



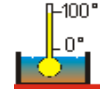
## Physical basis of dental material science 10.

Thermal and optical properties

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## Thermal properties

- temperature: proportional to the internal energy of the material.  
(unit: K, °C, in physics K is used mainly)
- Heat uptake/loss – exchange between the object and the environment.



**Heat capacity (C):**  
(energy that increases the temperature by 1 K)

$$C = \frac{\Delta Q}{\Delta T}$$

$\Delta Q$  – exchanged thermal energy  
 $\nu$  – no. of mols  
 $m$  – mass  
 $\Delta T$  – temperature change

**molar heat capacity ( $c_v$ ):**  
(heat capacity for one mol)

$$c_v = \frac{C}{\nu}$$

**specific heat capacity (c):**  
(heat capacity for unit mass)

$$c = \frac{C}{m}$$

$c_p$  – measured at constant pressure  
 $c_v$  – measured at constant volume

$$c_p > c_v$$

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## Specific heat capacity

High specific heat of the water is important from the viewpoint of the life! (thermal stability)



specific heat capacity of some dental materials:

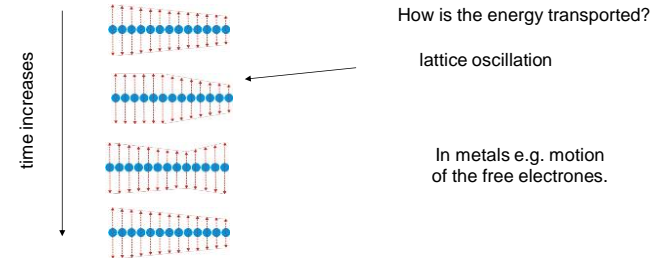
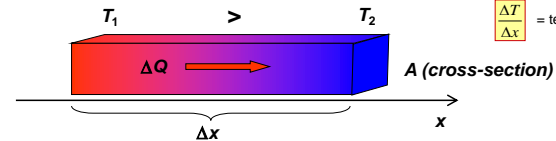
material	$c$ (J/(kg·K))
Enamel	750
Dentin	1260
Water	<b>4190</b>
Amalgam	210
Gold	126
Porcelain	1100
Glass	800
PMMA	1460
ZnPO <sub>4</sub>	500

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## Thermal conduction

$$\Delta T = T_2 - T_1$$

$$\frac{\Delta T}{\Delta x} = \text{temperature gradient}$$



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## Thermal conductivity

Fourier-law

$$\frac{\Delta Q}{\Delta t} = -\lambda A \frac{\Delta T}{\Delta x}$$

$\lambda$  — **thermal conductivity**  
J/(s·m<sup>2</sup>·K/m) = W/(m·K)

Characterizes well the phenomenon in  
the case of stationary flow!  
(stationary – the parameters are  
constant in time)

Thermal conductivity of some  
dental material:

material	$\lambda$ (W/(mK))
Enamel	0.9
Dentin	0.6
Water	0.44
Amalgam	23
Gold	300
Porcelain	1
Glass	0.6-1.4
Acrylate	0.2
PMMA	0.2-0.3
ZnPO <sub>4</sub>	1.2

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## Non-stationary case

$$D = \frac{\lambda}{c_p \rho}$$

$D$  — **thermal diffusivity** (m<sup>2</sup>/s)  
(may be different at the different points of the  
material)

$\rho$  — density  
 $c_p$  — specific heat capacity at  
constant pressure

Thermal diffusivity of some  
dental materials:

material	$\lambda$ (W/(mK))	$D$ (10 <sup>-6</sup> m <sup>2</sup> /s)
Enamel	0.9	0.5
Dentin	0.6	0.2
Water	0.44	0.14
Amalgam	23	9.6
Gold	300	118
Porcelain	1	0.4
Glass	0.6-1.4	0.3-0.7
Acrylate	0.2	0.1
PMMA	0.2-0.3	0.12
ZnPO <sub>4</sub>	1.2	0.3

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## Thermal expansion

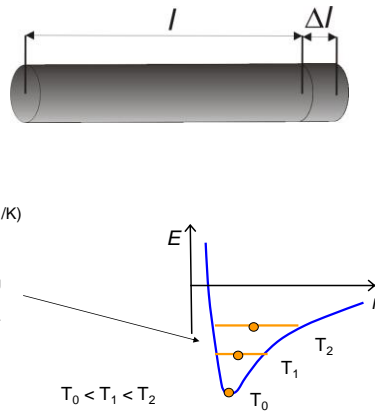
Linear expansion:

$$\frac{\Delta l}{l_0} = \alpha \Delta T$$

$$l = l_0(1 + \alpha) \Delta T$$

$\alpha$  — **coefficient of thermal expansion** (1/K)

Increasing temperature results increasing  
oscillation of particles.  
This may be observed as increasing size.



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## Volumetric thermal expansion

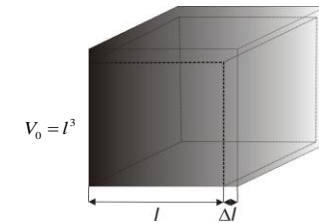
$$\frac{\Delta V}{V_0} = \beta \Delta T$$

$$V = V_0(1 + \beta) \Delta T$$

$\beta$  — **volumetric thermal expansion  
coefficient** (1/K)

for isotropic materials:

$$\beta \approx 3\alpha$$

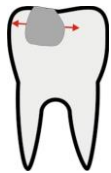


Isotropic: properties are independent from  
the direction

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## Effect of thermal expansion

Larger expansion  
(compression)



Smaller expansion  
(tension)



Cave is formed



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The coefficient of thermal expansion of  
some dental materials :

Material	$\alpha (10^{-6} 1/K)$
Enamel	11.4
dentin	8.3
Gold	14.2
Gold alloys	11-16
Amalgam	$\approx 25$
Porcelain	4-16
Acrylate	90
Glass	8
PMMA	90-160
Silicon	100-200
gypsum	15-20
wax	300-500

different expansion  $\Rightarrow$  stress!



Conservative dentistry!

Implants, braces.

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## Optical properties

Color of the teeth



Color of the amalgam

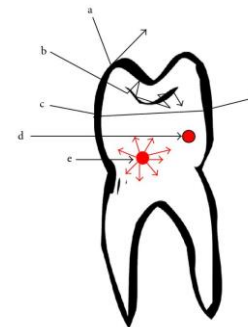


### Optical phenomena

Absorption  
Emission  
Reflection  
Scattering

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## Light and the tooth



- a - reflection
- b - scattering
- c - transmission and refraction
- d - absorption
- e - absorption and fluorescence

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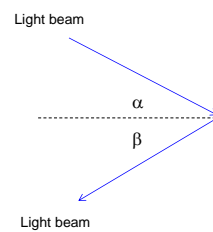
## Geometrical optics

- light propagates in straightline.

### reflection

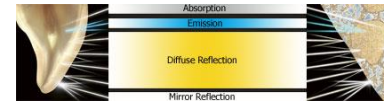


$$\alpha = \beta$$

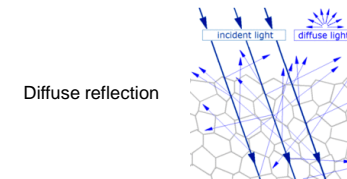


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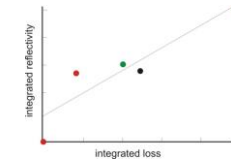
## Reflection



Determination  
of mineral loss



Diffuse reflection



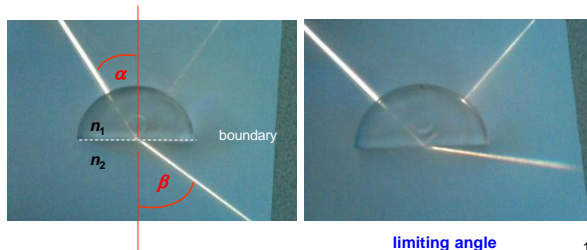
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## Refraction

Snell's law:

$$\frac{\sin \alpha}{\sin \beta} = \frac{c_1}{c_2} = \frac{n_2}{n_1} = n_{21}$$

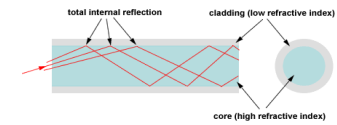
(relative) refractive  
index



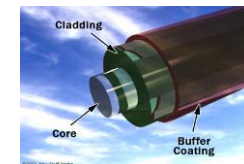
limiting angle

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## Application of the total internal reflection



optical fiber



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## Application of the total internal reflection

mirage:



dentistry



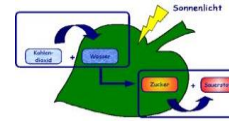
endoscopy



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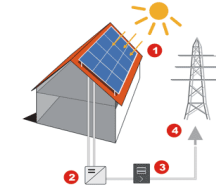
## Energy transport

Photosynthesis is the base of the life.



Chloroplast absorbs the light energy and stores in molecules as chemical energy.

Crude oil contains the stored energy of the Sun.



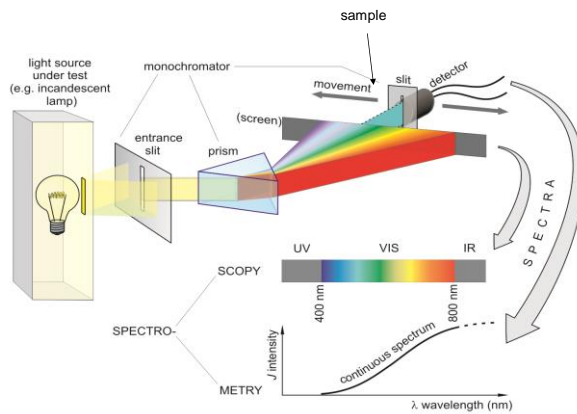
Solar cell converts the light energy into electric one.



The absorbed energy in the skin results reddening.

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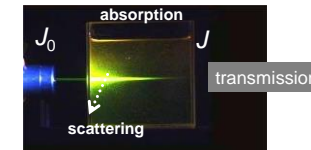
## Spectroscopy and spectrometry



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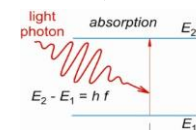
## Interaction to the matter

Consequence  
 $J < J_0$



Attenuation: decreasing intensity  
**attenuation = scattering + absorption**

Inhomogeneity of the refractive index in the material!



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## Light scattering

**elastic scattering**  
( $\lambda$ ,  $f$ ,  $\varepsilon$  are constant)



**Rayleigh-scattering**  
particle size  $\ll \lambda$

$$\text{scattered intensity} \sim \frac{1}{\lambda^4}$$

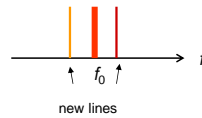
blue sky: blue is scattered better.  
(wavelength is shorter)

**Mie-scattering**  
size of the scattering particle  $\geq \lambda$   
(no strong  $\lambda$  dependency)  
(white clouds)



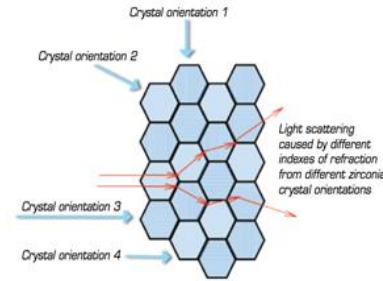
**inelastic scattering**  
( $\lambda$ ,  $f$ ,  $\varepsilon$  are not constant)

**Raman-scattering**



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## Light scattering



Scattering on crystals.

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## Attenuation law

if the scattering is negligible



**attenuation ~ absorption**

**transmission**

$$\dot{T} = \frac{J}{J_0} (\cdot 100 \%)$$

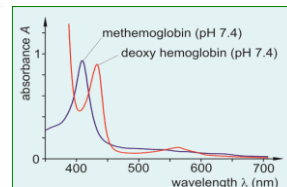
**absorbance**

$$A = \lg \frac{J_0}{J}$$

attenuation coefficient

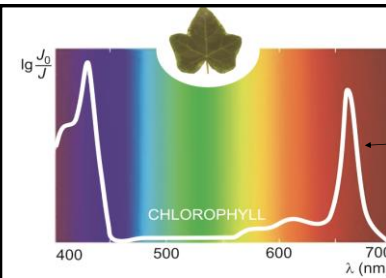
$$J = J_0 \cdot e^{-\mu \cdot x}$$

**absorption spectrum:  $A(\lambda)$**



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## Absorption spectra



Green color of the plants is due to the absorption in red.

Color vision

The colour of a material depends on the absorption.



**Absorption Spectra of Human Visual Pigments**

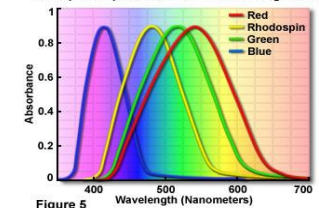
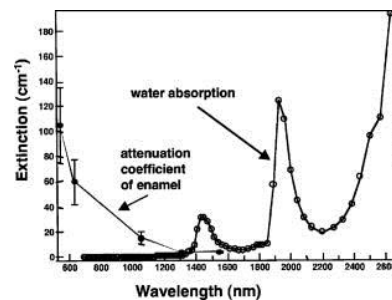


Figure 5

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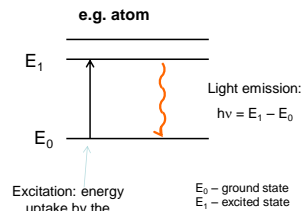
## Absorption of the natural materials



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## Luminescence

Light emission over the thermal radiation.  
Light emission after excitation.



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## Application of luminescence

excitation	name: -luminescence	example
light	photo-	quinine-sulphate, phosphor, ...
X-ray	X-ray	Nal(Tl)
radioactive radiation	radio-	Nal(Tl)
electric field	electro-	mercury-lamps
mechanical effect	tribo-	sugarcube
chemical reaction	chemo- (bio-)	firebug
heat	thermo-	CaSO <sub>4</sub> (Dy)

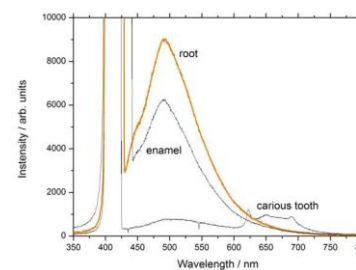


+ materials analysis, structure of biological macromolecules, fluorescence microscopy, sensors, monitors, radiation detectors, ...

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## Luminescence spectrum

Blue light excitation (405 nm)



less intensity

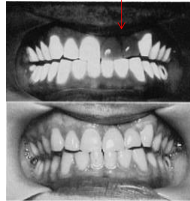
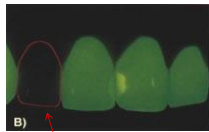


higher intensity



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## Dental application



Intensity: depends on the thickness of the plaque.

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## Transparency

transparent - translucent - opaque



**transparent:** light passes through the material without being scattered.

**translucent:** diffuse transparency, the light is scattered.

**opaque:** not transparent, diffuse reflection

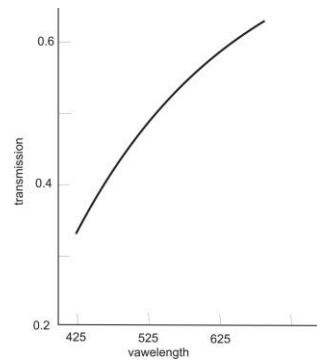
Examples:

transparent: plate glass, water ....

translucent: oil paper, ice, some plastics...

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## Transparency of the enamel

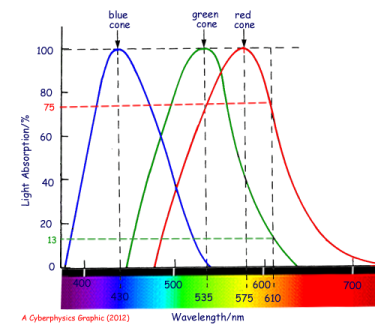


Transmission:

$$T = J/J_0$$

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## Why can we see colors?



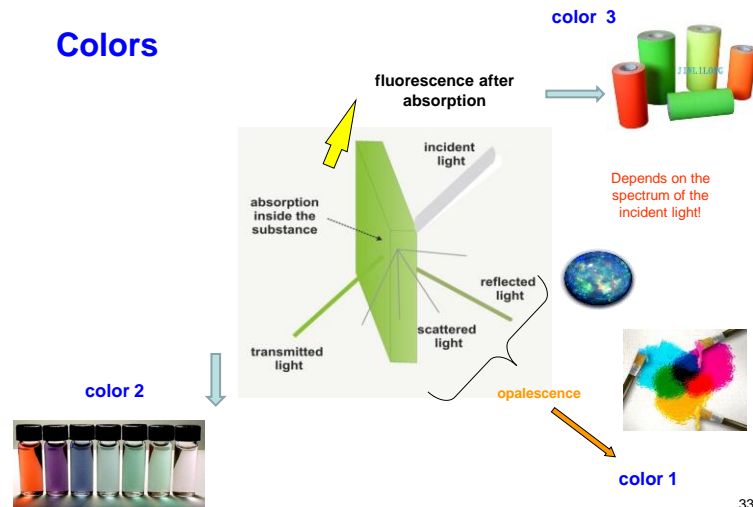
Color theory:

Every color may be produced mixing appropriate 3 colors.

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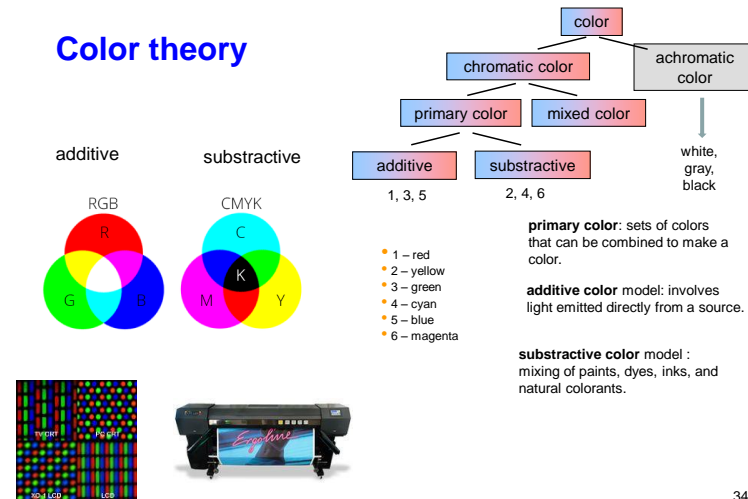


## Colors



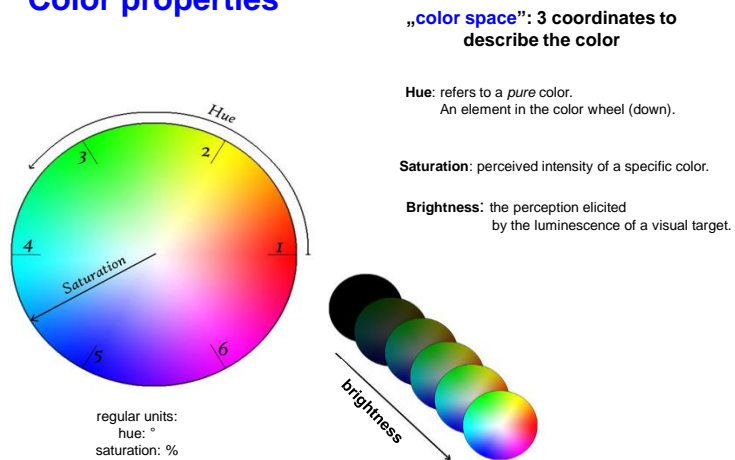
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## Color theory



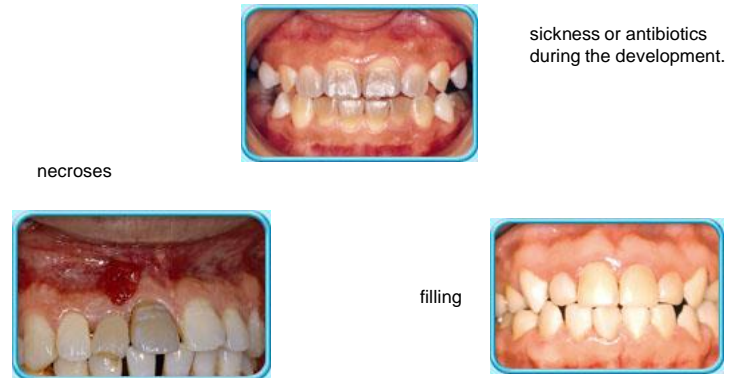
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## Color properties



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## Color of teeth



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