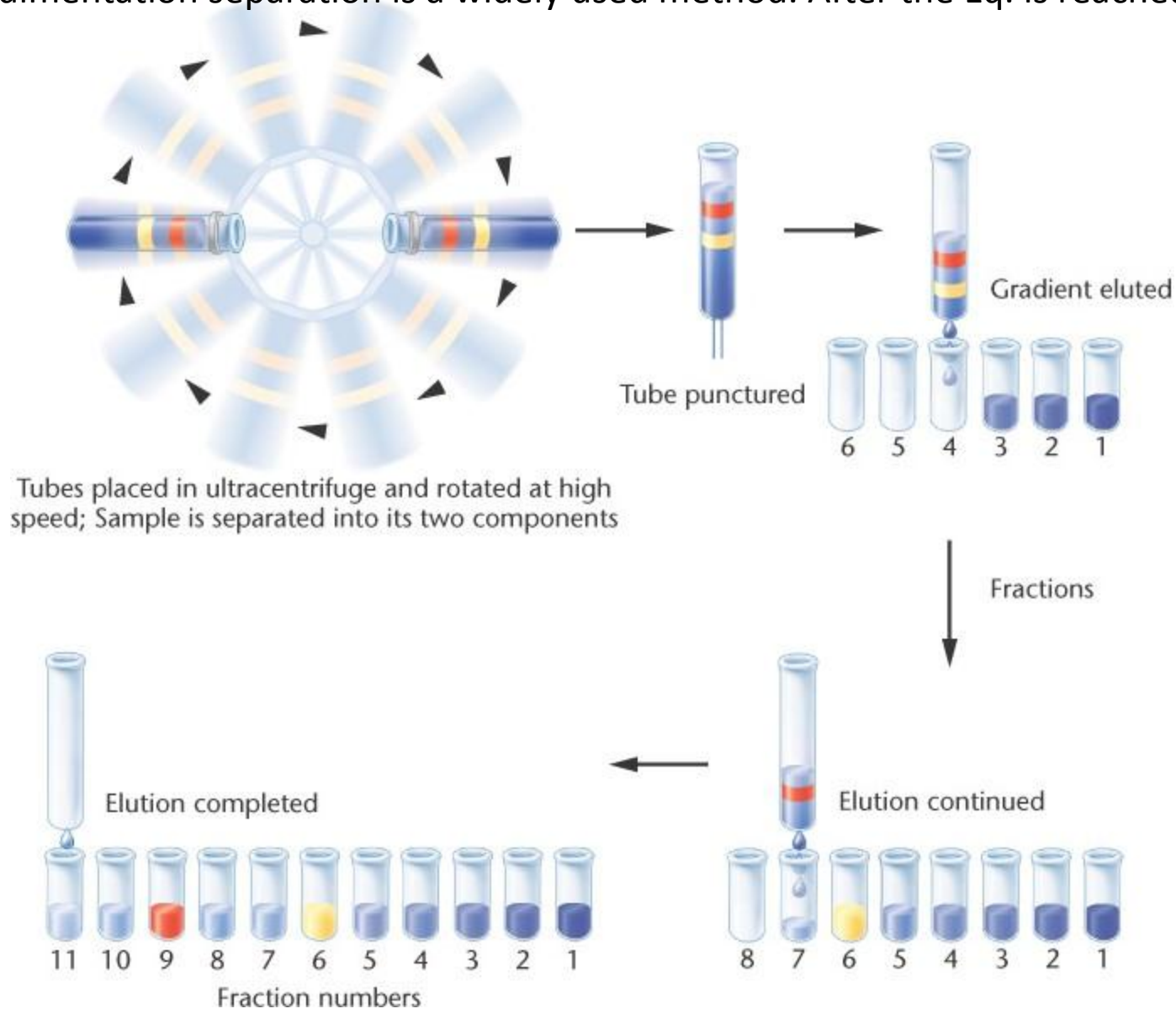
$$\ln\left(\frac{n_1}{n_2}\right) = \frac{m}{2kT} (r_1^2 - r_2^2) \omega^2 \left(1 - \frac{\rho_{fluid}}{\rho_{particle}}\right)$$

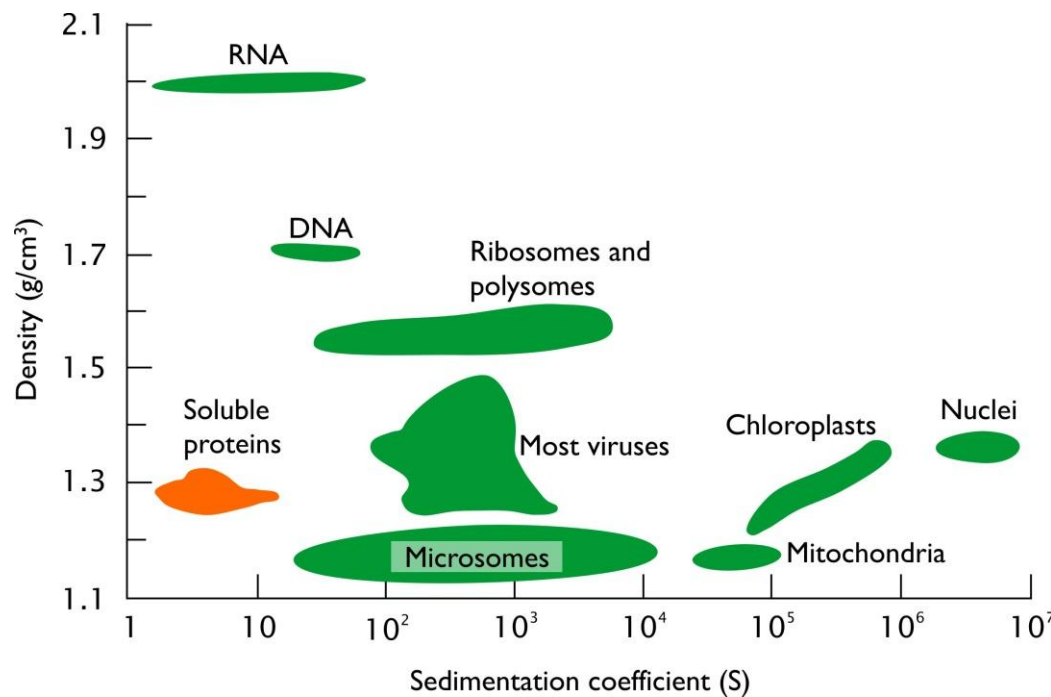
We can measure the concentrations (n_1, n_2) the densities, and we know the radii, so the mass can be calculated.

We do need the density, if that is unknown then at least 2 different solvents have to be used, so 2 independent equations can yield the 2 unknowns (m and density)



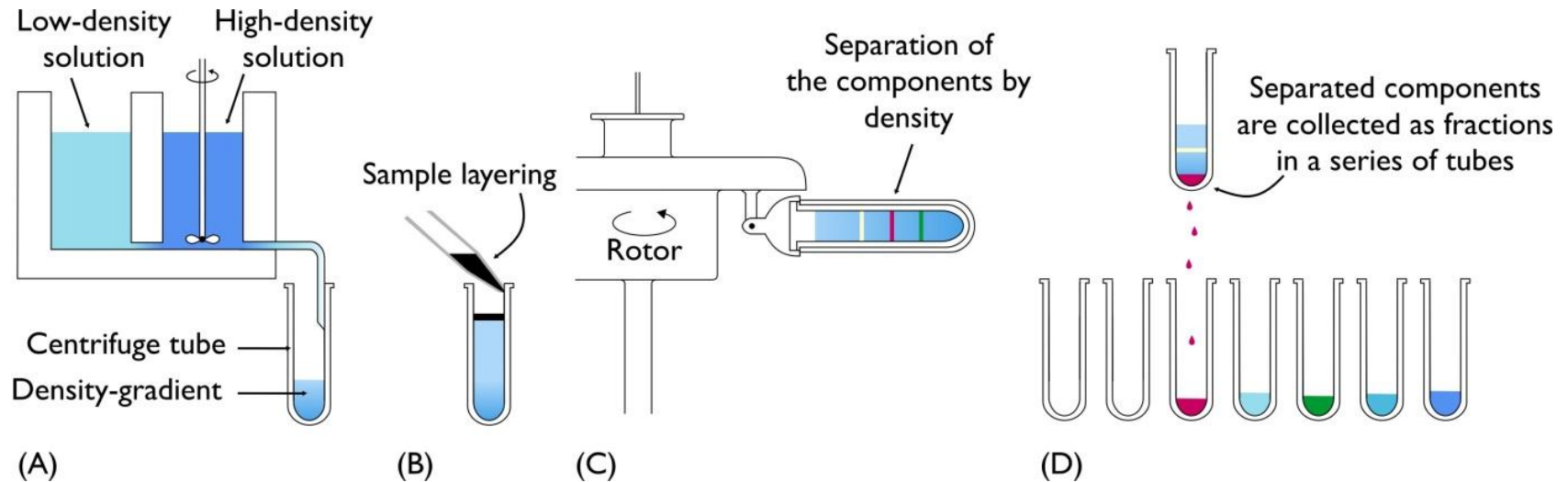
Sedimentation separation is a widely used method. After the Eq. is reached:





Based on S:
differential centrifugation

Then based on density:
gradient centrifugation



Equilibrium separation method is based on the usage of a density-gradient

Electrophoretic methods

If a molecule is charged, and placed into an electric field, then a force will act on it.

This force (analogous to the sedimentation analysis) will cause a separation of the particles/molecules.

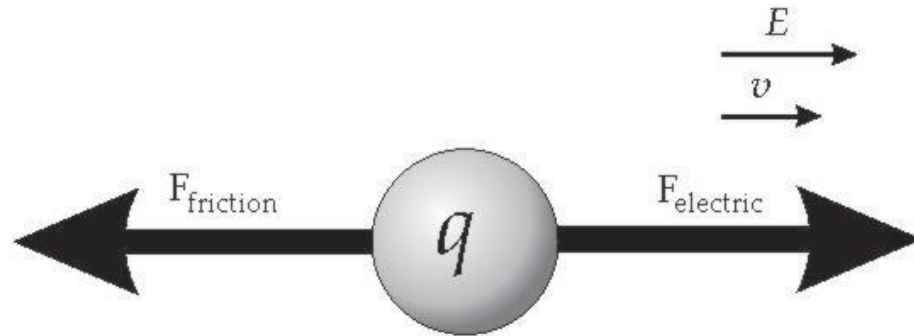
This is not an equilibrium method.

$$\mu_e = \frac{v}{E}$$

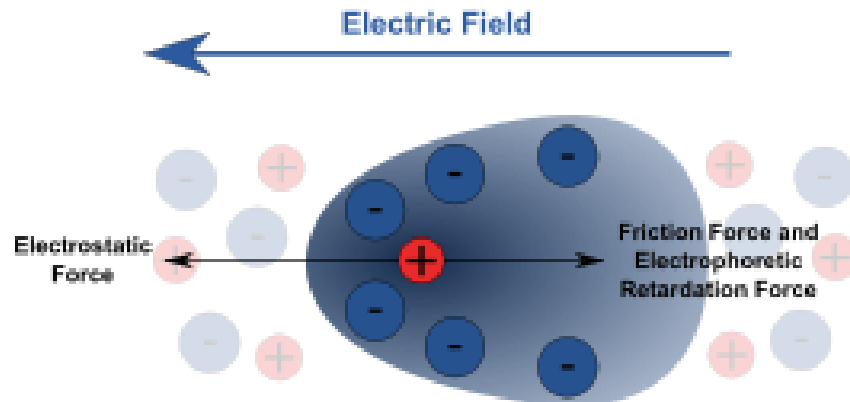
The **electrophoretic mobility** is defined by the velocity and the electric field creating that velocity.

This is specific for a given particle.

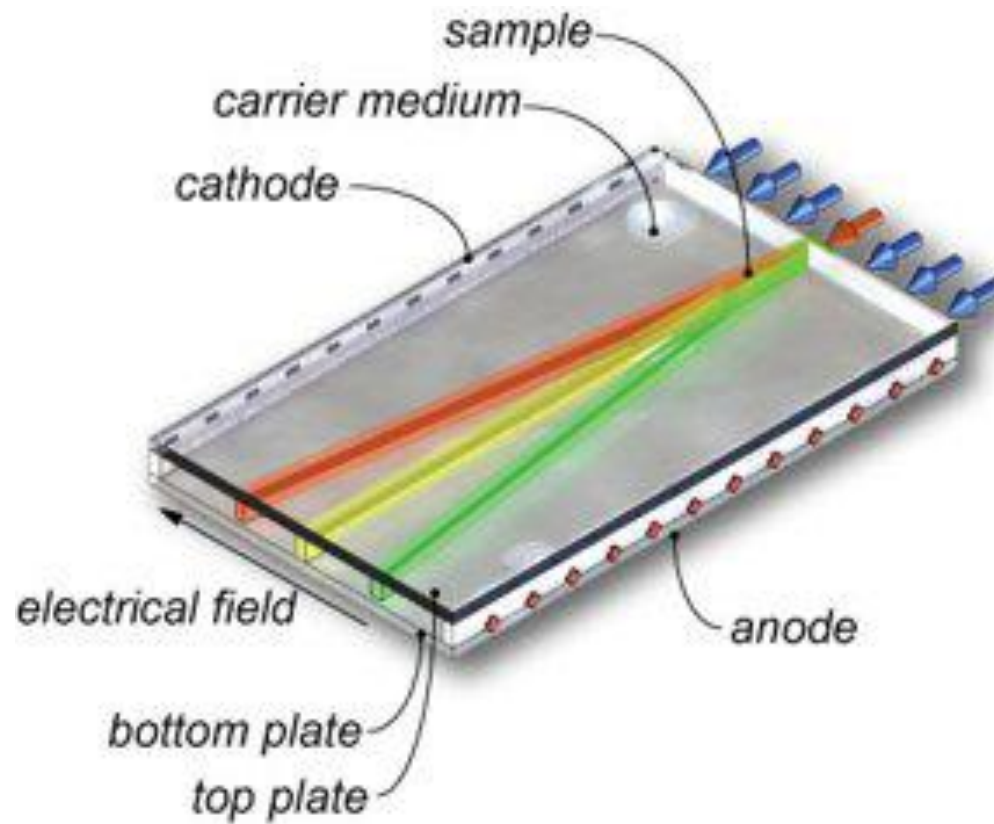
Forces in an uncharged solvent

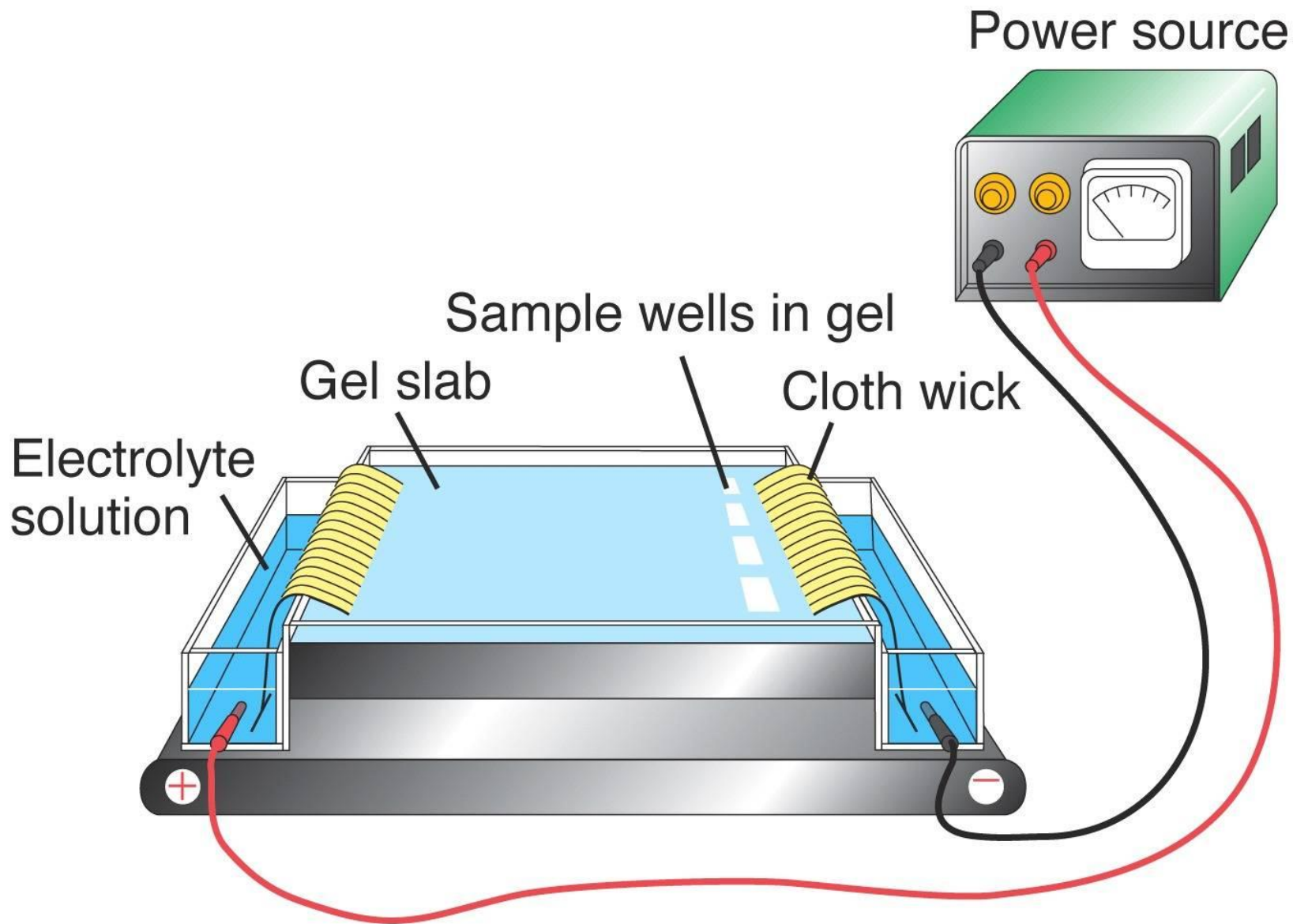


In a charged solvent there is retardation too:

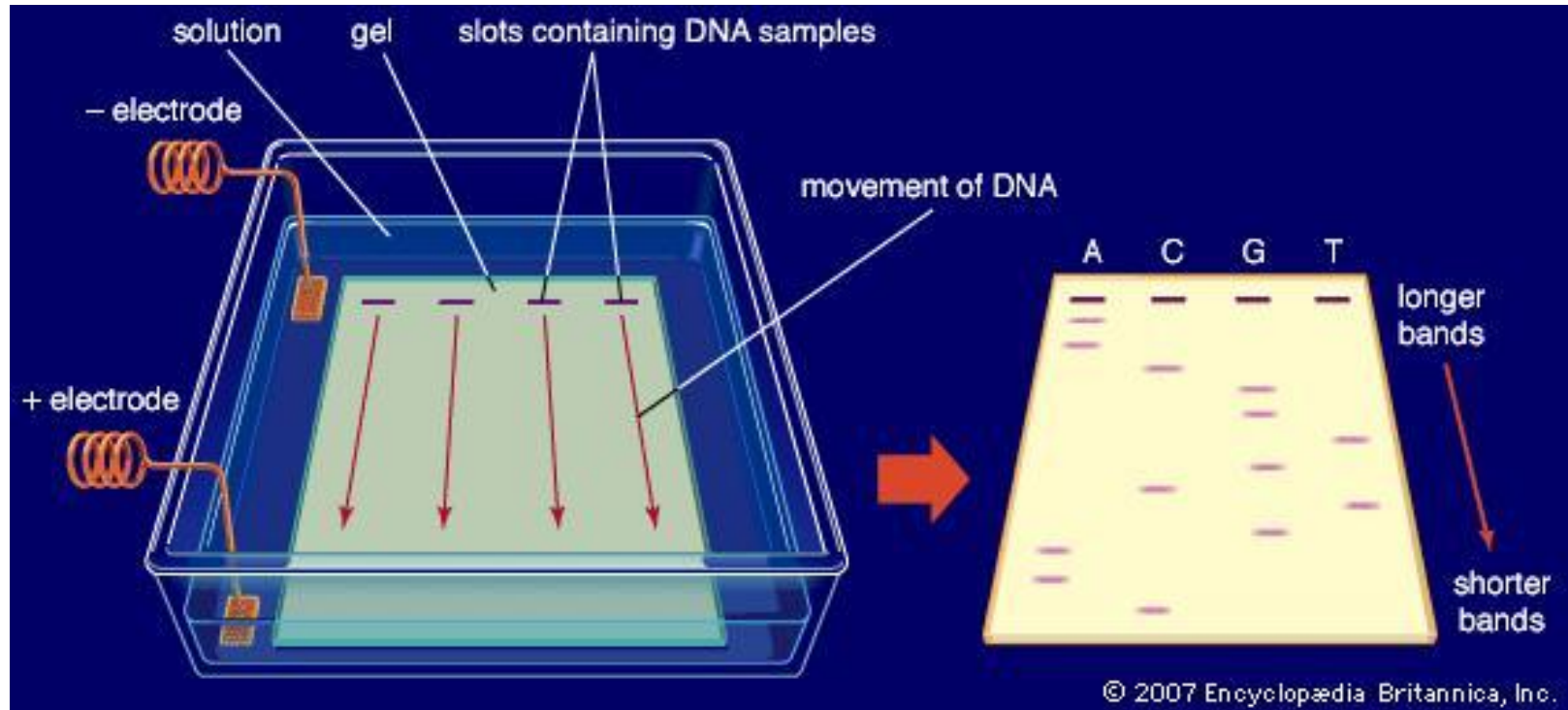


Free flow electrophoresis



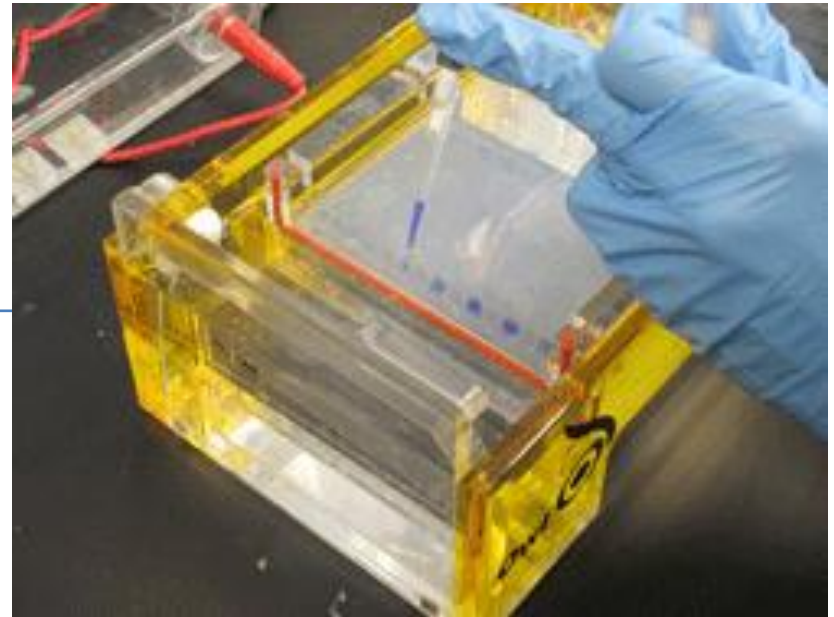


Gel electrophoresis

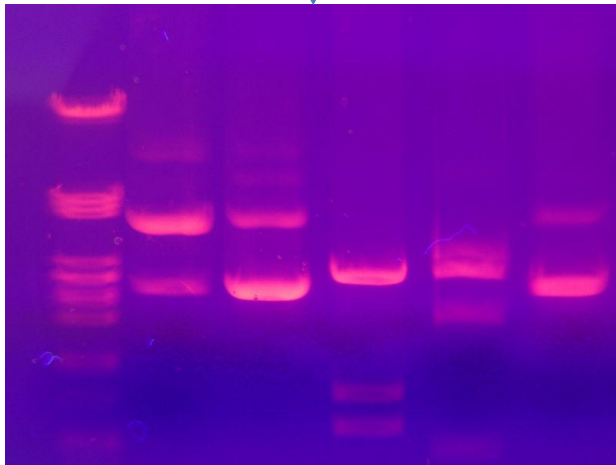
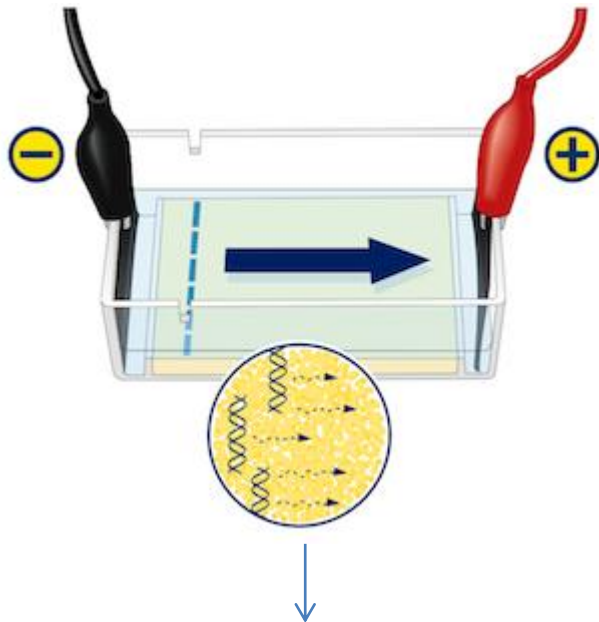


Gel electrophoresis

Load the gel



Run the gel



Label (here e.g. in-situ) and evaluate.

Labeling in a gel is not easy.

Blotting: one can transfer (and fix) the stripes on the gel onto a vinyl, or other membrane.

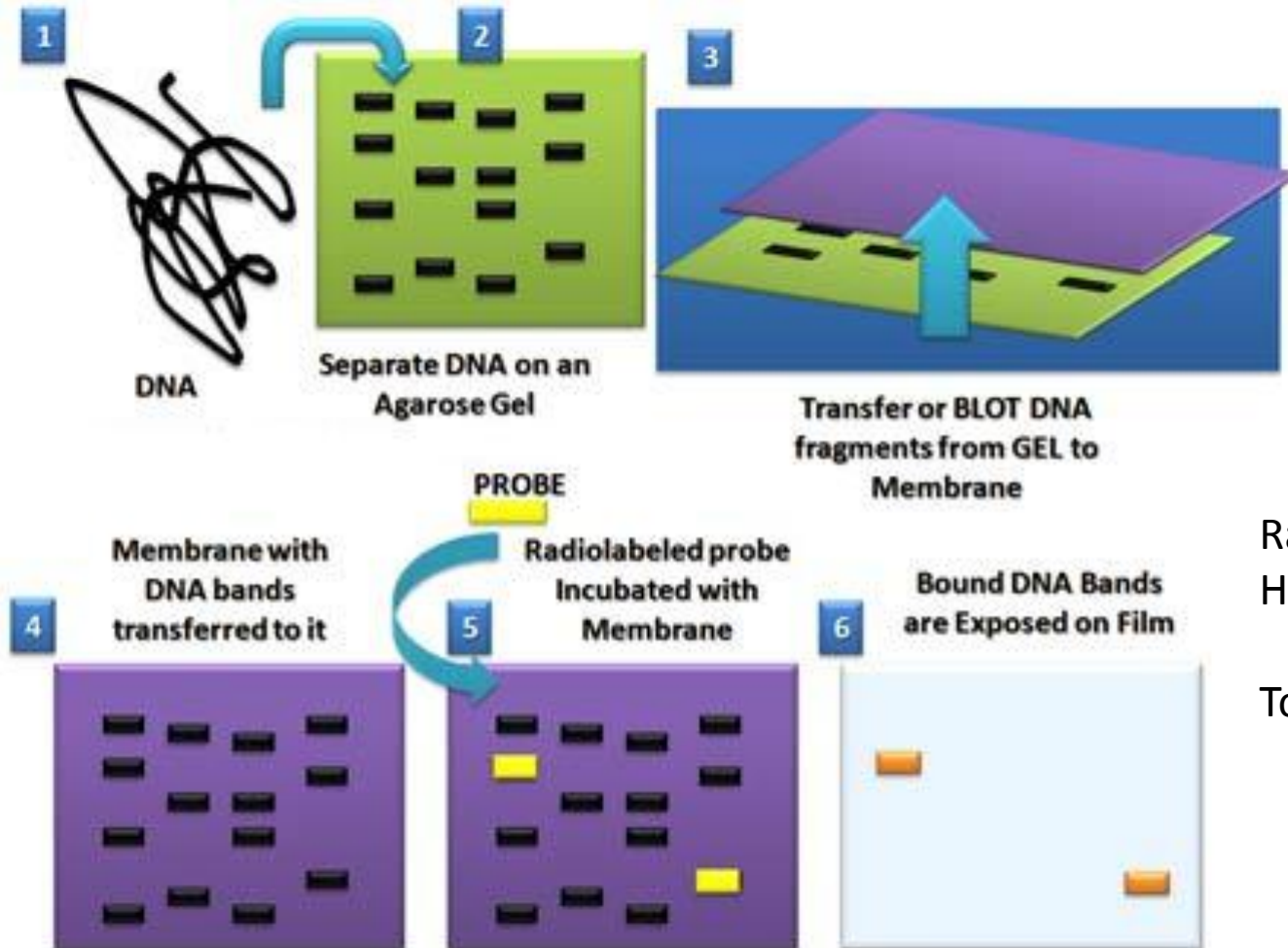
Visualization by staining is then done on the membrane.

This enables the use of complicated chemical/biochemical reactions.

Since the membrane has a higher density and viscosity than a gel, the diffusion is much less, so during the chemistry the bands will not “smear” as much.

Blotting is almost always done if the labeling takes considerable time (more than 1-2min)

Southern blot (Edwin Southern)

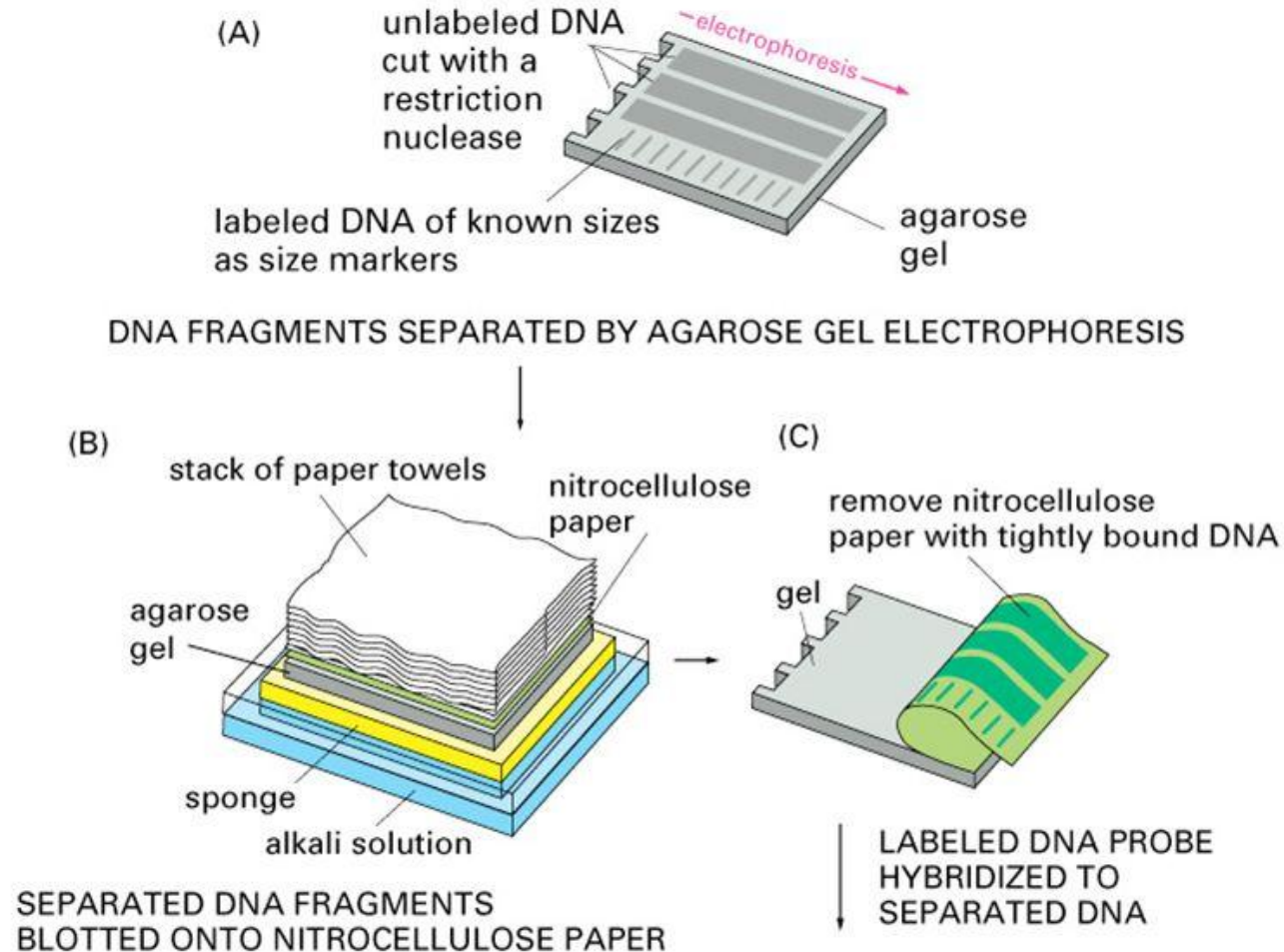


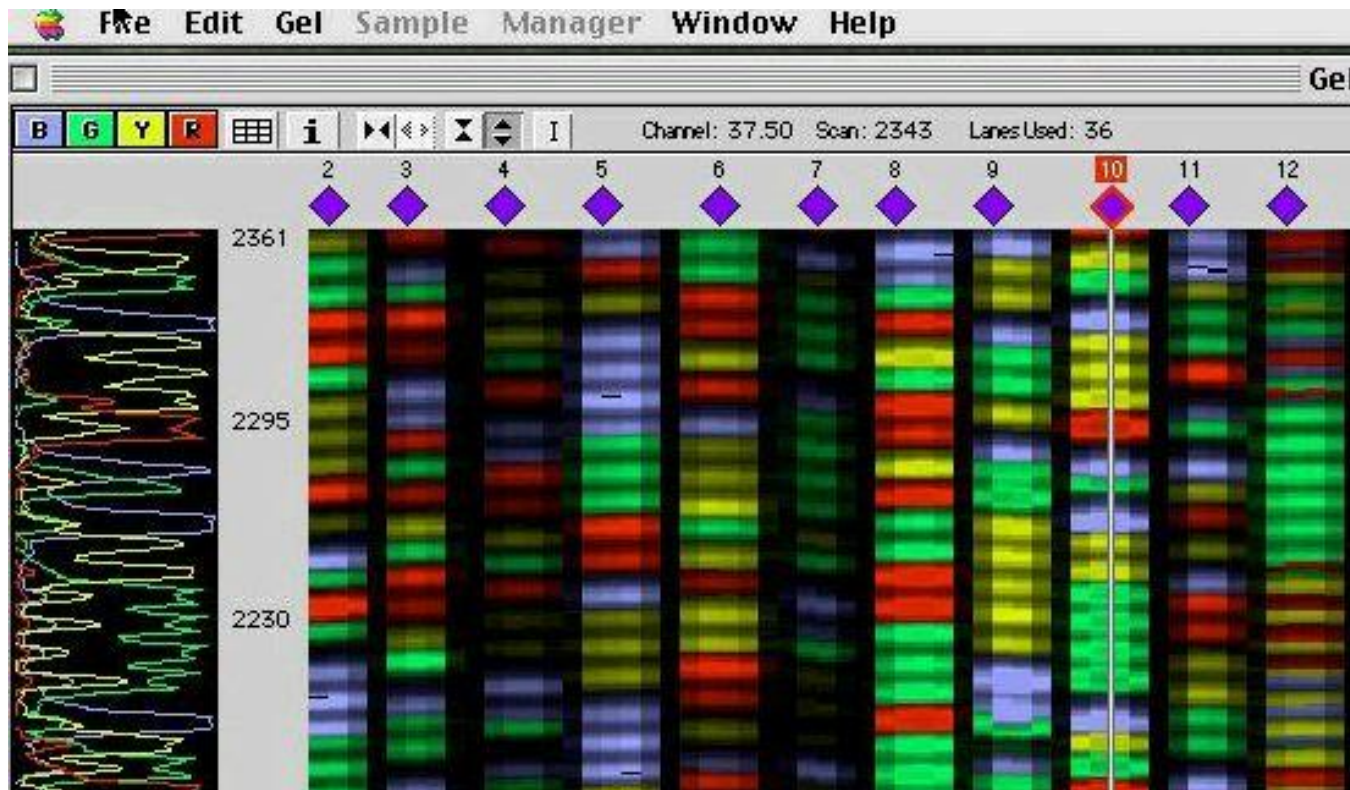
Radiolabeling:
High sensitivity!

Today: fluorescence
versions

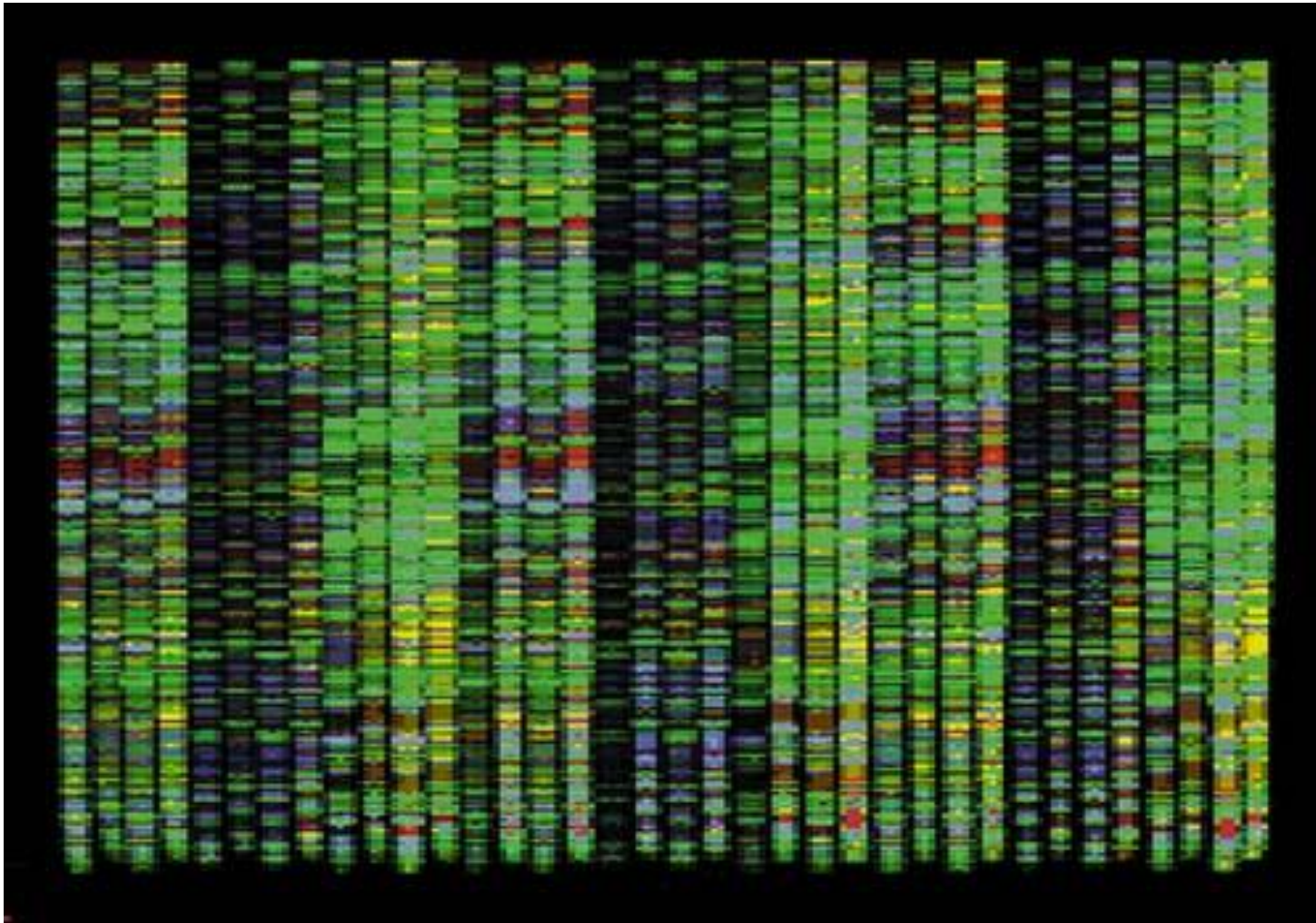
Some blotting details...

Southern Blot (DNA)



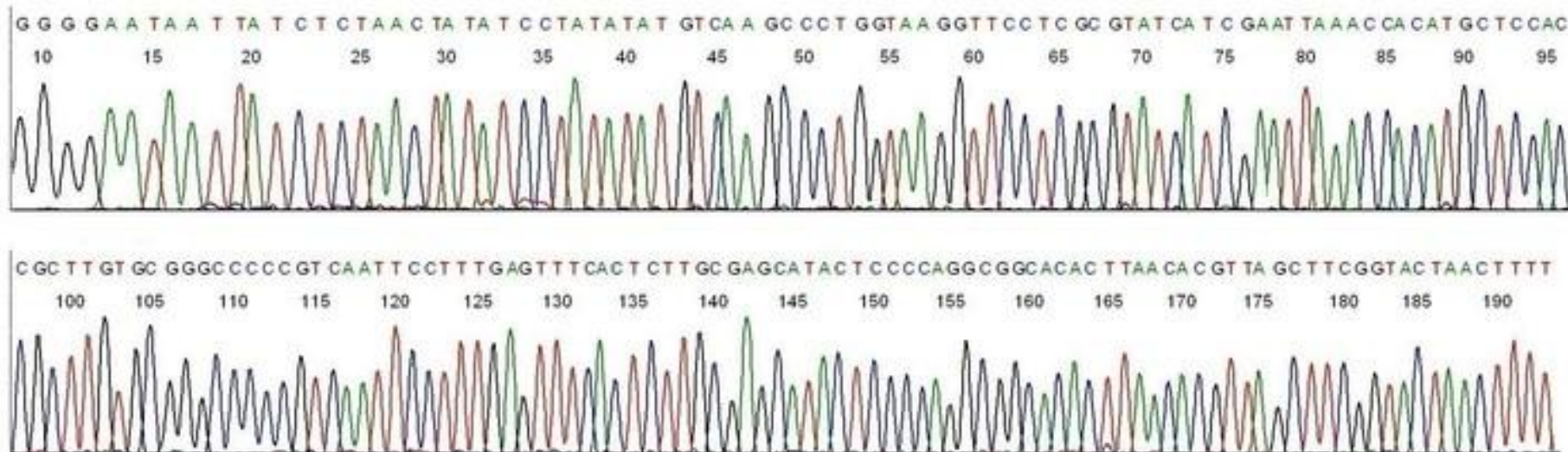


Fluorescence is much easier, and can be automated...



On a good quality gel a LOT of stripes can be differentiated...

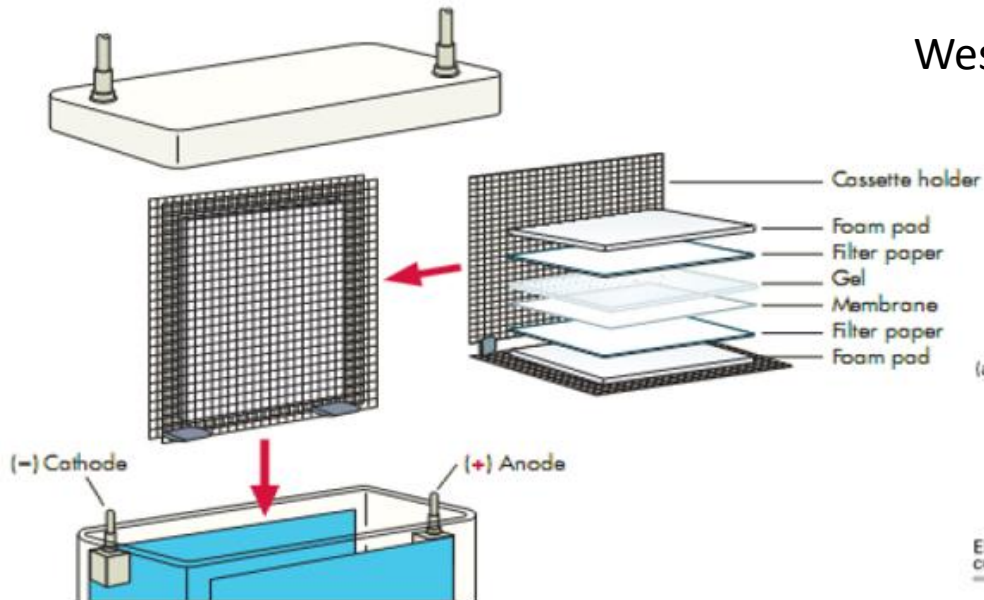
Used extensively in sequencing (getting the base sequence of DNA/RNA)



Borrelia burgdorferi CA382, complete genome
 Sequence ID: [gbKP005925.1](#) | Length: 910736 | Number of Matches: 1
 Range 1: 445107 to 445291 [GenBankGraphics](#)

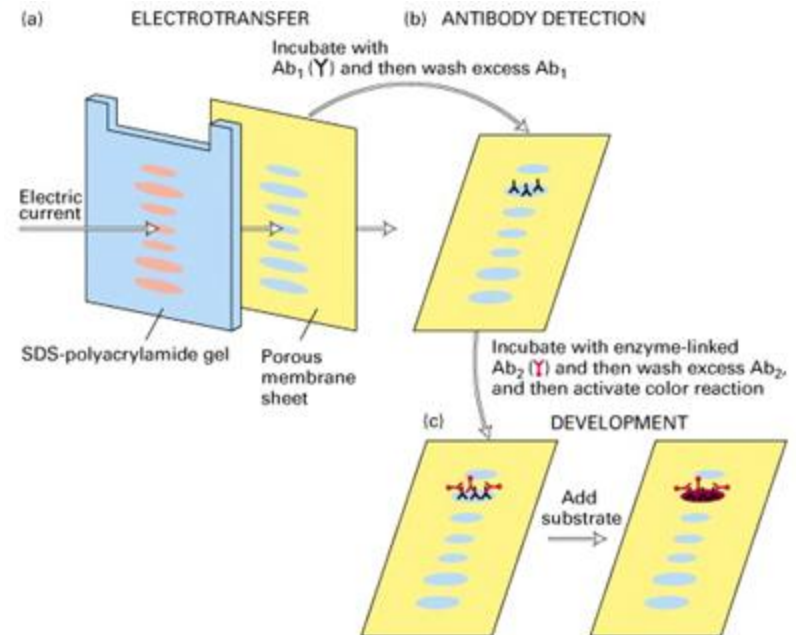
Score	Expect	Identities	Gaps	Strand
342 bits(185)	5e-91	185/185(100%)	0/185(0%)	Plus/Plus
Query 1	GGGGAATAATTATCTCTAACTATATCCTATATATGTCAAGCCCTGGTAAGGTTCCCTCGCG	60		
Sbjct 445107	GGGGAATAATTATCTCTAACTATATCCTATATATGTCAAGCCCTGGTAAGGTTCCCTCGCG	445166		
Query 61	TATCATCGAATTAAACCACATGCTCCACCGCTTGTGCGGGCCCCCGTCAATTCCTTTGAG	120		
Sbjct 445167	TATCATCGAATTAAACCACATGCTCCACCGCTTGTGCGGGCCCCCGTCAATTCCTTTGAG	445226		
Query 121	TTTCACTCTTGCAGCATACTCCCGAGCGGCACACTTAACACGTTAGCTTCGGTACTAA	180		
Sbjct 445227	TTTCACTCTTGCAGCATACTCCCGAGCGGCACACTTAACACGTTAGCTTCGGTACTAA	445286		
Query 181	CTTTT 185			
Sbjct 445287	CTTTT 445291			

Western and Northern blotting: the names come from the play with the original name of the southern blot.

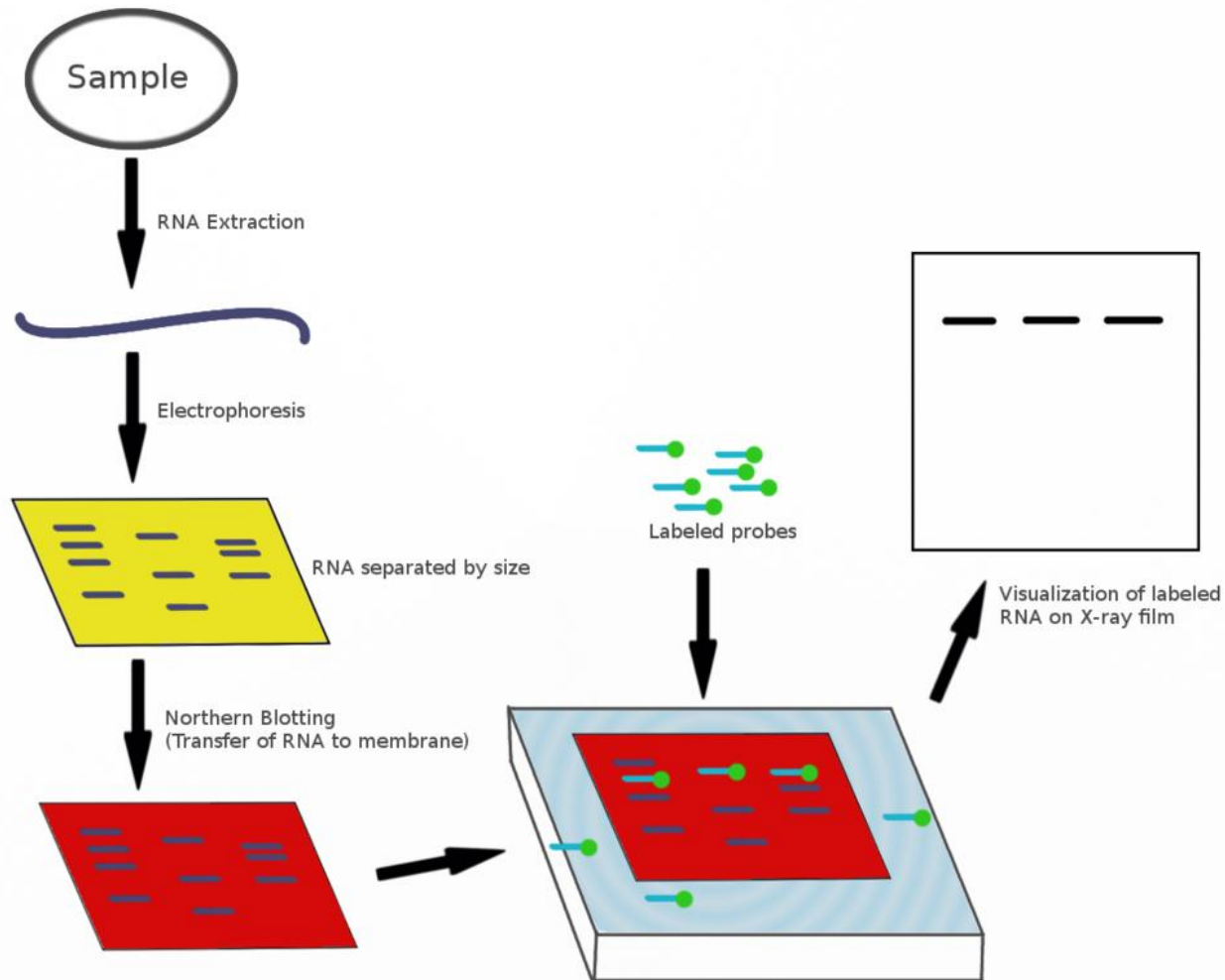


Western blot: protein detection

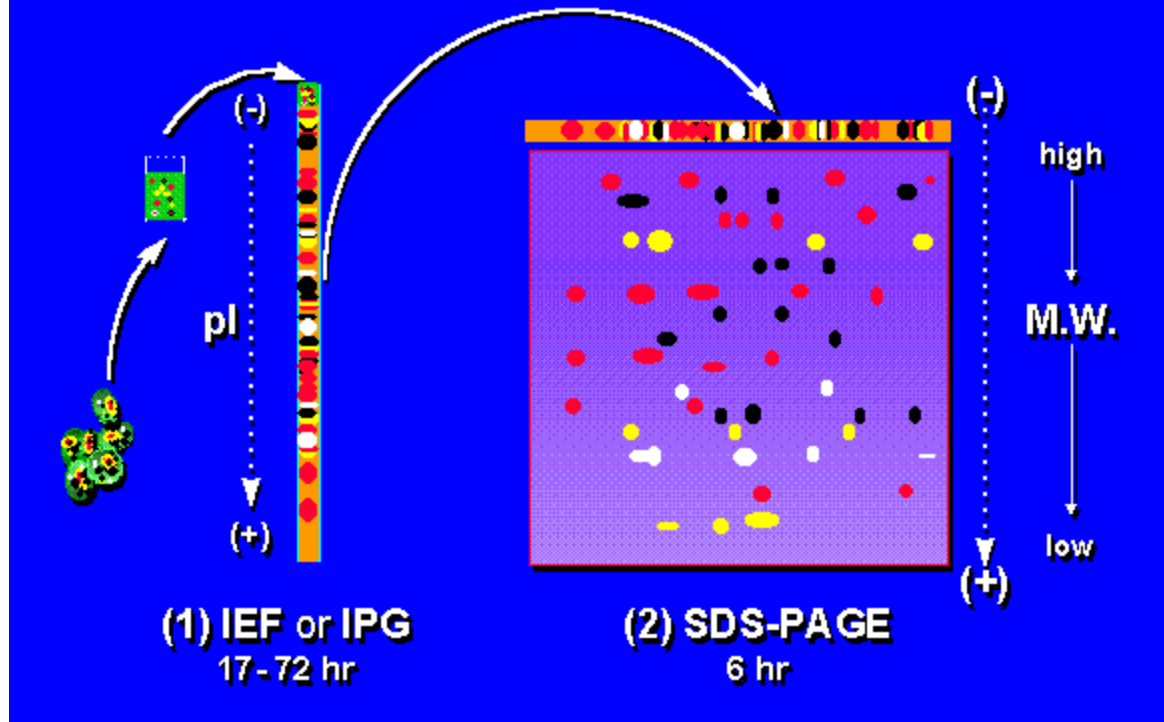
Proteins do not pair like DNA, but antibodies can be used for selective detection.



Northern blotting: detect RNA / expression levels



Two Dimensional Electrophoresis



Here we make TWO runs, the second goes 90 deg to the first one.
The chemical/physical conditions are different

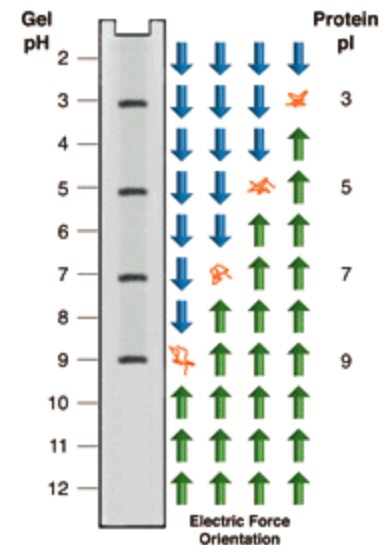
Isoelectric focusing

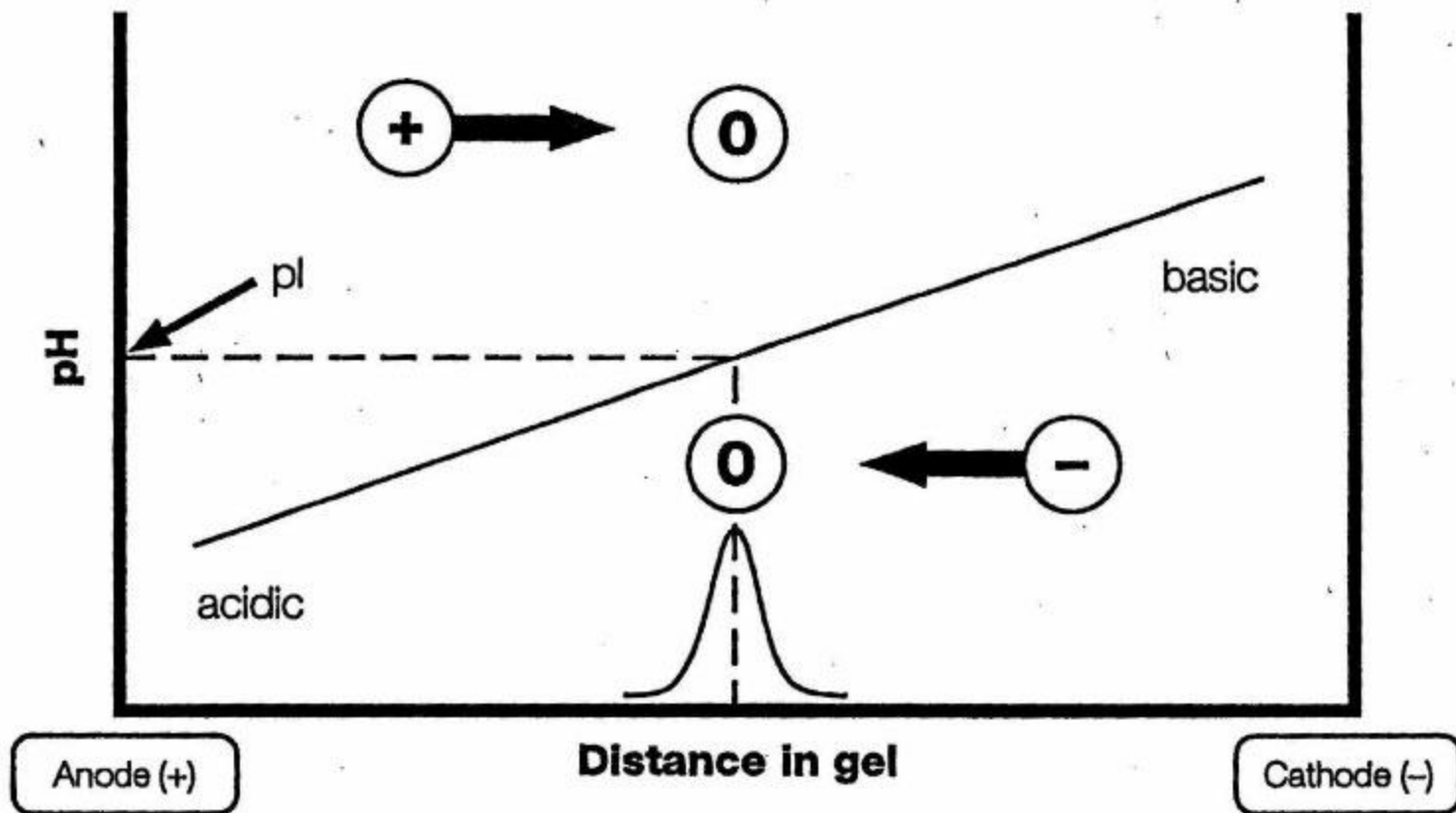
We use a gel, which has a pH gradient.

Due to the electrophoresis, the molecules will move towards the point in the gel, where the pH is equal to their *isoelectric point*.

At this point the molecules don't move any more, and are instead focused into sharp stripes.

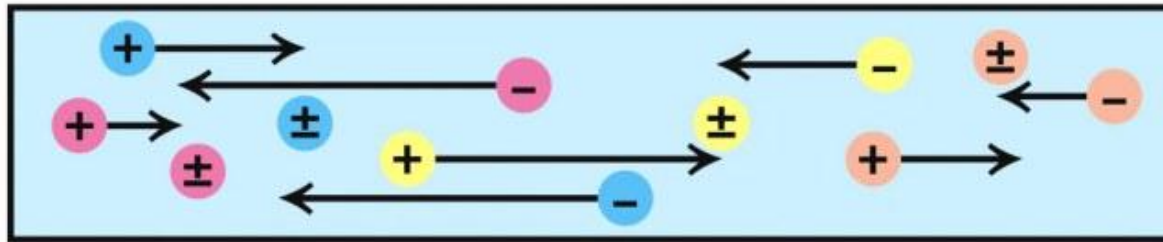
The technique is capable of separating proteins differing in a single elementary charge.





(A)

Low pH
(+)



High pH
(-)

(B)

Low pH
(+)



High pH
(-)

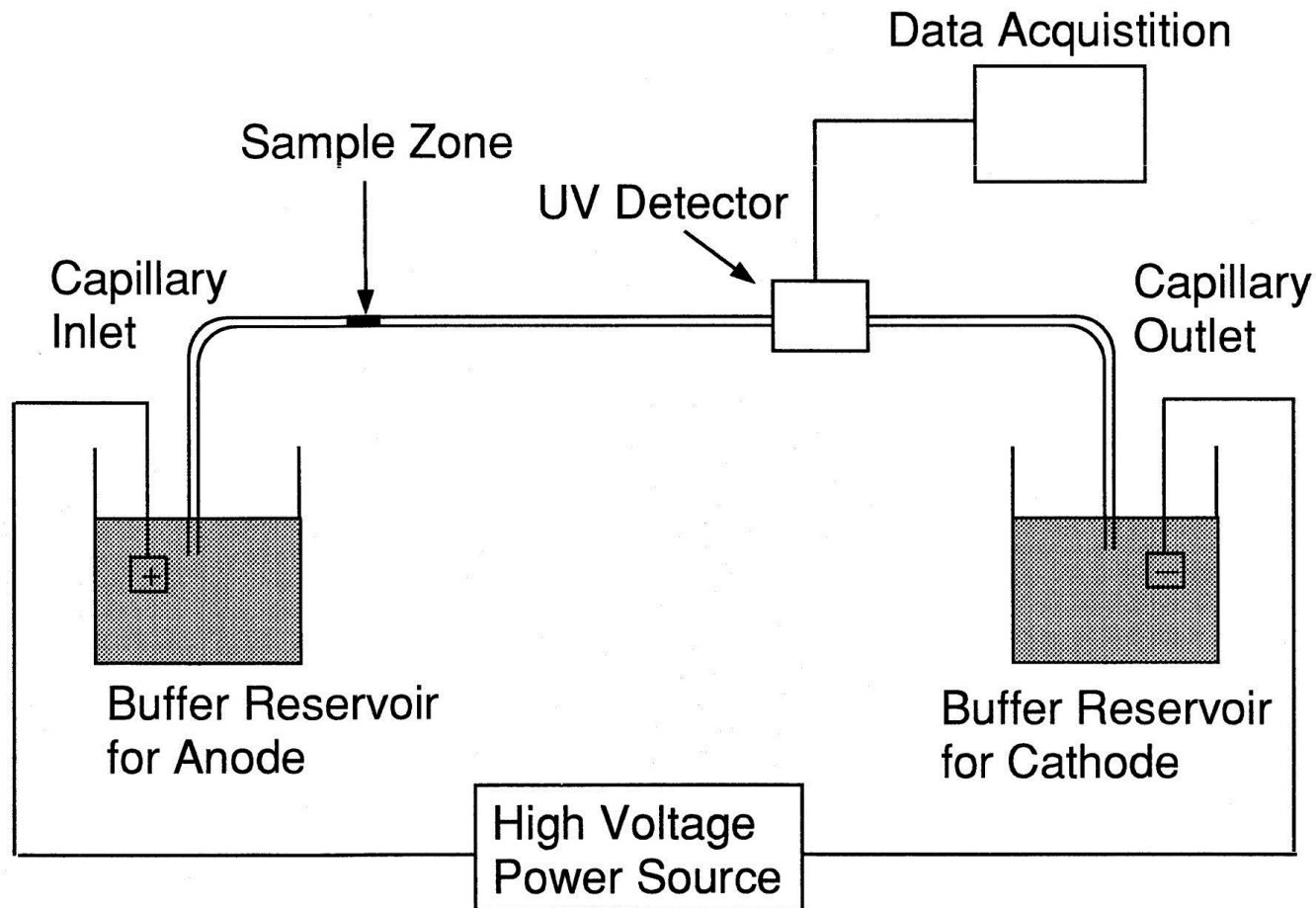
Figure 3.11

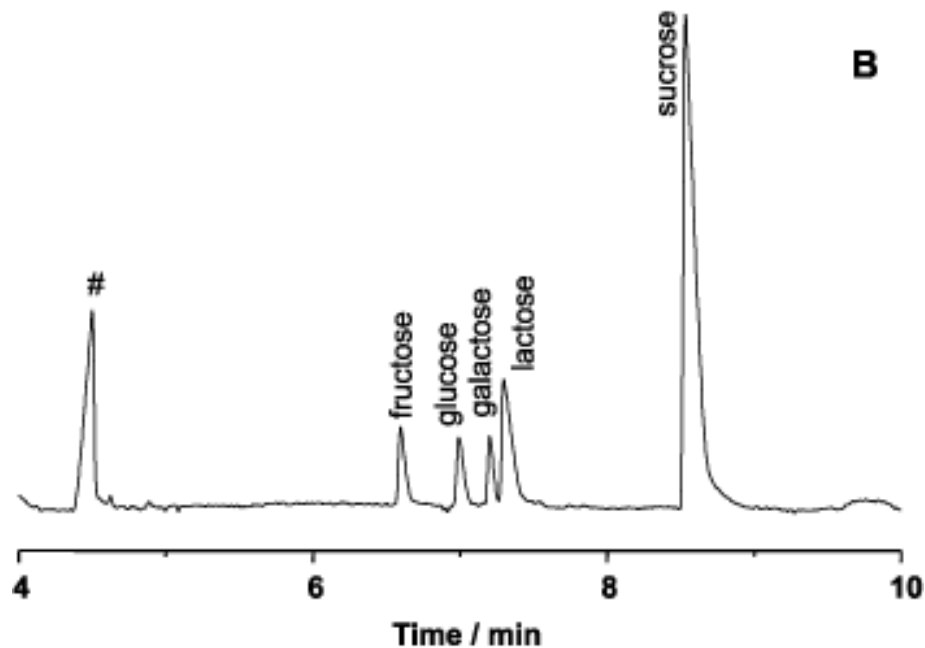
Biochemistry, Seventh Edition

© 2012 W. H. Freeman and Company

Capillary electrophoresis:

A chromatography technique, also useful for separation





Automated parallel analysis

Figure 7. Nutritional Applications of Capillary Electrophoresis: analysis of carboxylic acids in wine (A) and carbohydrates in yogurt (B). (A) 10 mmol L⁻¹ 3,5-dinitrobenzoic acid with 0.2 mmol L⁻¹ CTAB, pH 3.6; 254 nm. (B) 15 mmol L⁻¹ sorbate, 0.5 mmol L⁻¹ CTAB and 35 mol L⁻¹ NaOH; injection 3.4 kPa/15 s, 30 °C, -18 kV and 254 nm. (#) is a non-identified peak.

