

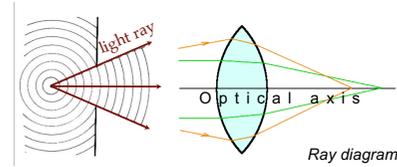
WAVE OPTICS

MIKLÓS KELLERMAYER

Geometric optics and wave optics

Geometric optics

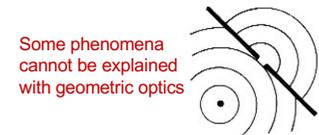
If light propagates through a slit much larger than its wavelength, then the spreading of the wavefront (phase) may be simplified into a line ("light ray").



- Optical (light) ray ("light beam"): abstraction, mathematical line.
- Arrows represent the direction of energy propagation.
- Optical axis: line connecting the midpoint of optical components (e.g., lenses).
- Principle of reversibility: the direction of energy propagation (arrows) may be reversed.

Wave optics

If light propagates through a slit comparable or smaller than its wavelength, then its wave properties must be taken into account.



- Important parameters of the propagating wave:
- Period (T)
 - Frequency ($f=1/T$)
 - Velocity (v, c)
 - Wavelength (λ): distance covered in a period:

$$\lambda = cT = \frac{c}{f}$$

Speed of propagation of light in **vacuum**: $c=2.99792458 \times 10^8 \text{ ms}^{-1}$
In optically denser media the speed of propagation is reduced (c_1).
 This may be expressed with the **absolute refractive index** (n_1):

$$n_1 = \frac{c}{c_1}$$

Wave: propagating oscillation

What is an oscillation?

Example:
Mechanical oscillation



- Tacoma Narrows Bridge ("Gallopin' Gertie")
- ("Gertie the Dinosaur" (1914), cartoon, Winsor McCay)
 - Opening: July 1, 1940.
 - During wind (50-70 km/h): oscillation for hours
 - Oscillation amplitude initially 0.5 m, then, after snapping of a suspension cable, up to 9 m!
 - Collapse: November 7, 1940.

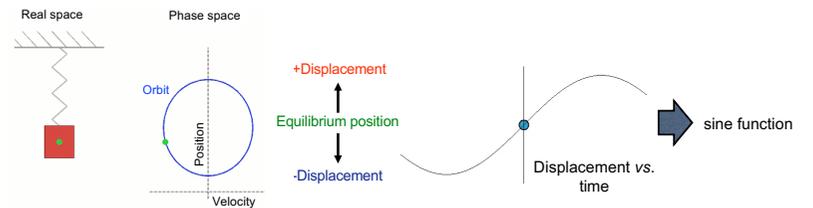
Explanation: Kármán vortices "shake" the object

Kármán vortex street

Theodore von Kármán
1881-1963

Harmonic oscillation

Restoring force acts on a system displaced out of equilibrium (e.g., mass on a spring).



$$y = R \sin \phi$$

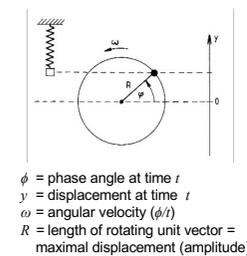
Because $\phi = \omega t$: $y = R \sin(\omega t)$

If the initial phase angle (ϕ_0) differs from 0: $y = R \sin(\omega t + \phi_0)$

Because angular velocity (ω) is the full circular orbit (2π) per period (T): $y = R \sin\left(\frac{2\pi}{T} t + \phi_0\right)$

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Types of waves

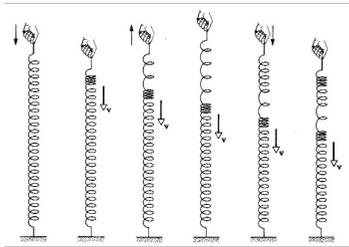
- According to **source**:
 1. Mechanical: elastic deformation propagating through elastic medium
 2. Electromagnetic: electric disturbance propagating through space (vacuum)

- According to **propagation dimension**:
 1. One-dimensional (rope)
 2. Surface waves (pond)
 3. Spatial waves (sound)

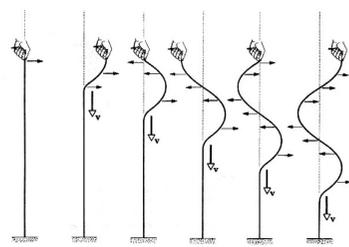


- According to **relative direction of oscillation and propagation**:

1. Longitudinal



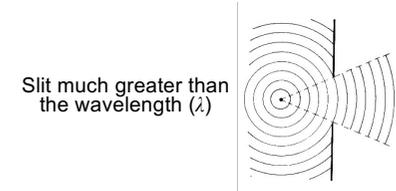
2. Transverse



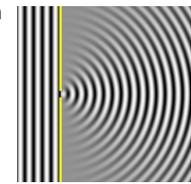
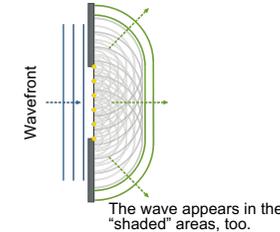
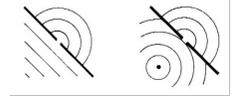
Wave phenomena I. Diffraction

Huygens-Fresnel principle:

every point of a wavefront is the source of further waves

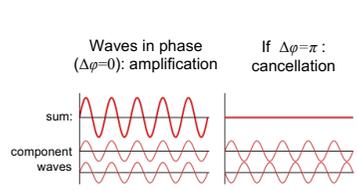


Slit much smaller than wavelength (λ)

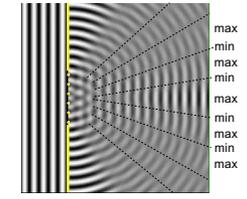


Wave phenomena II. interference

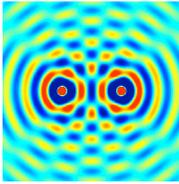
Principle of superposition



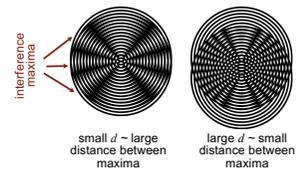
Slit comparable to wavelength
(=pointlike slits separated by distance d , where $d \sim \lambda$)



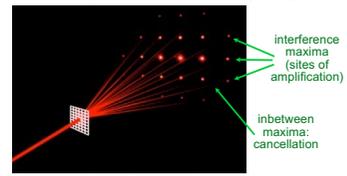
Interference of waves emerging from two point sources.



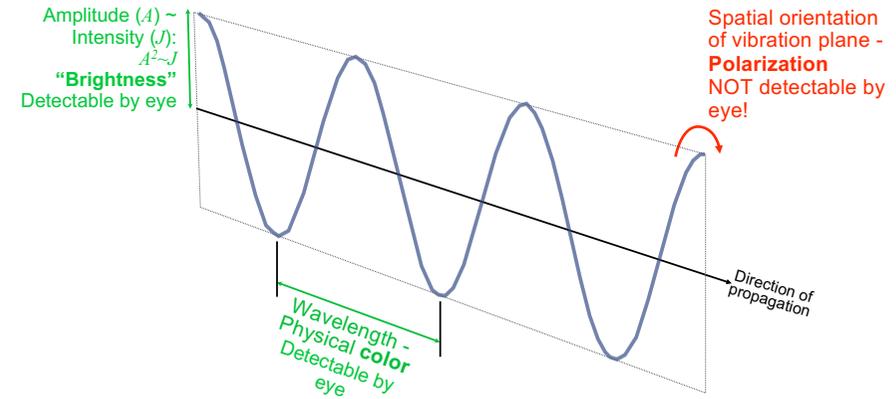
Interference pattern depends on distance (d) separating the pointlike slits



Diffraction pattern of a 2D optical grating



Detectable parameters of the light wave



Wave phenomena III.

Polarization

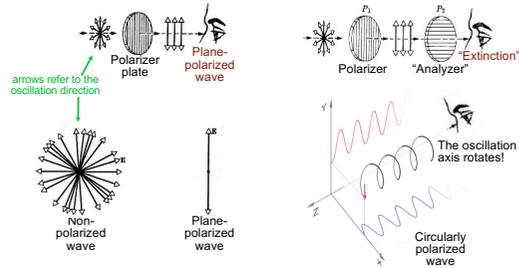
- Polarization: oscillation is oriented in some *preferred* direction
- Birefringence is related to polarization: anisotropic propagation velocity
- Only *transverse* waves can be polarized.



Polarization of Mechanical waves



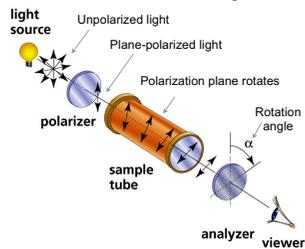
Polarization of Electromagnetic waves



Polarization can be understood by observing the head-on view of the wave:

Applications of polarization

Polarimetry



Rotation angle depends on the concentration (c) of the optically active* material:

$$\alpha = [\alpha]_D^{20} \cdot c \cdot l$$

[α] = specific angle of rotation ("20": room temperature; "D": emission spectral line of Na $\lambda=589$ nm)

l = length of sample tube

*Optically active material: contains *chiral* (mirror-symmetric) molecules that rotate the plane of polar

Polarization microscopy

Cross-striated skeletal muscle in the polarization microscope



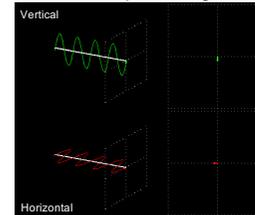
- A-band: anisotropic (birefringent) region (contains myosin helically ordered myosin molecules)
- I-band: isotropic region



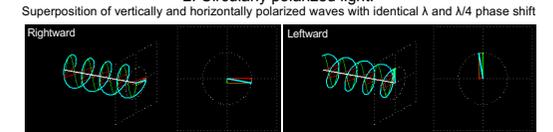
Polarized light and its interactions

Direction of the vibration (electric or magnetic field) has preferred orientation

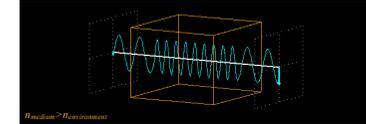
1. Plane-polarized light



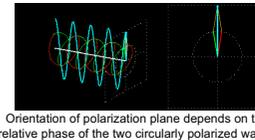
2. Circularly polarized light:



4. Light decelerates in optically dense medium; because its frequency is constant, its wavelength becomes reduced.



3. Superposition of a right- and leftward circularly polarized wave results in plane-polarized light.

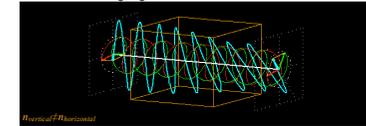


Orientation of polarization plane depends on the relative phase of the two circularly polarized waves

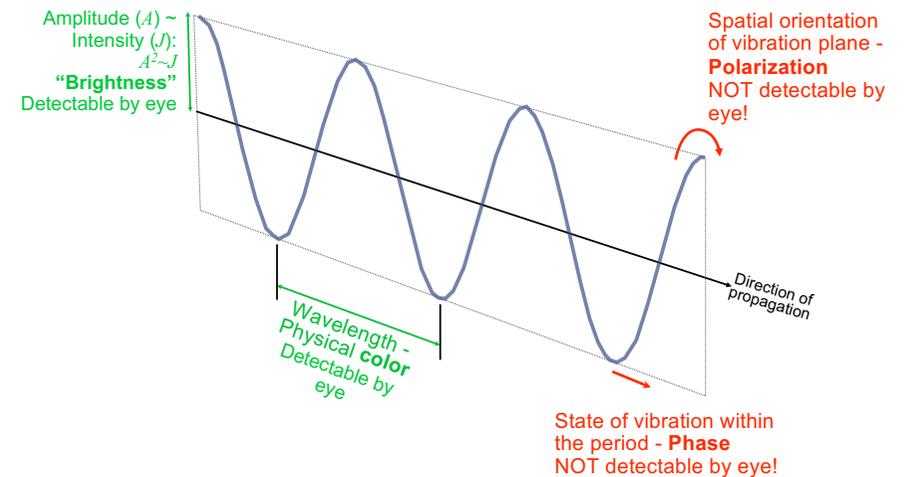
*Anisotropy (birefringence): refractive index (~light speed) is orientation dependent (i.e., in different directions within the sample, light propagates with different speeds).

Movies - http://cddemo.szilab.org/index_hu.html

5. In an anisotropic* medium a phase shift occurs between the circularly polarized components: the polarization plane of the emerging wave becomes *rotated*.



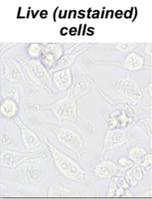
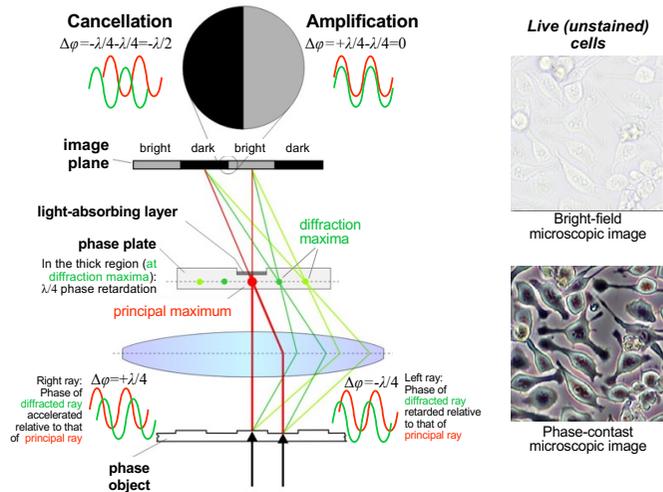
Detectable parameters of the light wave



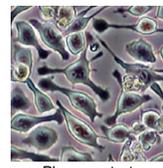
Phase contrast microscopy



Frits Zernike (1888-1966) Nobel-prize



Bright-field microscopic image



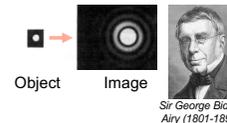
Phase-contrast microscopic image

- Phase: shows the state of vibration within the entire period (2π).
- Expressed with the phase angle (ϕ).
- Phase difference between waves ($\Delta\phi$): phase shift (retardation or acceleration)

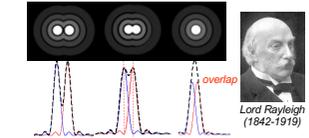
Resolution of the human eye I.

Diffraction limit

Because of diffraction: image of a point object is an Airy disk



Rayleigh criterion: objects may be resolved if their corresponding Airy disks do not overlap



Smallest resolved distance has a limit (Abbe equation):

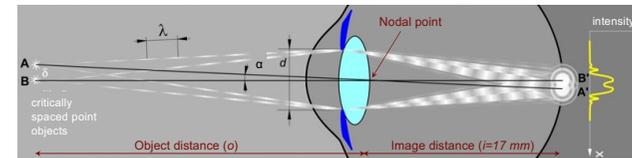
$$d = \frac{0.61\lambda}{n \sin \alpha}$$

λ = wavelength
 n = refractive index of medium
 α = angle between axis and outermost ray



Ernst Abbe (1840-1905)

Diffraction limit of the human eye



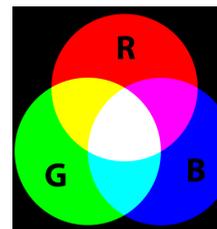
Limiting visual angle: $\alpha_H = 1.22 \frac{\lambda}{d}$ Smallest angle of view at which two closely spaced objects may be resolved. At average wavelength (550 nm) and pupil diameter (4 mm): **0.6'** (angular minutes)

Resolution of the human eye II.

Biological limit: receptor cell density

Object	Image on receptors	Sensed image

- Condition of resolution: at least one inactivated receptor cell falls in between two activated ones. The limiting angle of view under this condition is $(\alpha_H) \approx 0.8'$
- The diffraction and biological limits of the human eye are **comparable!**



Additive color coding

Any color may be generated by mixing three basic colors (R =red, G =green, B =blue) with varying weighing factors.

$$X = rR + gG + bB$$

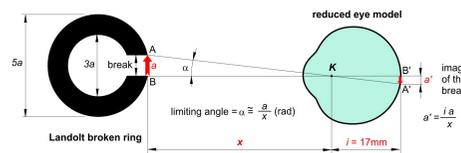
Visual Acuity ("visus", vision):

$$visual_acuity = \frac{1'}{\alpha} 100\%$$

α = experimental (measured) visual angle

Average visual angle in healthy humans: $1' (= 100\% \text{ vision})$

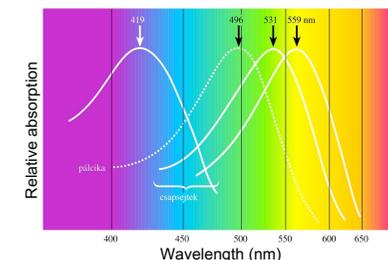
Measurement of visual acuity



In the human eye:

- 3 different color-sensitive receptors.
- Each receptor absorbs in different regions of the visible spectrum ($R=64\%$, $G=32\%$, $B=2\%$).

Absorption spectra of the human color-sensitive receptors (cones)



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