



Physical basis of dental material science 10.

Thermal and optical properties

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Thermal properties

- temperature: proportional to the internal energy of the material.
(unit: K, °C, in physics K is used mainly)
- Heat uptake/loss – exchange between the object and the environment.



Heat capacity (C):
(energy that increases the temperature by 1 K)

$$C = \frac{\Delta Q}{\Delta T}$$

ΔQ – exchanged thermal energy
 v – no. of mols
 m – mass
 ΔT – temperature change

molar heat capacity (c_v):
(heat capacity for one mol)

$$c_v = \frac{C}{v}$$

c_p – measured at constant pressure
 c_v – measured at constant volume

specific heat capacity (c):
(heat capacity for unit mass)

$$c = \frac{C}{m}$$

$$c_p > c_v$$

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Specific heat capacity

High specific heat of the water is important from the viewpoint of the life! (thermal stability)



specific heat capacity of some dental materials:

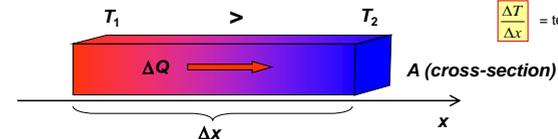
material	c (J/(kg·K))
Enamel	750
Dentin	1260
Water	4190
Amalgam	210
Gold	126
Porcelain	1100
Glass	800
PMMA	1460
ZnPO ₄	500

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Thermal conduction

$$\Delta T = T_2 - T_1$$

$$\frac{\Delta T}{\Delta x} = \text{temperature gradient}$$

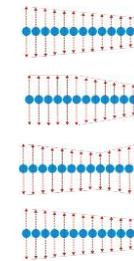


How is the energy transported?

lattice oscillation

In metals e.g. motion of the free electrons.

time increases



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Thermal conductivity

Fourier-law

$$\frac{\Delta Q}{\Delta t} = -\lambda A \frac{\Delta T}{\Delta x}$$

λ — thermal conductivity
 $J/(s \cdot m^2 \cdot K/m) = W/(m \cdot K)$

Characterizes well the phenomenon in the case of stationary flow!
 (stationary — the parameters are constant in time)

Thermal conductivity of some dental material:

material	λ (W/(mK))
Enamel	0.9
Dentin	0.6
Water	0.44
Amalgam	23
Gold	300
Porcelain	1
Glass	0.6-1.4
Acrylate	0.2
PMMA	0.2-0.3
ZnPO ₄	1.2

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Non-stationary case

$$D = \frac{\lambda}{c_p \rho}$$

D — thermal diffusivity (m²/s)
 (may be different at the different points of the material)

ρ — density
 c_p — specific heat capacity at constant pressure

Thermal diffusivity of some dental materials:

material	λ (W/(mK))	D (10 ⁻⁶ m ² /s)
Enamel	0.9	0.5
Dentin	0.6	0.2
Water	0.44	0.14
Amalgam	23	9.6
Gold	300	118
Porcelain	1	0.4
Glass	0.6-1.4	0.3-0.7
Acrylate	0.2	0.1
PMMA	0.2-0.3	0.12
ZnPO ₄	1.2	0.3

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Thermal expansion

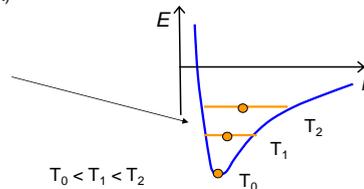
Linear expansion:

$$\frac{\Delta l}{l_0} = \alpha \Delta T$$

$$l = l_0(1 + \alpha) \Delta T$$

α — coefficient of thermal expansion (1/K)

Increasing temperature results increasing oscillation of particles.
 This may be observed as increasing size.



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Volumetric thermal expansion

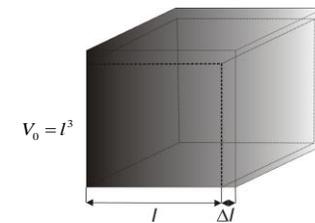
$$\frac{\Delta V}{V_0} = \beta \Delta T$$

$$V = V_0(1 + \beta) \Delta T$$

β — volumetric thermal expansion coefficient (1/K)

for isotropic materials:

$$\beta \approx 3\alpha$$



Isotropic: properties are independent from the direction

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Effect of thermal expansion

Larger expansion
(compression)



Smaller expansion
(tension)



Cave is formed



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The coefficient of thermal expansion of some dental materials :

Material	$\alpha (10^{-6} 1/K)$
Enamel	11.4
dentin	8.3
Gold	14,2
Gold alloys	11-16
Amalgam	≈ 25
Porcelain	4-16
Acrylate	90
Glass	8
PMMA	90-160
Silicon	100-200
gypsum	15-20
wax	300-500

different expansion \Rightarrow stress!



Conservative dentistry!

Implants, braces.

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Optical properties

Color of the teeth



Color of the amalgam

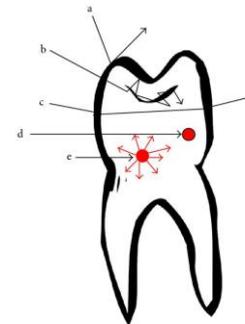


Optical phenomena

Absorption
Emission
Reflection
Scattering

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Light and the tooth



a - reflection
b - scattering
c - transmission and refraction
d - absorption
e - absorption and fluorescence

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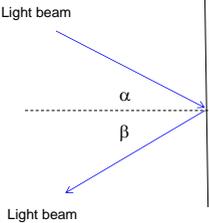
Geometrical optics

- light propagates in straightline.

reflection




$\alpha = \beta$

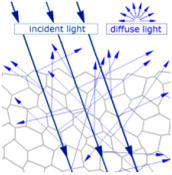
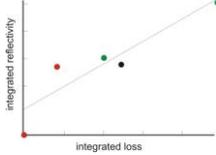


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Reflection



Determination of mineral loss

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Refraction

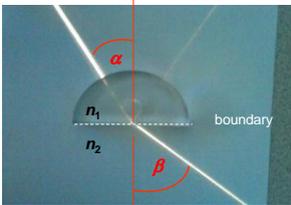
Snell's law:

$$\frac{\sin \alpha}{\sin \beta} = \frac{c_1}{c_2} = \frac{n_2}{n_1} = n_{21}$$

(relative) refractive index

→

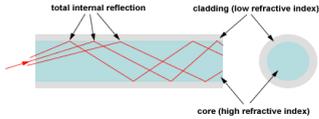





limiting angle

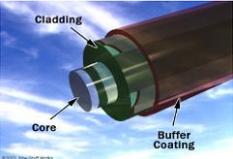
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Application of the total internal reflection



optical fiber



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Application of the total internal reflection

mirage:



dentistry



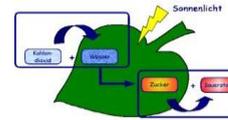
endoscopy



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Energy transport

Photosynthesis is the base of the life.



Chloroplast absorbs the light energy and stores in molecules as chemical energy.

Crude oil contains the stored energy of the Sun.



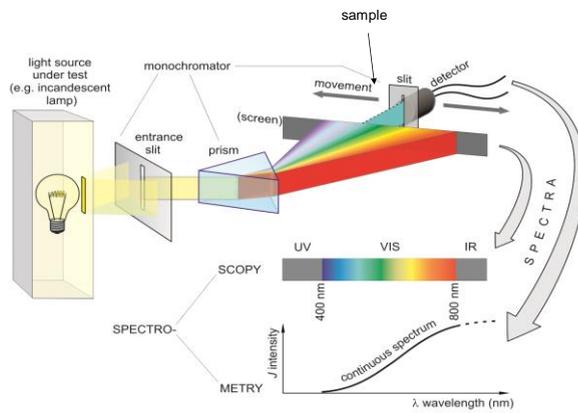
Solar cell converts the light energy into electric one.



The absorbed energy in the skin results reddening.

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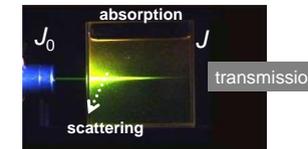
Spectroscopy and spectrometry



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Interaction to the matter

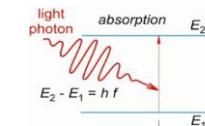
Consequence
 $J < J_0$



Attenuation: decreasing intensity
attenuation = scattering + absorption



Inhomogeneity of the refractive index in the material!



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Light scattering

elastic scattering
(λ, f, ε are constant)



Rayleigh-scattering
particle size $\ll \lambda$

scattered intensity $\sim \frac{1}{\lambda^4}$

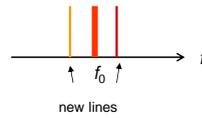
blue sky: blue is scattered better.
(wavelength is shorter)

Mie-scattering
size of the scattering particle $\geq \lambda$
(no strong λ dependency)
(white clouds)



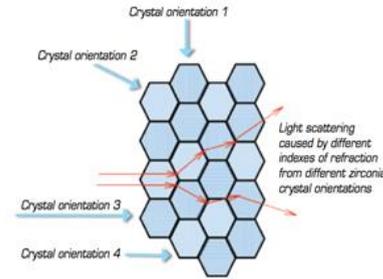
inelastic scattering
(λ, f, ε are not constant)

Raman-scattering



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Light scattering



Scattering on crystals.

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Attenuation law

if the scattering is negligible



attenuation ~ absorption

transmission

$$\hat{T} = \frac{J}{J_0} (\cdot 100 \%)$$

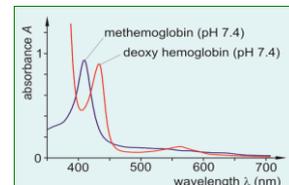
absorbance

$$A = \lg \frac{J_0}{J}$$

attenuation coefficient

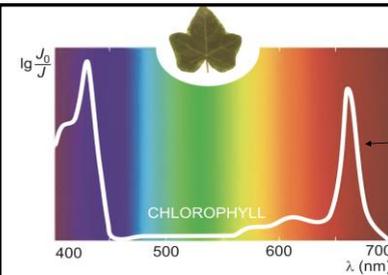
$$J = J_0 \cdot e^{-\mu \cdot x}$$

absorption spectrum: $A(\lambda)$



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Absorption spectra



Green color of the plants is due to the absorption in red.

Color vision

The colour of a material depends on the absorption.



Absorption Spectra of Human Visual Pigments

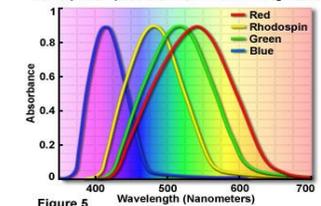
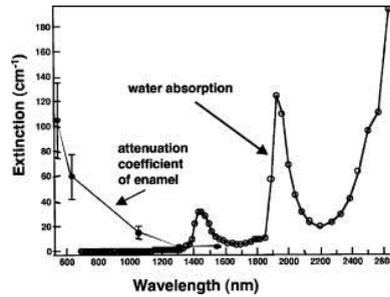


Figure 5

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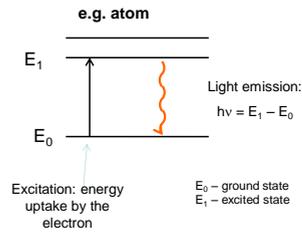
Absorption of the natural materials



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Luminescence

Light emission over the thermal radiation.
Light emission after excitation.



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Application of luminescence

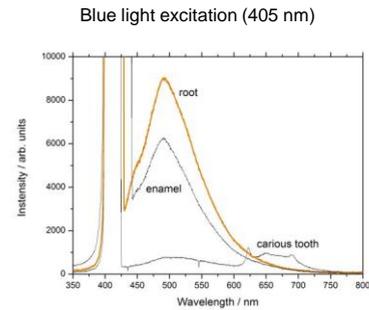
excitation	name: -luminescence	example
light	photo-	quinine-sulphate, phosphor, ...
X-ray	X-ray	Nal(Tl)
radioactive radiation	radio-	Nal(Tl)
electric field	electro-	mercury-lamps
mechanical effect	tribo-	sugarcube
chemical reaction	chemo- (bio-)	firebug
heat	thermo-	CaSO ₄ (Dy)



+ materials analysis, structure of biological macromolecules, fluorescence microscopy, sensors, monitors, radiation detectors, ...

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Luminescence spectrum



less intensity

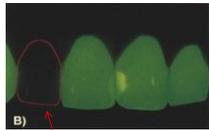


higher intensity



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Dental application



Intensity: depends on the thickness of the plaque.

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Transparency

transparent - translucent - opaque



transparent: light passes through the material without being scattered.

translucent: diffuse transparency, the light is scattered.

opaque: not transparent, diffuse reflection

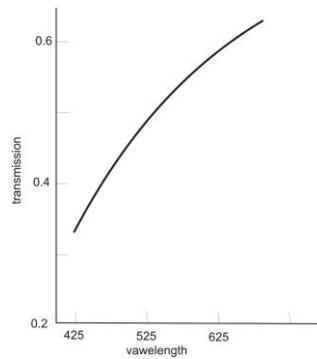
Examples:

transparent: plate glass, water

translucent: oil paper, ice, some plastics...

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Transparency of the enamel

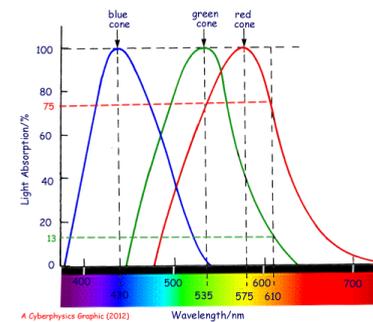


Transmission:

$$T = J/J_0$$

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Why can we see colors?



Color theory:

Every color may be produced mixing appropriate 3 colors.

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Colors

fluorescence after absorption

color 3

Depends on the spectrum of the incident light!

absorption inside the substance

incident light

reflected light

transmitted light

scattered light

opalescence

color 1

color 2

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Color theory

```

    graph TD
      color --> chromatic_color[chromatic color]
      color --> achromatic_color[achromatic color]
      chromatic_color --> primary_color[primary color]
      chromatic_color --> mixed_color[mixed color]
      primary_color --> additive[additive]
      primary_color --> subtractive[subtractive]
      additive --> RGB[RGB]
      RGB --> R[R]
      RGB --> G[G]
      RGB --> B[B]
      subtractive --> CMYK[CMYK]
      CMYK --> C[C]
      CMYK --> M[M]
      CMYK --> Y[Y]
      CMYK --> K[K]
      achromatic_color --> white_gray_black[white, gray, black]
  
```

additive

subtractive

RGB

CMYK

1, 3, 5

2, 4, 6

- 1 - red
- 2 - yellow
- 3 - green
- 4 - cyan
- 5 - blue
- 6 - magenta

white, gray, black

primary color: sets of colors that can be combined to make a color.

additive color model: involves light emitted directly from a source.

subtractive color model: mixing of paints, dyes, inks, and natural colorants.

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Color properties

„color space”: 3 coordinates to describe the color

Hue: refers to a *pure* color.
An element in the color wheel (down).

Saturation: perceived intensity of a specific color.

Brightness: the perception elicited by the luminance of a visual target.

regular units:
hue: °
saturation: %

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Color of teeth

sickness or antibiotics during the development.

necroses

filling

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