

Ligand-protein interactions and binding thermodynamics

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Subject

- Focus on ligand-protein binding
 - Qualitative and quantitative characterisation
 - Thermodynamics (and kinetics)
 - How to interact/influence - drug design
 - Computational support to drug discovery

Outline

- Basic relationships
 - Measurements and computations
 - Analysis of ligand-protein binding
 - Role of water
-

- Computations
 - Molecular dynamics (MD)
 - Tool for quantitative description
 - MD based applications to characterize ligand-protein binding
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- Very fast estimation of ligand-protein interactions
 - Docking-scoring
 - Drug discovery application

Ligand-protein binding

- Signal transduction
 - G-protein coupled receptors (GPCRs)
- Enzymatic catalysis
 - Cytochrome P450
- Transcription
 - Nuclear receptors...
- Endogenous and exogenous (e.g. drugs) ligands

Few basic relationships



$$K_d = \frac{[L][P]}{[LP]} ; \text{p}K_d = -\log(K_d)$$

$$\Delta G_{\text{bind}} = RT \ln(K_d/C_{\text{ref}})$$

$$\Delta G = \Delta H - T\Delta S \quad (\text{Gibbs}) \text{ typical experimental conditions} \\ (\text{NPT})$$

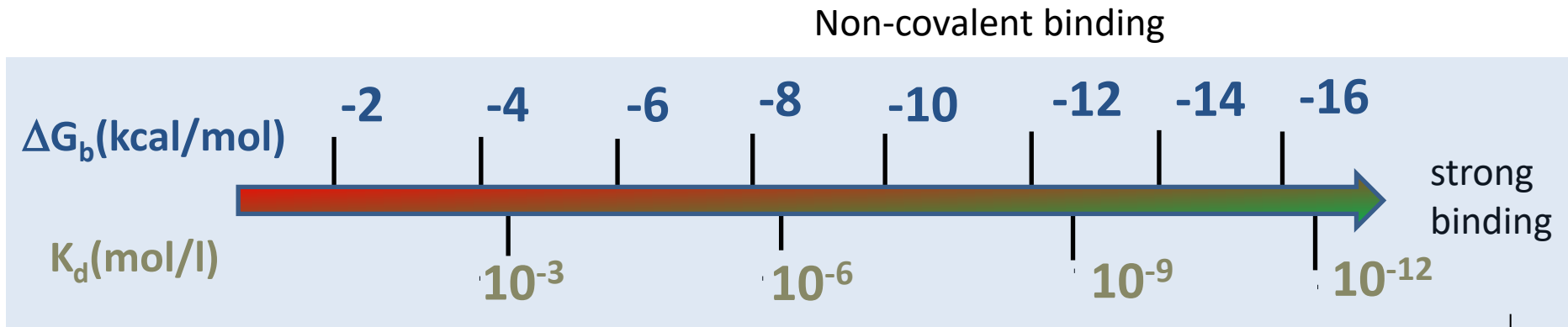
$$\Delta F = \Delta U - T\Delta S \quad (\text{Helmholtz}) \text{ calculations for solutions, often used} \\ (\text{NVT, canonical})$$

$$F = -k_B T \ln Z,$$

$$Z = \sum_i e^{-\frac{E_i}{k_B T}} - \text{partition function} \quad (\sim \int e^{-\frac{E(r,p)}{k_B T}} dr dp)$$

can be calculated for simple systems only

Free energy – Equilibrium constant



$$A + P \leftrightarrow AP; K_A = \frac{[A][P]}{[AP]}; \Delta G_A^{bind} = RT \ln K_A$$

$$B + P \leftrightarrow BP; K_B = \frac{[B][P]}{[BP]}; \Delta G_B^{bind} = RT \ln K_B$$

$$\Delta \Delta G = \Delta G_B^{bind} - \Delta G_A^{bind} = RT \ln \frac{[B]}{[BP]} / \frac{[A]}{[AP]}$$

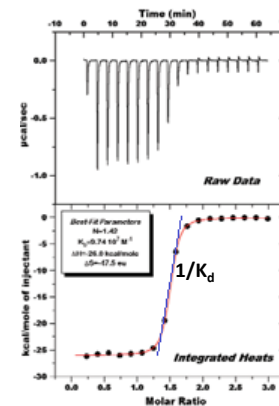
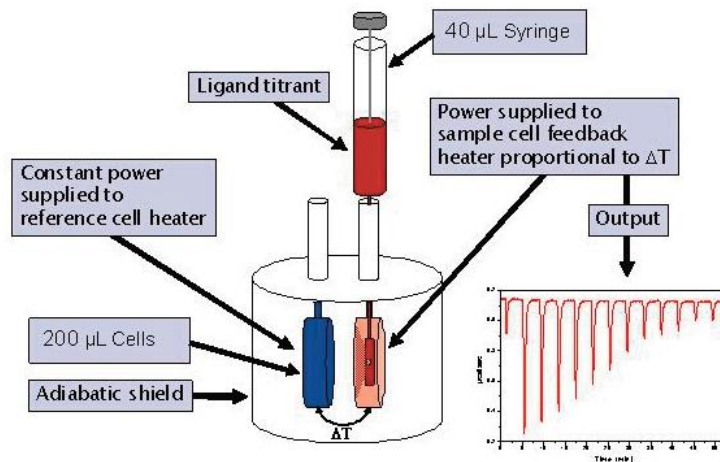
$$\begin{aligned} \Delta \Delta G \sim 1.4 \text{ kcal/mol} &\rightarrow \frac{[B]}{[BP]} / \frac{[A]}{[AP]} \sim 10 \\ 2.8 \text{ kcal/mol} &\rightarrow \sim 100 \end{aligned}$$

(RT ~ 0.6 kcal/mol; rotational barrier in ethane ~ 2.9 kcal/mol)

biotin-avidin
 $\Delta G = -20.4 \text{ kcal/mol}$
 $K_d = 10^{-15} \text{ mol/l}$

Measuring binding thermodynamics

- Isothermal titration calorimetry
 - n , K_d , ΔH $\rightarrow \Delta G$, ΔS
 - limits:
 - solutions
 - protein quantity (10-100 μg)
 - throughput



Measuring binding thermodynamics

- Van't Hoff analysis

- $\ln K_d = \frac{\Delta H_b}{RT} - \frac{\Delta S_b}{R}$ ($\Delta G_b = \Delta H_b - T\Delta S_b = RT \ln K_d$)

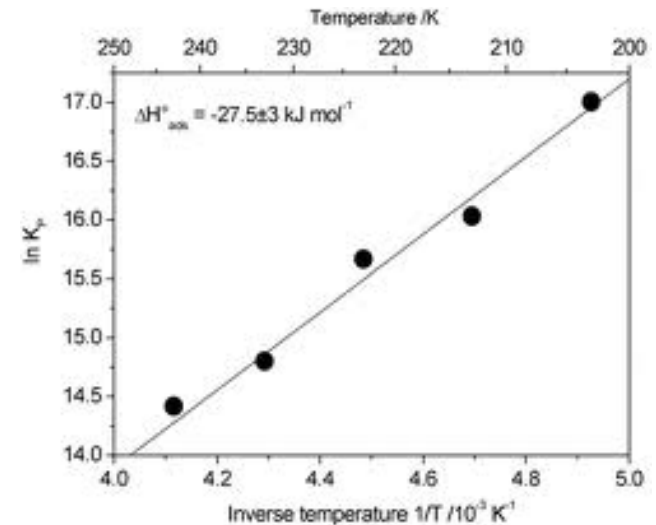
- Measure K_d at various $T \rightarrow \Delta H$ és ΔS

- Experimental techniques

- Radioligand displacement
 - Mass spectrometry
 - Chromatography
 - Surface plasmon resonance (SPR)
 - ...

- limits

- ΔH depends on T
 - extrapolation (ΔS : $1/T=0$)



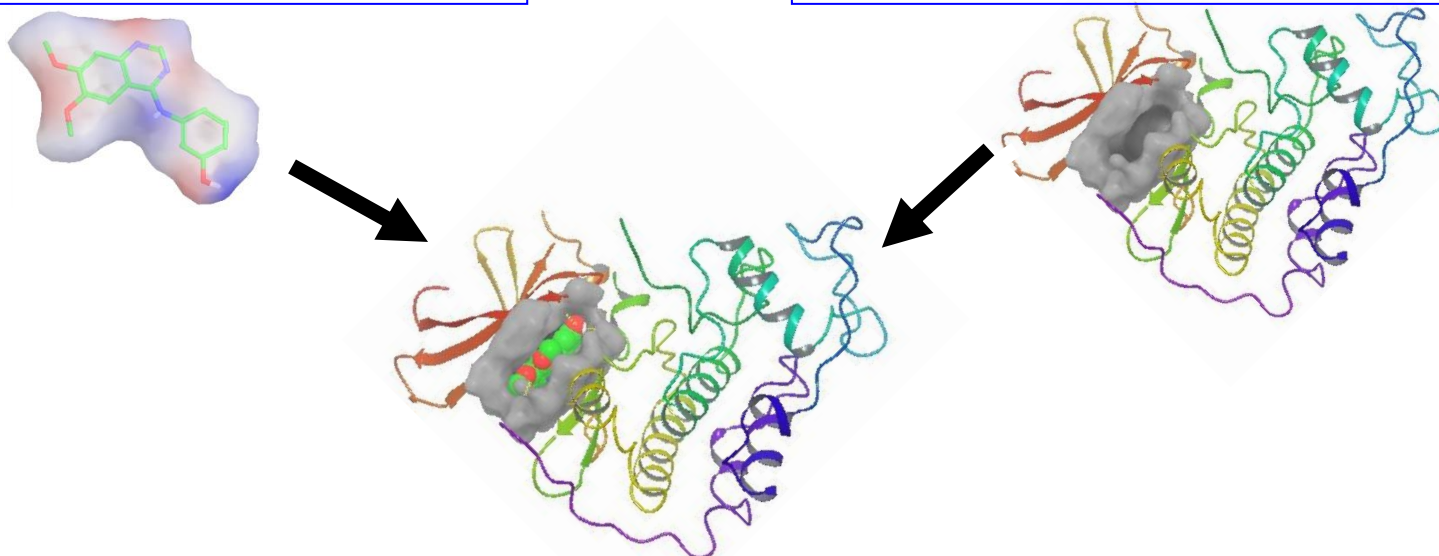
Ligand-protein binding “steps”

Ligand in water

- Conformational change
- (partial) desolvation

Protein in water

- Conformational change
- Partial desolvation



Ligand-protein complex

- Ligand-protein interactions

Water plays a substantial role in the binding process

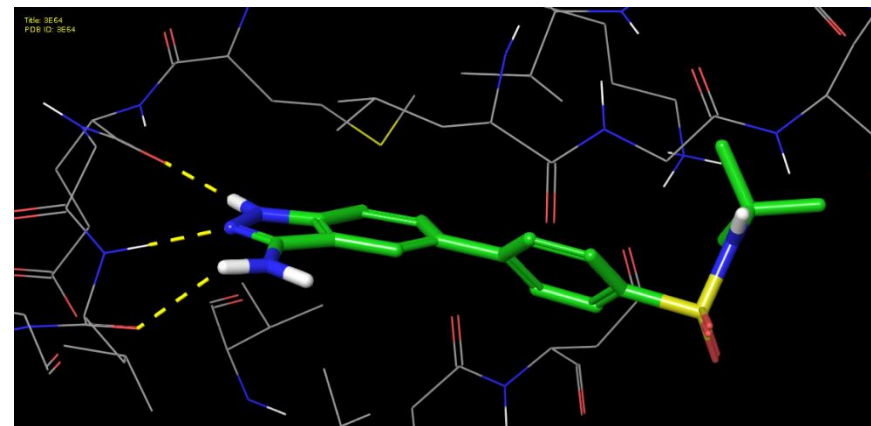
Qualitative binding thermodynamics

- desolvation (ligand+protein)
 - beneficial ΔS (change in water structure)
 - disadvantageous ΔH
- Conformational change (ligand+protein)
 - disadvantageous ΔH (optimal before binding)
- Ligand-protein interactions
 - beneficial ΔH (polar and van der Waals interactions)
 - disadvantageous ΔS (restricted motion)

ΔG is a sum of several terms with positive and negative signs

Qualitative binding thermodynamics

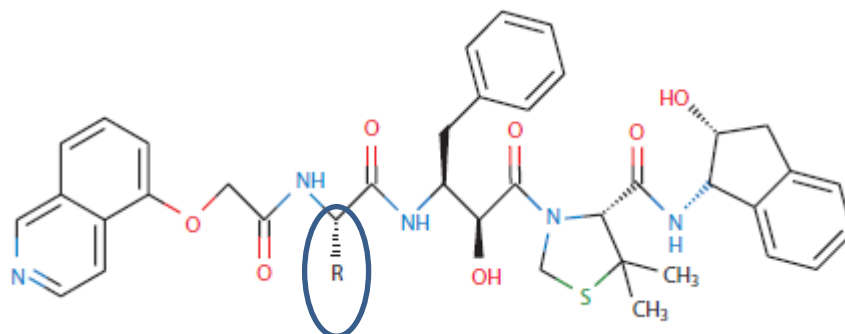
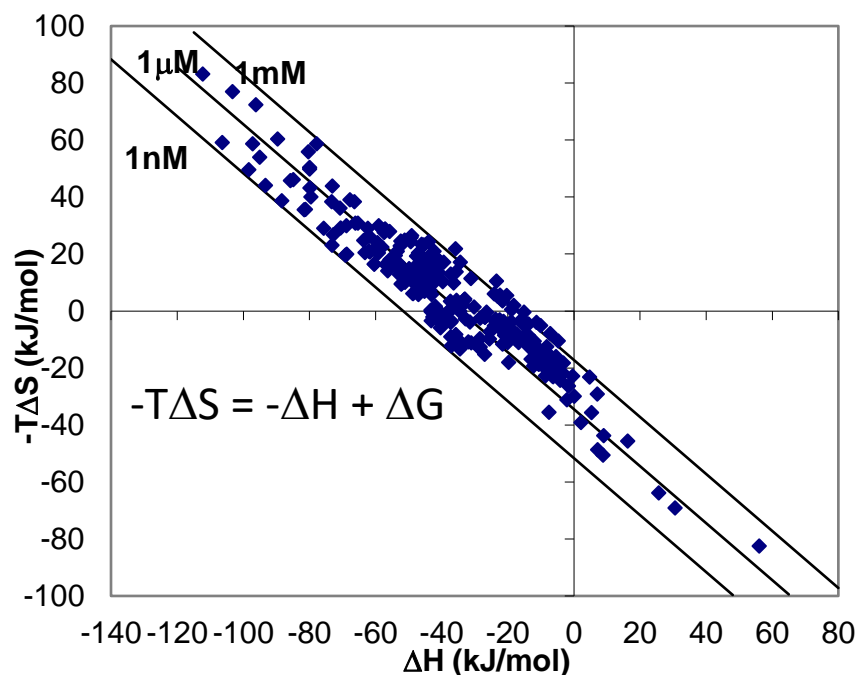
- ΔG , ΔH , ΔS can be assigned to steps from one state to another – state functions
- Assigning ΔG , ΔH , ΔS to structural elements is problematic
 - Limited additivity
 - ΔH additivity – good approximation
 - ΔS additivity – bad approximation



Enthalpy-entropy compensation

Small structural changes of a ligand-protein complex results in significant $\Delta\Delta H$ és $\Delta(T\Delta S)$ changes of opposite sign and a small change in $\Delta\Delta G$

- The compensation is observed for a wide range of phenomena
- Both in water and in apolar solvents



R group	ΔG	ΔH	$-T\Delta S$
$-S-CH_3$	-14.87(9)	-8.2(2)	-6.67(9)
$-SO_2CH_3$	-14.6(2)	-12.1(6)	-2.5(2)

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**ΔG changes are limited
(within ~35kJ/mol)**

Hydrophobic effect

- Hydrophobic effect:

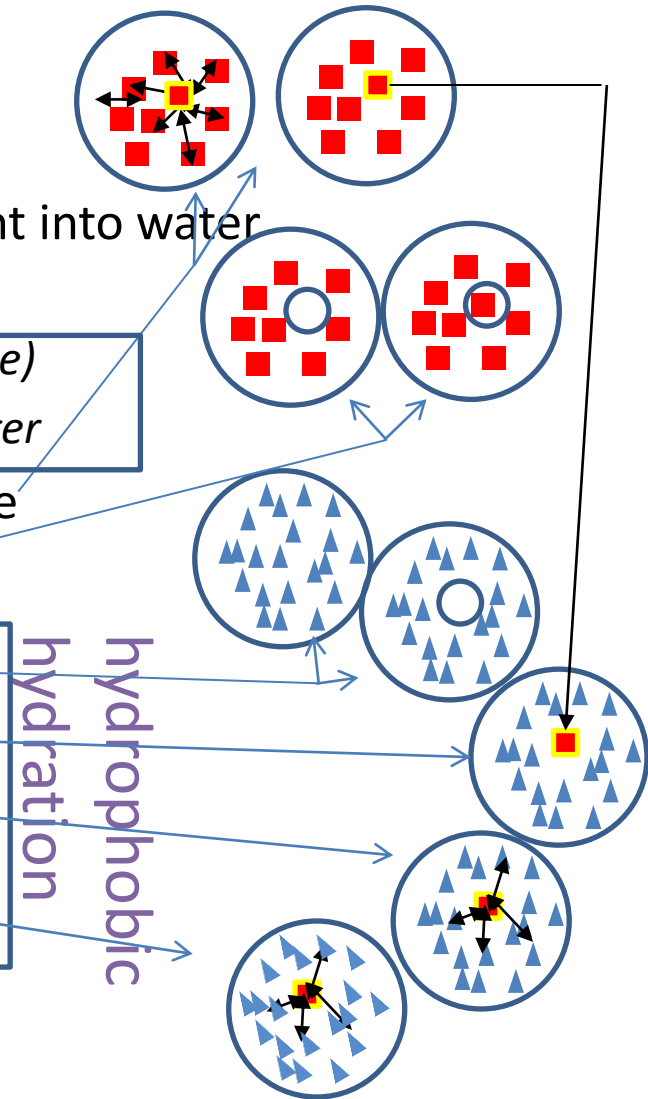
Bringing an apolar substance from its apolar solvent into water
(hydrocarbon → water)

analogy: desolvation upon ligand-protein binding (inverse)
apolar moieties - water → apolar-apolar, water-water

- Breaking apolar contacts and removing molecule
- Filling empty space in the apolar medium

- Hole formation in water
- Inserting the apolar substance
- Formation of solute-solvent interactions
- Reorganization of water structure

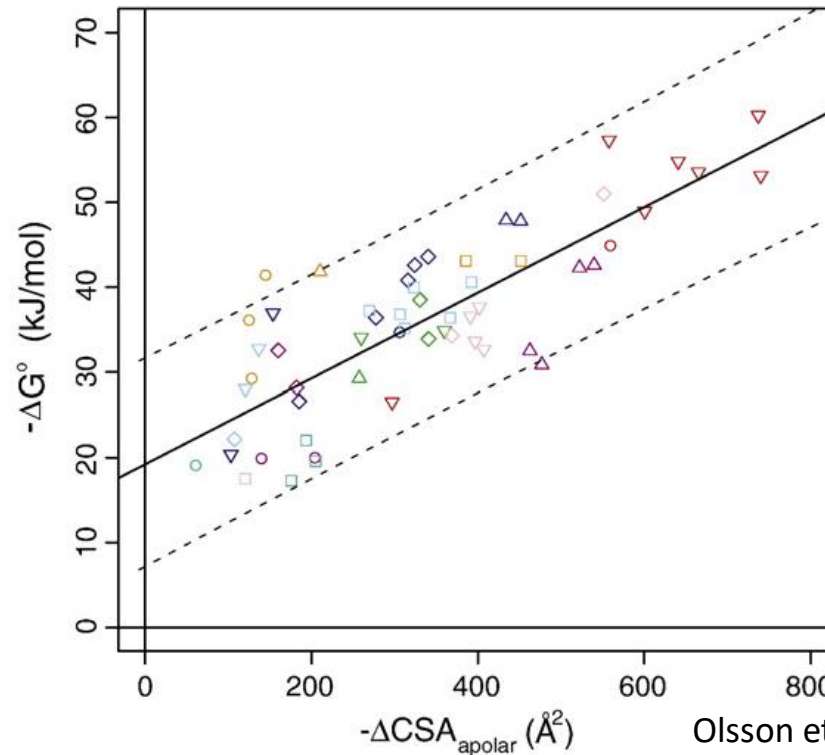
ΔG positive



Hydrophobic effect

- ΔG increase
 - 20°C
 - ΔH (advantageous) and $T\Delta S$ (disadvantageous) decrease; $T\Delta S$ change dominates
 - higher T
 - small change in ΔG
 - ΔH increases and becomes dominant
 - disadvantageous for enthalpy
 - advantageous for free energy
 - interactions are sacrificed for increased disorder
 - Explanation: focuses on hydrophobic hydration
 - Key factor in entropy decrease: *Water structure perturbed*
 - Hole formation - small size of water molecules
 - Water H-bonds near to the apolar solute
 - No general quantitative model available!

Apolar surface and binding free energy



- Ligand-protein binding free energy correlates with apolar surface buried in the binding ($R^2=0.65$).
- Shape fitting and polar/apolar feature mapping give significant contribution to binding
 - Directional interactions do not contribute importantly to the above correlation

Affinity and molecular size

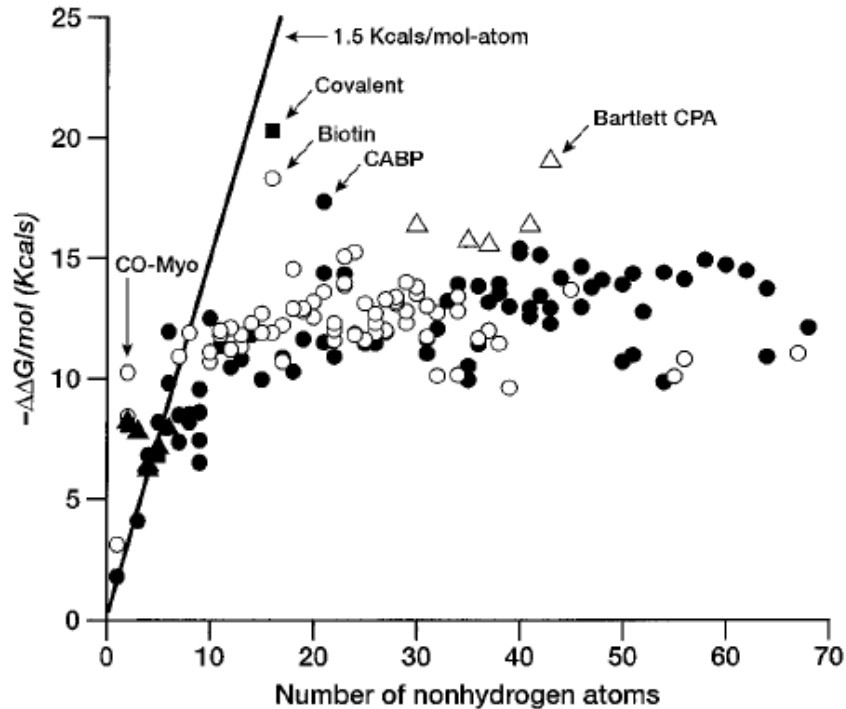


FIG. 1. Free energy of binding (in kcal/mol) for ligands and enzyme inhibitors plotted as a function of the number of nonhydrogen atoms in the ligand. See Table 1. A line with slope of 1.5 kcal/mol and an intercept of 0 is included as a visual aid to analysis. Δ , Metal ions or metalloenzymes; \blacktriangle , small anions; \circ , natural ligands; \bullet , enzyme inhibitors.

Available binding affinity is

- limited
- limit does not increase with size above ~25 nonhydrogen atoms

PNAS 1999, 96, 9997

Summary

- Binding thermodynamics – characterizes ligand-protein interactions
- Key elements of binding: polar interactions and apolar desolvation
- Related phenomena: hydrophobic effect, enthalpy-entropy compensation
- Ligand size affects maximal available binding free energy
 - ΔG_{\max} – available binding free energy increase fast with ligand size for small ligands and is insensitive to size for larger ligands