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# KÉPLETTÁR

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## BIOFIZIKA ÉS BIOSTATISZTIKA TÁRGYAKHOZ

*Összeállította:*

*A Biofizikai és Sugárbiológiai Intézet*

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# GYAKORLATOK

## I.FÉLÉV

### MIKROSZKÓPIA I.

$$D = \frac{1}{f} = (n_{21} - 1) \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$\frac{1}{f} = \frac{1}{t} + \frac{1}{k}$$

$$D = \frac{1}{f_1} + \frac{1}{f_2} = D_1 + D_2$$

$$N = \frac{K}{T} = \frac{k}{t}$$

$$N_{\text{össz}} = N_{\text{obj}} \cdot N_{\text{ok}}$$

### MIKROSZKÓPIA II.

$$\Delta s = d \sin \alpha_k = k\lambda$$

$$\delta = 0,61 \frac{\lambda}{n \sin \omega}$$

$$NA = n \cdot \sin \omega$$

$$f = \frac{1}{\delta}$$

$$N_{\text{szög}} = - \frac{da}{f_{\text{ok}} f_{\text{obj}}}$$

$$N_{k=\infty} = - \frac{a}{f}$$

$$k_1 = d + f_{\text{obj}}$$

$$K = \frac{(J_{\text{vil}} - J_{\text{söt}})}{(J_{\text{vil}} + J_{\text{söt}})}$$

$$A_{\text{eredő}} = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos \Delta\varphi}$$

### REFRAKTOMETRIA

$$c = f\lambda$$

$$n = \frac{c_{\text{vákuum}}}{c_{\text{közeg}}}$$

$$n_{21} = \frac{n_2}{n_1}$$

$$\frac{\sin \alpha}{\sin \beta} = \frac{c_1}{c_2} = \frac{n_2}{n_1} = n_{21}$$

$$\frac{1}{\sin \beta_h} = n_{21}$$

$$n = n_0 + kc$$

### MÉRÉSTECHNIKA

$$H = |X_{\text{mért}} - X_{\text{tényleges}}|$$

$$h = \frac{|X_{\text{mért}} - X_{\text{tényleges}}|}{X_{\text{tényleges}}} \cdot 100\%$$

$$U = RI$$

$$R_{\text{soros,eredő}} = R_1 + R_2$$

$$\frac{1}{R_{\text{párhuzamos,eredő}}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$U_1 = U_0 \frac{R_1}{(R_1 + R_2)}$$

$$U_{\text{cs-cs}} = 2U_{\text{max}} = 2\sqrt{2}U_{\text{eff}}$$

## REZONANCIA

$$F = -Dx$$

$$F_{neh} = mg$$

$$x = A \sin(\varphi_0 + \omega t)$$

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{D}{m}}$$

$$\omega = 2\pi f$$

$$f = \frac{1}{T}$$

$$x = A_0 e^{-\delta t} \sin(\omega t)$$

$$A = A_0 e^{-\delta t}$$

$$D_{\text{párhuzamos,eredő}} = D_1 + D_2$$

$$\frac{1}{D_{\text{soros,eredő}}} = \frac{1}{D_1} + \frac{1}{D_2}$$

## FÉNYEMISSZIÓ

$$\varepsilon = hf = h \frac{c}{\lambda}$$

$$\lambda_{\max} T = b$$

$$hf = E_j - E_i$$

## FÉNYABSORPCIÓ

$$hf = E_j - E_i$$

$$\varepsilon = hf = h \frac{c}{\lambda}$$

$$T = \frac{J}{J_0} (100\%)$$

$$A = \lg\left(\frac{J_0}{J}\right) = \varepsilon(\lambda)cx$$

## A SZEM OPTIKÁJA

$$D = \frac{n}{t} + \frac{n'}{k}$$

$$\Delta D = D_p - D_r = \frac{1}{t_p} - \frac{1}{t_r}$$

$$D_t = \sum_i D_i$$

$$\text{visus} = \frac{l(^{\circ})}{\alpha(^{\circ})} 100\%$$

$$\alpha(^{\circ}) \approx \frac{a}{x} (\text{rad}) \frac{360(^{\circ})}{2\pi(\text{rad})} 60\left(\frac{'}{\circ}\right)$$

$$a' = \frac{17a}{x} (\text{mm})$$

$$\text{receptorsűrűség} \approx \frac{1}{(a')^2} \left(\frac{1}{\text{mm}^2}\right)$$

$$d'_1 = 17 \frac{d}{x_1} (\text{mm}) \quad d'_2 = 17 \frac{d}{x_2} (\text{mm})$$

## POLARIMETRIA

$$\alpha = [\alpha]_D^{20} c l$$

$$\alpha = \sum \alpha_i$$

$$\alpha = \Delta n l \pi / \lambda$$

## BŐRIMPEDANCIA

$$I = I_{\max} \sin(2\pi ft)$$

$$U = U_{\max} \sin(2\pi ft)$$

$$I_{\text{eff}} = \frac{I_{\max}}{\sqrt{2}}$$

$$U_{\text{eff}} = \frac{U_{\max}}{\sqrt{2}}$$

$$R = \frac{U_{\text{gen}}}{I}$$

$$Z = \frac{U_{\text{eff}}}{I_{\text{eff}}}$$

$$R = \rho \frac{l}{A}$$

$$\rho^* = RA$$

$$C = \varepsilon \frac{A}{l}$$

$$X_C = \frac{1}{2\pi f C}$$

$$\gamma^* = \frac{C}{A}$$

$$U_{\text{gen}} = U_{\text{coarse}} U_{\text{fine}} 5V$$

$$U_{\text{gen.eff}} = U_{\text{coarse}} U_{\text{fine}} 5V \frac{1}{\sqrt{2}}$$

$$|Z| = \frac{R}{\sqrt{1 + (2\pi f RC)^2}}$$

## NUKLEÁRIS MÉRÉSTECHNIKA

$$N_j = N_{j+z} - N_z$$

$$E_\gamma = A + E_e$$

$$E_\gamma = A + E_e + E'_\gamma$$

$$E_\gamma = 2m_e c^2 + E_e + E_p$$

## GAMMAABSORPCIÓ

$$J = J_0 e^{-\mu \cdot x}$$

$$J = J_0 e^{-\mu_m \cdot x_m}$$

$$x_{1/10} = \frac{D}{\lg 2}$$

$$\mu = \frac{\ln 2}{D}$$

$$\mu = \mu_m \cdot \rho$$

$$x_m = x \cdot \rho$$

$$D_m = D \cdot \rho$$

$$\mu_m = \tau_m + \sigma_m + \kappa_m$$

## II. FÉLÉV

### GAMMAENERGIA

$$\frac{\varepsilon_1}{\varepsilon_2} = \frac{U_1}{U_2}$$

### IZOTÓPDIAGNOSZTIKA

$$\frac{1}{T_{\text{eff}}} = \frac{1}{T_{\text{fiz}}} + \frac{1}{T_{\text{biol}}}$$

$$\lambda_{\text{eff}} = \lambda_{\text{fiz}} + \lambda_{\text{biol}}$$

### DOZIMETRIA

$$D = \frac{\Delta E}{\Delta m}$$

$$D_t = \frac{D}{t}$$

$$X = \frac{\Delta q}{\Delta m}$$

$$D = f_0 \cdot X$$

$$H_T = \sum_R D_{T,R} \cdot w_R$$

$$E = \sum_T H_T \cdot w_T$$

$$D_{\text{levegő}} = K_\gamma \frac{At}{r^2}$$

$$U = \frac{Q}{C} \sim X$$

$$U = IR = \frac{Q}{t} R \sim \frac{X}{t}$$

$$X_i = \frac{I_{tel}}{m}$$

$$D_i = f_0 \cdot X_i$$

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## RÖNTGEN

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$$\varepsilon_{el} = \varepsilon_{kin} = \varepsilon_{foton} + Q = \varepsilon_{foton, max}$$

$$eU = hf_{max} = h \frac{c}{\lambda_{min}}$$

$$\lambda_{min} = \frac{h \cdot c}{e \cdot U} = \frac{k}{U}$$

$$P_{befektetett} = P_{hasznos} + P_{veszteség}$$

$$P_{el} = P_{Rtg} + P_Q$$

$$P_{Rtg} = c_{Rtg} U^2 I Z$$

$$P_{be} = U I$$

$$\eta = P_{Rtg} / P_{be} = c_{Rtg} U Z$$

$$\tau_m = C \lambda^3 Z^3$$

$$\mu = \frac{1}{x} \ln \left( \frac{J_0}{J} \right)$$

$$\mu_m = \frac{\mu}{\rho}$$

$$\tau_m = \mu_m - 0,2 \frac{\text{cm}^2}{\text{g}}$$

$$P = \frac{\Delta E}{\Delta t}$$

$$P_Q = \frac{Q}{\Delta t}$$

$$J = \frac{P}{A}$$

$$A_{gömb} = 4r^2 \pi$$

$$\sin \Theta = \frac{N\lambda}{2d}$$

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## RÖNTGEN - CT

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$$J = J_0 e^{-(\mu_1 \Delta x + \mu_2 \Delta x + \dots + \mu_n \Delta x)} = J_0 e^{-\sum_{i=1}^n \mu_i \Delta x}$$

$$D_i = \lg \frac{J_{i_0}}{J_i} = \lg e \cdot \sum_{j=1}^n \mu_{ij} \Delta x$$

$$D = \lg \frac{J_0}{J} = \sum_{i=1}^n D_i$$

$$HU = \frac{\mu - \mu_{viz}}{\mu_{viz}} 1000$$

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## ERŐSÍTŐ

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$$R = \frac{U}{I}$$

$$P = U \cdot I = \frac{U^2}{R} = I^2 \cdot R$$

$$U_1 = I \cdot R_1 = \frac{U_0}{R_1 + R_2} \cdot R_1 = konst. \cdot R_1$$

$$A_p = \frac{P_{ki}}{P_{be}}$$

$$A_U = \frac{U_{ki}}{U_{be}}$$

$$A_p = \frac{U_{ki}^2 / R_{ki}}{U_{be}^2 / R_{be}} = A_U^2 \frac{R_{be}}{R_{ki}} \approx A_U^2$$

$$n = 10 \cdot \lg A_p \text{ (dB)}$$

$$n = 20 \cdot \lg A_U + 10 \cdot \lg \frac{R_{be}}{R_{ki}} \approx 20 \log A_U \text{ (dB)}$$

$$U = U_{be} - U_{ki} \cdot \beta$$

$$U_{ki} = (U_{be} - U_{ki} \cdot \beta) \cdot A_U$$

$$A_{U,NVCS} = \frac{U_{ki}}{U_{be}} = \frac{A_U}{1 + A_U \beta}$$

$$A_{U,NVCS} \cong \frac{1}{\beta}$$

$$U_{be,max} = U_{coarse} \cdot U_{fine} \cdot 5V$$

$$T_{AMV} = \tau_1 + \tau_2$$

$$D = \frac{\tau_1}{\tau_1 + \tau_2} \cdot 100\%$$

$$f = \frac{1}{T}$$

$$U = U_{t=0} \cdot e^{-\frac{t}{RC}}$$

$$U = U_{t=\infty} \cdot \left(1 - e^{-\frac{t}{RC}}\right)$$

## COULTER SZÁMLÁLÓ

$$R = \rho \frac{l}{A}$$

$$U = I_{gen} \cdot R$$

$$h = \frac{c_{tényl}}{c_{mért}} = \frac{c_{tényl}}{n \cdot 10^4 / \mu l}$$

$$c_{tényl} = h \cdot c_{mért} = h \cdot n \cdot 10^4$$

## IMPULZUSGENERÁTOR

$$I = \frac{\Delta Q}{\Delta t}$$

$$U = \Delta \phi = \frac{\Delta E}{\Delta Q}$$

$$R = \frac{U}{I}$$

$$P = \frac{\Delta E}{\Delta t}$$

$$P = U \cdot I = \frac{U^2}{R} = I^2 \cdot R$$

$$E_C = \frac{1}{2} C U^2$$

$$\tau = R \cdot C$$

## AUDIOMETRIA

$$c = \lambda \cdot f = \frac{\lambda}{T}$$

$$p(t) = p_1 \cdot \sin(\omega t + \varphi)$$

$$Z = c \rho$$

$$J = \frac{P}{A}$$

$$J = \frac{p_{eff}^2}{Z}$$

$$R = \frac{J_{refl}}{J_0} = \left( \frac{Z_1 - Z_2}{Z_1 + Z_2} \right)^2$$

$$n_{oktáv} = \log_2 \frac{f_2}{f_1}$$

$$J_{dB} = 10 \lg \left( \frac{J}{J_0} \right)$$

$$H_{phon} = 10 \lg \left( \frac{J}{J_0} \right)_{1000Hz}$$

$$H_{son} = \frac{1}{16} \left( \frac{J}{J_0} \right)_{1000Hz}^{0,3}$$

$$H_{phon} + 10 phon = H_{son} \cdot 2$$

$$D_{hang} = J_{hang} \cdot t$$

$$J = \eta \frac{U_{eff}^2}{R}$$

$$U_{gen} = U_{coarse} \cdot U_{fine} \cdot 5V$$

$$J_{saját} = AU^2 \left( = 1 \cdot 10^{-5} \cdot U^2 (W / m^2) \right)$$

$$J_{dB,saját} = 10 \lg \left( \frac{J_{saját}}{J_0} \right)$$

$$HV = J_{dB,saját} - J_{dB,norm}$$

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## SZENZOR

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$$\Psi_W = konst. \log \frac{\Phi}{\Phi_0}$$

$$\Psi_S = konst. \left( \frac{\Phi}{\Phi_0} \right)^n$$

$$H_{rel} = konst. \left( \frac{J}{J_0} \right)^n$$

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## EKG

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$$U = \Delta \varphi = \frac{\Delta E}{\Delta q}$$

$$U_{TM} = \varphi_{intracell} - \varphi_{extracell}$$

$$U_{ki} = (U_{be_1} - U_{be_2}) A_U$$

$$U_I = \varphi_L - \varphi_R = U_{frontal} \cdot \cos(0^\circ - \alpha) = U_{frontal} \cdot \cos(\alpha)$$

$$U_{II} = \varphi_F - \varphi = U_{frontal} \cdot \cos(60^\circ - \alpha)$$

$$U_{III} = \varphi_F - \varphi_L = U_{frontal} \cdot \cos(120^\circ - \alpha)$$

$$U_{II} = U_I + U_{III}$$

$$\phi_{CT} = (\phi_L + \phi_R + \phi_F) / 3 = 0$$

$$U_{Vi} = \phi_{Ci} - (\phi_L + \phi_R + \phi_F) / 3$$

$$U_{aVR} = \phi_R - (\phi_L + \phi_F) / 2$$

$$U_{aVL} = \phi_L - (\phi_R + \phi_F) / 2$$

$$U_{aVF} = \phi_F - (\phi_R + \phi_L) / 2$$

$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$

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## ÁRAMLÁS

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$$I_V = \frac{\Delta V}{\Delta t}$$

$$I_V = \frac{A \cdot \overline{\Delta l}}{\Delta t} = A \cdot \bar{v}$$

$$A_1 \cdot \bar{v}_1 = A_2 \cdot \bar{v}_2 = konst.$$

$$I_V = -\frac{\pi}{8\eta} r^4 \frac{\Delta p}{\Delta l}$$

$$Re = \frac{\bar{v} \cdot \rho \cdot r}{\eta}$$

$$v_{krit} = 1160 \frac{\eta}{\rho \cdot r}$$

$$\eta = \frac{\pi}{8} \frac{r^4}{\Delta V} \frac{\overline{\Delta h} \rho g}{l} \Delta t$$

$$\Delta p = R_{cső} I_V \quad (U = RI)$$

$$R_{cső} = 8\pi\eta \frac{l}{A^2}$$

$$R = \frac{U}{I}$$

$$R_{párhuzamos, eredő} = \frac{R}{n}$$

$$I_B = \frac{I_A}{n}$$

$$I_C = \frac{I_A}{m}$$

## DIFFÚZIÓ

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$$J_v = \frac{\Delta v}{\Delta t \Delta A}$$

$$w = 6 \cdot \sqrt{2 \cdot D \cdot t} \quad R_{\text{átlag}} = \sqrt{6 \cdot D \cdot t}$$

$$J_v = -D \cdot \frac{\Delta c}{\Delta x}$$

$$D \cdot \frac{\Delta \left( \frac{\Delta c}{\Delta x} \right)}{\Delta x} = \frac{\Delta c}{\Delta t}$$

$$D = \frac{kT}{6\pi\eta r_{\text{Stokes}}}$$

$$D = 1,38 \cdot 10^{-8} \text{ m}^2/\text{mm}^2 \cdot \text{mered}^2$$

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## TANKÖNYVHÖZ KAPCSOLÓDÓ KÉPLETEK

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### I. AZ „ÉLŐ” ANYAG LEGFONTOSABB SZERKEZETI TULAJDONSÁGAI ÉS SZEREPÜK A BIOLÓGIAI FUNKCIÓKBAN

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$$hf = E_m - E_i \quad (1.1)$$

$$p = \frac{NkT}{V - Nb} - an^2 \quad (1.36)$$

$$\lambda = \frac{h}{p} = \frac{h}{mv} \quad (1.3)$$

$$\left( p + a \frac{N^2}{V^2} \right) (V - Nb) = nkT \quad (1.37)$$

$$\Delta M = [Z \cdot m_p + (A - Z) \cdot m_n] - M(A, Z) \quad (1.19)$$

$$\sigma = konst \cdot e^{-\frac{\Delta \varepsilon}{2kT}} \quad (1.39)$$

$$E = mc^2$$

$$n_s \cong N \cdot e^{-\frac{\varepsilon_s}{kT}} \quad (1.40)$$

$$n_i = n_0 e^{-\frac{\varepsilon_i - \varepsilon_0}{kT}} \quad R = N_A k \quad (1.25)$$

$$c = \frac{\Delta Q}{m \cdot \Delta T}$$

$$\frac{n_{(h)}}{n_{(0)}} = e^{-\frac{mgh}{kT}} \quad (1.26)$$

$$L_o = \frac{\Delta Q_{\text{olvadás}}}{m}$$

$$\frac{n_A}{n_B} = e^{-\frac{qU}{kT}} \quad (1.28)$$

$$L_p = \frac{\Delta Q_{\text{párolgás}}}{m}$$

$$\bar{\varepsilon}_{\text{mozgási}} = \frac{1}{2} m \overline{v^2} = \frac{3}{2} kT \quad (1.34)$$

$$pV = NkT \quad (1.35)$$

$$pV = nRT$$

## II. SUGÁRZÁSOK ÉS KÖLCSÖNHATÁSUK AZ „ÉLŐ” ANYAGGAL

$$n = \frac{c_{\text{vákuum}}}{c_{\text{közeg}}} \qquad \frac{\sin \alpha}{\sin \beta} = \frac{c_1}{c_2} = n_{21} \qquad (\text{II.14})$$

$$N = \frac{K}{T} = \frac{k}{t} \qquad D = \frac{n_2 - n_1}{r} \qquad (\text{II.17})$$

$$N_{\text{szög}} = -\frac{da}{f_{\text{ok}} f_{\text{obj}}} \qquad D = D_1 + D_2 \qquad (\text{II.21})$$

$$f = \frac{1}{T} \qquad \frac{1}{f} = D = \frac{1}{t} + \frac{1}{k} \qquad (\text{II.22})$$

$$c = f\lambda \qquad D = \frac{1}{f} = (n_{21} - 1) \left( \frac{1}{R_1} + \frac{1}{R_2} \right) \qquad (\text{II.23})$$

$$\Delta s = d \sin \alpha_k = k\lambda \qquad c = \frac{\lambda}{T}, \text{ illetve } c = \lambda f \qquad (\text{II.26})$$

$$P = \frac{\Delta E}{\Delta t} \qquad (\text{II.1}) \qquad J \sim A^2 \qquad (\text{II.27})$$

$$M = \frac{\Delta P}{\Delta A} \qquad (\text{II.2}) \qquad J_1 + J_2 \neq J_{\text{eredő}} \qquad (\text{II.28})$$

$$M_\lambda = \frac{\Delta M}{\Delta \lambda} \qquad A_{\text{eredő}}^2 = 2A^2(1 + \cos \Delta\varphi) \qquad (\text{II.31})$$

$$E_{\text{be}} = \frac{\Delta P}{\Delta A} \sim \frac{1}{r^2}, \sim \frac{1}{r} \qquad (\text{II.3}) \qquad \Delta x \approx \Delta s \frac{L}{d} \qquad (\text{II.33})$$

$$I_E = \frac{\Delta E}{\Delta t} \qquad (\text{II.4}) \qquad \Delta\varphi = \Delta s \frac{2\pi}{\lambda} \qquad (\text{II.34})$$

$$J_E = \frac{\Delta E}{\Delta t \Delta A} \qquad (\text{II.5}) \qquad d \approx \lambda \frac{L}{d} \qquad (\text{II.36})$$

$$E_{\text{be}} = E_{\text{be,max}} \cdot \cos \alpha \qquad (\text{II.8}) \qquad E_{\text{mozgási}} = hf - W_{\text{ki}} \qquad (\text{II.37})$$

$$\Delta J = -\mu \Delta x J \qquad (\text{II.10}) \qquad E = E_{\text{mozgási}} + E_{\text{elektron}} + E_{\text{rezgési}} + E_{\text{förgási}}$$

$$J = J_0 e^{-\mu x} \qquad (\text{II.11}) \qquad p = mc = \frac{hf}{c} = \frac{h}{\lambda} \qquad (\text{II.38})$$

$$\mu = \frac{1}{\delta} \qquad \frac{M_{\lambda_i}}{\alpha_{\lambda_i}} = \frac{M_{\lambda_j}}{\alpha_{\lambda_j}} \qquad (\text{II.39})$$

$$J = J_0 2^{-\frac{x}{D}} \qquad (\text{II.12}) \qquad M_{\text{fekete}}(T) = \sigma T^4 \qquad (\text{II.41})$$

$$\mu = \frac{\ln 2}{D} \qquad (\text{II.13})$$

$$\Delta M = \sigma(T_{\text{test}}^4 - T_{\text{környezet}}^4)$$

$$\Delta E = \sigma(T_{\text{test}}^4 - T_{\text{környezet}}^4) \cdot A \cdot t$$

$$\lambda_{\text{max}} T = \text{állandó} \quad (\text{II.42})$$

$$\Delta N_a = K_1 B_{12} N_1 J' \Delta t \quad (\text{II.44})$$

$$\Delta N_{se} = K_1 A N_2 \Delta t \quad (\text{II.45})$$

$$\Delta N_{ie} = K_1 B_{21} N_2 J' \Delta t \quad (\text{II.46})$$

$$\Delta J = JK(N_2 - N_1) \quad (\text{II.54})$$

$$\mu = K(N_1 - N_2) \quad (\text{II.56})$$

$$2L = m\lambda \quad (\text{II.57})$$

$$J = J_0 e^{-\frac{t}{\tau}}$$

$$\rho(\lambda) = \frac{J_{\text{visszavert}}(\lambda)}{J_0(\lambda)}$$

$$\rho(\lambda) = \left( \frac{n_2 - n_1}{n_2 + n_1} \right)^2$$

$$\sigma(\lambda) = \frac{J_{\text{szórt}}(\lambda)}{J_0(\lambda)}$$

$$\sigma(\lambda) \sim \frac{d^6}{\lambda^4}$$

$$J_{\text{szórt}, \lambda} = J_0 \frac{8\pi^4 N \alpha^2}{\lambda^4 R^2} (1 + \cos^2(\beta))$$

$$P_{\text{szórt}} \sim \frac{p_0^2}{c^3} \omega^4 \sim \frac{1}{\lambda^4} \quad (\text{II.60})$$

$$\alpha(\lambda) = \frac{J_{\text{elnyelt}}(\lambda)}{J_0(\lambda)}$$

$$J = J_0 e^{-a \cdot x}$$

$$a = \frac{1}{\delta}$$

$$a = \frac{\ln 2}{D}$$

$$A = \lg \left( \frac{J_0}{J} \right)$$

$$A = \varepsilon(\lambda) \cdot c \cdot x$$

$$\tau(\lambda) = \frac{J_{\text{áteresztett}}(\lambda)}{J_0(\lambda)}$$

$$\rho(\lambda) + \sigma(\lambda) + \alpha(\lambda) + \tau(\lambda) = 1$$

$$\alpha = [\alpha]_D^{20} \cdot c \cdot l$$

$$D = E \cdot t$$

$$H = E \cdot t \cdot S$$

$$2L = m \cdot \lambda$$

$$\kappa = \frac{-\frac{\Delta V}{V}}{\Delta p} \quad (\text{II.63})$$

$$c = \frac{1}{\sqrt{\rho \kappa}} \quad (\text{II.64})$$

$$Z = c\rho \quad (\text{II.67})$$

$$Z = \sqrt{\frac{\rho}{\kappa}} \quad (\text{II.68})$$

$$R = \frac{J_R}{J_0} \quad (\text{II.76})$$

$$R = \left( \frac{Z_1 - Z_2}{Z_1 + Z_2} \right)^2 \quad (\text{II.77})$$

$$Z_{\text{csatoló}} \approx \sqrt{Z_{\text{forrás}} \cdot Z_{\text{bőr}}}$$

$$eU_{\text{anód}} = \varepsilon_{\text{max}} = hf_{\text{max}} \quad (\text{II.79})$$

$$\lambda_{\text{min}} = \frac{hc}{eU_{\text{anód}}} \quad (\text{II.80})$$

$$P_{\text{Rtg}} = c_{\text{Rtg}} U_{\text{anód}}^2 Z I_{\text{anód}} = \eta U_{\text{anód}} I_{\text{anód}} \quad (\text{II.82})$$

$$\eta = \frac{P_{\text{kisugárzott}}}{P_{\text{befektetett}}} = c_{\text{Rtg}} \cdot U_{\text{anód}} \cdot Z \quad (\text{II.83})$$

$$J = J_0 e^{-\mu \cdot x} \quad (\text{II.84})$$

$$\mu = \mu_m \rho \quad x_m = \rho x \quad (\text{II.85})$$

$$\tau = \tau_m \rho \quad \sigma = \sigma_m \rho \quad \kappa = \kappa_m \rho$$

$$\varepsilon = hf = E_{\text{kötési}} + E_{\text{mozgási}} \quad (\text{II.86})$$

$$\tau_m = \frac{\tau}{\rho} = C_{\text{foto}} \lambda^3 Z^3 \quad (\text{II.87})$$

$$Z_{\text{eff}} = \sqrt[3]{\sum_{i=1}^n w_i Z_i^3} \quad (\text{II.88})$$

$$hf = E_{\text{kötési}} + hf' + E_{\text{mozgási}} \quad (\text{II.89})$$

$$\frac{\Delta N}{\Delta t} = -\lambda N \quad (\text{II.95})$$

$$N = N_0 e^{-\lambda t} \quad \lambda = \frac{1}{\tau} \quad (\text{II.96})$$

$$\frac{N_0}{2} = N_0 e^{-\lambda T} \quad (\text{II.97})$$

$$\lambda T = \ln 2 \quad (\text{II.98})$$

$$\frac{1}{T_{\text{eff}}} = \frac{1}{T_{\text{fiz}}} + \frac{1}{T_{\text{biol}}}$$

$$\lambda_{\text{eff}} = \lambda_{\text{fiz}} + \lambda_{\text{biol}}$$

$$A = -\frac{\Delta N}{\Delta t} \quad (\text{II.99})$$

$$A = A_0 e^{-\lambda t} \quad (\text{II.101})$$

$$s = \frac{\Delta E}{\Delta x}$$

$$s = s_m \rho$$

$$\mu = \tau + \sigma + \kappa \quad (\text{II.102})$$

$$\mu_m = \tau_m + \sigma_m + \kappa_m$$

$$E_\gamma = A + E_{\text{e,kin}}$$

$$E_\gamma = A + E_{\text{e,kin}} + E'_\gamma$$

$$E_\gamma = hf = 2m_e c^2 + E_{\text{e,kin}} + E_{p,\text{kin}} \quad (\text{II.103})$$

$$qvB = \frac{mv^2}{r}$$

$$D = \frac{\Delta E}{\Delta m} \quad (\text{II.105})$$

$$D_{\text{levegő}} = K_\gamma \frac{At}{r^2}$$

$$X = \frac{\Delta Q}{\Delta m} \quad (\text{II.106})$$

$$D_{\text{levegő}} = f_0 X \quad (\text{II.107})$$

$$D \sim \mu_m J, \text{ illetve } D \sim s_m$$

$$H_T = \sum_R w_R D_{\text{TR}} \quad (\text{II.108})$$

$$\sum_T w_T = 1 \quad (\text{II.109})$$

$$E = \sum_T w_T H_T \quad (\text{II.110})$$

$$S = \sum_i N_i E_i \quad (\text{II.111})$$

$$S_T = \sum_i N_i H_{T,i} \quad (\text{II.112})$$

### III. TRANSPORTJELENSÉGEK ÉLŐ RENDSZEREKBE

$$I_V = \frac{\Delta V}{\Delta t} \quad (III.1) \qquad l = \bar{v} \tau \quad (III.25)$$

$$I_V = A \bar{v} = \text{állandó} \quad (III.4) \qquad v_{\text{drift}} = \frac{F}{m} \tau \quad (III.26)$$

$$p + \frac{1}{2} \rho v^2 + \rho g h = \text{állandó} \quad (III.5) \qquad I_N = \frac{\Delta N}{\Delta t} \quad (III.28)$$

$$F = \eta A \frac{\Delta v}{\Delta h} \quad (III.6) \qquad I_v = \frac{\Delta v}{\Delta t} \quad (III.29)$$

$$\eta = \frac{\tau}{D} \qquad J_v = \frac{\Delta I_v}{\Delta A} \quad (III.30)$$

$$I_V = -\frac{\pi}{8\eta} R^4 \frac{\Delta p}{\Delta l} \quad (III.12) \qquad J_v = -D \frac{\Delta c}{\Delta x} \quad (III.31)$$

$$R_{\text{cső}} = 8\pi \eta \frac{\Delta l}{(r^2 \pi)^2} \quad (III.14) \qquad D = \frac{1}{3} v l = u k T \quad (III.33)$$

$$\text{Re} = \frac{\bar{v} \cdot \rho \cdot r}{\eta} \qquad D = \frac{k \cdot T}{6 \cdot \pi \cdot \eta \cdot r_{\text{Stokes}}} \quad (III.34)$$

$$v_{\text{krit}} = \text{Re} \frac{\eta}{\rho r} \quad (III.17) \qquad -\frac{\Delta J_v}{\Delta x} = \frac{\Delta c}{\Delta t} \quad (III.38)$$

$$\sigma_\theta = \frac{P \cdot r}{t} = \frac{F}{t \cdot l} \qquad D \frac{\Delta \left( \frac{\Delta c}{\Delta x} \right)}{\Delta x} = \frac{\Delta c}{\Delta t} \quad (III.39)$$

$$C = \frac{\Delta V}{\Delta P} \qquad \sigma_x \sim \overline{R(t)} \sim \sqrt{Dt} \quad (III.40)$$

$$\Delta p = \frac{2\gamma}{R} \qquad \overline{R(t)} = \sqrt{N l^2} = \sqrt{3Dt}$$

$$P_{\text{total}} = \sum_{i=1}^n P_i \qquad p_{\text{ozmózis}} = cRT \quad (III.50)$$

$$p = k_H c \qquad \text{ozm.} = \sum (\varphi_i n_i c_i) \qquad J_v = -L_T \frac{\Delta T}{\Delta x} \quad (III.51)$$

$$F = 6\pi \eta r v \quad (III.18) \qquad J_E = -\lambda \frac{\Delta T}{\Delta x} \quad (III.53)$$

$$u = \frac{v}{F} = \frac{1}{6\pi \eta r} \quad (III.19) \qquad J = LX \quad J = \frac{\Delta x_{\text{ext}}}{A \Delta t} \quad X = -\frac{\Delta y_{\text{int}}}{\Delta x} \quad (III.54)$$

$$v_{\text{átl}} = \sqrt{\frac{3kT}{m}} \quad (III.24) \qquad \Delta E = Q_E + W \quad Q_E = cm \Delta T \quad (III.56)$$

$$W_V = -p\Delta V \quad W_Q = \varphi\Delta Q \quad W_v = \mu\Delta v \quad (\text{III.58})$$

$$W^{(i)} = y_{\text{int}}^{(i)} \Delta x_{\text{ext}}^{(i)} \quad (\text{III.59})$$

$$W_{vQ} = W_v + W_Q = (\mu + zF\varphi)\Delta v = \mu_e \Delta v \quad (\text{III.61})$$

$$Q_E = T\Delta S \quad (\text{III.63})$$

$$\Delta E = \sum_{(i)} y_{\text{int}}^{(i)} \Delta x_{\text{ext}}^{(i)} \quad (\text{III.64})$$

$$W_{\text{mech}} = -n \cdot R \cdot T \cdot \ln \frac{V_2}{V_1}$$

$$W_{\text{kém}} = -n \cdot R \cdot T \cdot \ln \frac{c_2}{c_1}$$

$$\Delta S = c \cdot m \cdot \ln \frac{T_2}{T_1}$$

$$\Delta S = \frac{\Delta E_1}{T_1} + \frac{\Delta E_2}{T_2} = \Delta E \left( \frac{1}{T_1} - \frac{1}{T_2} \right) \quad (\text{III.67})$$

$$S = k \ln \Omega \quad (\text{III.72})$$

$$\frac{P_i}{P_j} = \frac{\Omega_i}{\Omega_j} = \frac{e^{\frac{S_i}{k}}}{e^{\frac{S_j}{k}}} = e^{\frac{S_i - S_j}{k}} \quad (\text{III.74})$$

$$\Delta U = T\Delta S - p\Delta V + \sum_{i=1}^n \mu_i \Delta v_i + \varphi \Delta q + A \Delta \xi$$

$$E = TS - pV + \mu v \quad (\text{III.83})$$

$$H = E + pV \quad (\text{III.84})$$

$$\Delta H_p = Q_E + W_v \quad (\text{III.87})$$

$$\Delta H_{p,v} = Q_E \quad (\text{III.88})$$

$$F = E - TS \quad (\text{III.89})$$

$$\Delta F_T = W_V + W_v \quad (\text{III.91})$$

$$\Delta F_{T,v} = W_V \quad (\text{III.92})$$

$$\Delta F_{T,V} = W_v \quad (\text{III.93})$$

$$G = H - TS \quad (\text{III.94})$$

$$\Delta G_{T,p} = W_v \quad (\text{III.96})$$

$$\Delta G_{T,p} \leq 0 \quad (\text{III.99})$$

$$\Delta F_{T,V} \leq 0 \quad (\text{III.100})$$

$$\Delta H_{S,p} \leq 0 \quad (\text{III.101})$$

$$G = \mu_A v_A + \mu_B v_B \quad (\text{III.105})$$

$$\mu_A = \mu^0_A + RT \ln(c_A) \quad (\text{III.109})$$

$$\mu^e = \mu + ZF\varphi$$

$$J_m = -p(c_{v_2} - c_{v_1}) \quad (\text{III.113})$$

$$p = \frac{D}{d}$$

$$J_k = -L_k \frac{\Delta \mu_e}{\Delta x} \quad (\text{III.116})$$

$$L_k = c_k \frac{D_k}{RT} = \frac{c_k u_k}{N_A} \quad (\text{III.118})$$

$$J_k = -D_k \left( \frac{\Delta c_k}{\Delta x} + c_k \frac{z_k F}{RT} \frac{\Delta \varphi}{\Delta x} \right) \quad (\text{III.119})$$

$$U = \frac{RT}{F} \ln \frac{\sum_{k=1}^m p_k^+ c_{k,\text{II}}^+ + \sum_{k=1}^n p_k^- c_{k,\text{I}}^-}{\sum_{k=1}^m p_k^+ c_{k,\text{I}}^+ + \sum_{k=1}^n p_k^- c_{k,\text{II}}^-} \quad (\text{III.121})$$

$$U = \varphi^{\text{II}} - \varphi^{\text{I}} = \frac{RT}{z_i F} \ln \frac{c_i^{\text{I}}}{c_i^{\text{II}}} \quad (\text{III.123})$$

$$U_m(t) = U_t \left( 1 - e^{-\frac{t}{R_m C_m}} \right) \quad (\text{III.130})$$

$$\tau = R_m C_m \quad (\text{III.131})$$

$$\lambda \approx \sqrt{\frac{R_m}{R_i + R_e}} \approx \sqrt{\frac{R_m}{R_i}}$$

$$U_m(t) = U_t e^{-\frac{t}{R_m C_m}} \quad (\text{III.132})$$

$$U_m(x) - U_m(0) = U_t e^{-\frac{x}{\lambda}} \quad (\text{III.133})$$

## IV. AZ ÉRZÉKSZERVEK BIOFIZIKÁJA

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$$\Psi_W = konst. \log \frac{\Phi}{\Phi_0} \quad (IV.6) \quad n_{\text{oktáv}} = \log_2 \frac{f_2}{f_1} \quad (IV.22)$$

$$\Psi_S = konst. \left( \frac{\Phi}{\Phi_0} \right)^n \quad (IV.8) \quad p(t) = p_{\text{max}} \cdot \sin(\omega t + \varphi) \quad (IV.23)$$

$$P = J \cdot \pi \cdot \left( \frac{d}{2} \right)^2 \quad (IV.9) \quad R = \frac{J_{\text{refl}}}{J_0} = \left( \frac{Z_1 - Z_2}{Z_1 + Z_2} \right)^2$$

$$\frac{P_{\text{max}}}{P_{\text{min}}} = \left( \frac{d_{\text{max}}}{d_{\text{min}}} \right)^2 = 16 \quad (IV.10) \quad F_{\text{dob}} = p_{\text{lev}} \cdot A_{\text{dob}} \quad n = 10 \lg \left( \frac{P_{\text{ki}}}{P_{\text{be}}} \right) = 10 \lg \left( \frac{J_{\text{ki}}}{J_{\text{be}}} \right) \quad (IV.26)$$

$$D = \frac{n - n'}{r} \quad (IV.11) \quad n = n_{\text{erősítés}} + n_{\text{csillapítás}} \quad (IV.27)$$

$$D = \frac{n_t}{t} + \frac{n_k}{k} \quad (IV.12) \quad n = 10 \lg \left( \frac{J}{J_0} \right) \quad (IV.28)$$

$$\text{visus} = \frac{1(^{\circ})}{\alpha(^{\circ})} 100\% \quad (IV.14) \quad H_{\text{phon}} = 10 \lg \left( \frac{J}{J_0} \right)_{1000\text{Hz}} \quad (IV.29)$$

$$\alpha_H = 1,22 \cdot \frac{\lambda}{d} \quad (IV.15) \quad H_{\text{son}} = \frac{1}{16} \left( \frac{J}{J_0} \right)_{1000\text{Hz}}^{0,3} \quad (IV.31)$$

$$A = \frac{E_{\text{ion}}}{E_{\text{foton}}} = \frac{ne\Delta\varphi}{hf} \quad H_{\text{phon}} + 10 \text{ phon} = H_{\text{son}} \cdot 2$$

$$X = rR + gG + bB$$

## V. BIOMECHANIKA

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$$\frac{F}{A} = E \frac{\Delta L}{L} \quad (V.1) \quad E = \frac{\sigma}{\varepsilon}$$

$$\sigma = \frac{F}{A} \quad c_{\text{hang}} = \frac{1}{\sqrt{\rho \cdot \kappa}}$$

$$\varepsilon = \frac{\Delta L}{L} \quad \kappa = \frac{-\Delta V / V}{\Delta p}$$

$$\sigma = \eta \frac{\Delta \varepsilon}{\Delta t}$$

$$(R^2)_{\text{átlag}} = 2L_p L \quad (\text{V.3})$$

$$r = \frac{\tau_{be}}{\tau_{be} + \tau_{ki}} = \frac{\tau_{be}}{\tau_{teljes}} \quad (\text{V.4})$$

$$v_{\text{csapás}} = \frac{\delta}{\tau_{be}}$$

$$\tau_{\text{teljes}} = \frac{1}{k_{\text{ATPáz}}}$$

$$r = \frac{\delta \cdot k_{\text{ATPáz}}}{v_{\text{csapás}}}$$

$$P = Fv \quad (\text{V.5})$$

$$(F + a)(v + b) = (F_0 + a)b$$

$$v_{\text{max}} = \frac{bF_0}{a}$$

$$\frac{\Delta L}{L} = \alpha \cdot \Delta T$$

$$\frac{\Delta V}{V} = \beta \cdot \Delta T$$

## VI. A MOLEKULÁRIS ÉS SEJTDIAGNOSZTIKA FIZIKAI MÓDSZEREI

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$$N_{\text{szög}} = \frac{\text{tg } \beta}{\text{tg } \alpha} = a \left( \frac{1}{f} - \frac{1}{k} \right) \quad (\text{VI.18})$$

$$Q_{ST} = \frac{k_{isc}}{k_f + k_{nr}}$$

$$N_{k=\infty} = -\frac{a}{f} \quad (\text{VI.20})$$

$$Q_{ph} = Q_{ST} \frac{k_{ph}}{k_{ph} + k_{nr,ph}} \quad (\text{VI.37})$$

$$N_{\text{szög}} = -\frac{da}{f_1 f_2} \quad (\text{VI.23})$$

$$\Delta N = -(k_f + k_{nr}) \cdot N \cdot \Delta t \quad (\text{VI.38})$$

$$\Delta s = d \sin \alpha_k = k\lambda \quad (\text{VI.24})$$

$$N = N_0 e^{-(k_f + k_{nr})t} \quad (\text{VI.39})$$

$$\delta = 0,61 \frac{\lambda}{n \sin \omega} \quad f = \frac{1}{\delta} \quad (\text{VI.28})$$

$$\tau = \frac{1}{k_f + k_{nr}} \quad (\text{VI.40})$$

$$J = J_0 e^{-\mu \cdot x} \quad (\text{VI.29})$$

$$Q_f = k_f \tau \quad (\text{VI.41})$$

$$T = \frac{J}{J_0} (100\%) \quad (\text{VI.33})$$

$$p = \frac{J_{VV} - J_{VH}}{J_{VV} + J_{VH}} \quad (\text{VI.43})$$

$$A = \lg \left( \frac{J_0}{J} \right) = \varepsilon(\lambda) c x \quad (\text{VI.34})$$

$$D = \frac{w^2}{4t_D}$$

$$Q_F = \frac{k_f}{k_f + k_{nr}} = \frac{k_f}{k_f + k_{ic} + k_{isc} + k_Q} \quad (\text{VI.36})$$

$$F = k \frac{Q_1 Q_2}{r^2}$$

$$E = \frac{F}{q}$$

$$U_{21} = \frac{W_{1 \rightarrow 2}}{q} \quad \phi_i = \frac{W_{0 \rightarrow i}}{q}$$

$$U_{21} = E \cdot s$$

$$C = \frac{Q}{U}$$

$$C = \epsilon_0 \epsilon_r \frac{A}{l}$$

$$W = \frac{1}{2} UQ = \frac{1}{2} CU^2 = \frac{1}{2} \frac{Q^2}{C}$$

$$C_{\text{párhuzamos,eredő}} = C_1 + C_2$$

$$\frac{1}{C_{\text{soros,eredő}}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$I = \frac{\Delta Q}{\Delta t}$$

$$J = \frac{\Delta Q}{A \cdot \Delta t}$$

$$R = \frac{U}{I}$$

$$G = \frac{1}{R} = \frac{I}{U}$$

$$R = \rho \frac{l}{A}$$

$$\sigma = \frac{1}{\rho}$$

$$R_{\text{soros,eredő}} = R_1 + R_2$$

$$\frac{1}{R_{\text{párhuzamos,eredő}}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$W = U \cdot I \cdot t$$

$$P = U \cdot I = \frac{U^2}{R} = I^2 \cdot R$$

$$U_R = U_T e^{-\frac{t}{RC}} \quad U_C = U_T \left(1 - e^{-\frac{t}{RC}}\right) \quad (\text{VII.2})$$

$$I = I_{\max} \sin(2\pi \cdot f \cdot t)$$

$$U = U_{\max} \sin(2\pi \cdot f \cdot t)$$

$$I_{\text{eff}} = \frac{I_{\max}}{\sqrt{2}}$$

$$U_{\text{eff}} = \frac{U_{\max}}{\sqrt{2}}$$

$$P = U_{\text{eff}} \cdot I_{\text{eff}}$$

$$Z = \frac{U_{\text{eff}}}{I_{\text{eff}}}$$

$$X_C = \frac{1}{2\pi f C} = \frac{1}{\omega C} \quad (\text{VII.4})$$

$$U_{\text{ki}} = U_{\text{be}} \frac{R}{\sqrt{R^2 + X_C^2}} \quad (\text{VII.5})$$

$$U_{\text{ki, alulvágó}} = U_{\text{be}} \frac{RC\omega}{\sqrt{1 + C^2 R^2 \omega^2}}$$

$$U_{\text{ki, felülvágó}} = U_{\text{be}} \frac{1}{\sqrt{1 + C^2 R^2 \omega^2}}$$

$$f_0 = \frac{1}{2\pi RC}$$

$$f_0 = \frac{1}{2\pi \sqrt{LC}}$$

$$A_U = \frac{U_{ki}}{U_{be}} \quad A_P = \frac{P_{ki}}{P_{be}} \quad (\text{VII.6})$$

$$A_{U,V^-} = \frac{A_U}{1 + A_U \beta} \quad (\text{VII.14})$$

$$A_P = A_U^2 \quad \text{ha } R_{ki} = R_{be} \quad (\text{VII.8})$$

$$\beta = \frac{U_{vissza}}{U_{ki}}$$

$$n = 10 \lg A_P = 20 \lg A_U \quad (\text{VII.10})$$

$$U_{ki} = \frac{R_2}{R_1 + R_2} \cdot U_{be}$$

$$H = \sum_i p_i \cdot \log_2 \frac{1}{p_i}$$

$$U_{ki} = (U_{be_1} - U_{be_2}) A_U \quad (\text{VII.11})$$

$$A_{U,V^+} = \frac{A_U}{1 - A_U \beta}$$

## VIII. KÉPALKOTÓ MÓDSZEREK

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$$J = J_0 e^{-(\mu_1 \Delta x + \mu_2 \Delta x + \dots + \mu_n \Delta x)} = J_0 e^{-\sum_{i=1}^n \mu_i \Delta x}$$

$$\frac{\Delta l}{l} = E \times d$$

$$\lg \frac{J_0}{J} = (\mu_1 x_1 + \mu_2 x_2 + \dots) \lg e \quad (\text{VIII.2})$$

$$c = \sqrt{\frac{Y}{\rho}} = \sqrt{\frac{1}{\kappa \rho}}$$

$$hf_0 = g_N \mu_N H_0 \quad (\text{VIII.3})$$

$$f' = f \left( 1 \pm \frac{v}{c} \right) \quad (\text{VIII.4})$$

$$M_{long}(t) = M_{long}(0) \cdot \left( 1 - e^{-\frac{t}{T_1}} \right)$$

$$f_D = f' - f = \frac{\pm v}{c} f \quad f_D = \frac{\pm 2v}{c} f \quad (\text{VIII.5})$$

$$M_{transz}(t) = M_{transz}(0) \cdot e^{-\frac{t}{T_2}}$$

$$HU = \frac{\mu - \mu_{v\acute{e}z}}{\mu_{v\acute{e}z}} 1000 \quad (\text{VIII.10})$$

$$P = d \times \frac{F}{A}$$

## IX. TERÁPIÁS MÓDSZEREK FIZIKAI ALAPJAI

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$$a_{k\ddot{u}sz\ddot{o}b} = \frac{q}{\tau} + r$$

$$2r = \frac{q}{C} + r$$

$$k_t = \frac{1}{\tau_D} \frac{R_0^6}{R^6} \quad (\text{X.6})$$

$$2d \sin \theta = n \cdot \lambda$$

$$\vec{F}_{el} = \vec{E} \cdot q$$

$$\vec{F}_{mágn} = q \cdot \vec{v} \times \vec{B}$$

$$\vec{F}_{cp} = m \cdot \frac{\vec{v}^2}{r}$$

$$\frac{m}{q} = \frac{\vec{E} + \vec{v} \times \vec{B}}{\vec{a}}$$

$$r_{el} = \frac{mv^2}{Eq}$$

$$r_m = \frac{1}{B} \sqrt{\frac{2mU}{q}}$$

$$t = \frac{d}{\sqrt{2U}} \sqrt{\frac{m}{q}}$$

$$L = \sqrt{l(l+1)}\hbar \quad (\text{X.26})$$

$$M_N = \gamma_N L = g_N \mu_N \sqrt{l(l+1)} \quad (\text{X.28})$$

$$M_e = -g \mu_B \sqrt{S(S+1)} \quad (\text{X.29})$$

$$\Delta E = hf_0 = g_N \mu_N H_0 \quad (\text{X.30})$$

$$\Delta E = \frac{h\omega_0}{2\pi}$$

$$\omega_0 = \gamma B_0$$

$$f_{Larmor} = \frac{\gamma}{2\pi} B_0$$

$$\frac{N_\beta}{N_\alpha} = e^{-\frac{\Delta E}{kT}} \quad (\text{X.31})$$

## ÁLLANDÓK ÉS ADATOK

egyetemes gázállandó	$R = 8,314 \text{ J}/(\text{mol}\cdot\text{K})$
Avogadro-szám	$N_A = 6\cdot 10^{23} /\text{mol}$
Boltzmann-állandó	$k = 1,38\cdot 10^{-23} \text{ J}/\text{K}$
Faraday-állandó	$F = 96500 \text{ C}/\text{mol}$
Planck-állandó	$h = 6,626\cdot 10^{-34} \text{ J}\cdot\text{s}$
fénysebesség (vákuumban)	$c = 3\cdot 10^8 \text{ m}/\text{s}$
elektron töltése (elemi töltés)	$e = 1,6\cdot 10^{-19} \text{ C}$
elektron nyugalmi tömege	$m_e = 9,1\cdot 10^{-31} \text{ kg}$
proton nyugalmi tömege	$m_p = 1,673\cdot 10^{-27} \text{ kg}$
neutron nyugalmi tömege	$m_n = 1,675\cdot 10^{-27} \text{ kg}$
Stefan–Boltzmann-állandó	$\sigma = 5,67\cdot 10^{-8} \text{ J}/(\text{m}^2\cdot\text{K}^4\cdot\text{s})$
Wien-féle eltolódási állandó	$b = 2,898\cdot 10^{-3} \text{ m}\cdot\text{K}$
nehézségi gyorsulás (normál érték)	$g = 9,81 \text{ m}/\text{s}^2$
Reynolds-szám (sima falú csövekre)	$Re = 1160$
Röntgenkonstans	$C_{\text{Rtg}} = 1,1\cdot 10^{-9} \text{ V}^{-1}$
proton g faktora	$g_p = 5,59$
nukleáris magneton	$\mu_N = 5,05\cdot 10^{-27} \text{ J}/\text{T}$
Fotoeffektushoz tartozó állandó	$C_{\text{foto}} = 6 \text{ cm}^2/(\text{g}\cdot\text{nm}^3)$
Konverziós tényező levegőre	$f_0 = 34 \text{ J}/\text{C}$
Coulomb-féle arányossági tényező	$k = 9\cdot 10^9 \text{ Nm}^2/\text{C}^2$
vákuum dielektromos állandója	$\epsilon_0 = 8,85\cdot 10^{-12} \text{ C}^2/(\text{Nm}^2)$
hallásküszöb (emberi fül, 1kHz)	$10^{-12} \text{ W}/\text{m}^2$
képtávolság a redukált szemben	$i = 17 \text{ mm}$

## AZ ELEMEEK PERIÓDUSOS RENDSZERE

1 <b>H</b> Hidrogén 1.00794																	2 <b>He</b> Hélium 4.003																												
3 <b>Li</b> Lítium 6.941	4 <b>Be</b> Berillium 9.012182											5 <b>B</b> Bór 10.811	6 <b>C</b> Szén 12.0107	7 <b>N</b> Nitrogén 14.00674	8 <b>O</b> Oxigén 15.9994	9 <b>F</b> Fluor 18.9984032	10 <b>Ne</b> Neon 20.1797																												
11 <b>Na</b> Szódium 22.989770	12 <b>Mg</b> Magnézium 24.3050											13 <b>Al</b> Alumínium 26.9815386	14 <b>Si</b> Szilícium 28.0855	15 <b>P</b> Foszfor 30.973761	16 <b>S</b> Kén 32.066	17 <b>Cl</b> Klór 35.4527	18 <b>Ar</b> Argon 39.948																												
19 <b>K</b> Kálium 39.0983	20 <b>Ca</b> Kalcium 40.078	21 <b>Sc</b> Szkandium 44.955910	22 <b>Ti</b> Titán 47.867	23 <b>V</b> Vanádium 50.9415	24 <b>Cr</b> Krom 51.9961	25 <b>Mn</b> Mangán 54.938045	26 <b>Fe</b> Vas 55.845	27 <b>Co</b> Kobalt 58.933200	28 <b>Ni</b> Nikkel 58.6934	29 <b>Cu</b> Réz 63.546	30 <b>Zn</b> Cink 65.39	31 <b>Ga</b> Gallium 69.723	32 <b>Ge</b> Germánium 72.61	33 <b>As</b> Arzén 74.92160	34 <b>Se</b> Szelén 78.96	35 <b>Br</b> Brom 79.904	36 <b>Kr</b> Kripton 83.80																												
37 <b>Rb</b> Rubídium 85.4678	38 <b>Sr</b> Stroncium 87.62	39 <b>Y</b> Ittrium 88.90585	40 <b>Zr</b> Cirkónium 91.224	41 <b>Nb</b> Nióbium 92.90638	42 <b>Mo</b> Molibdén 95.94	43 <b>Tc</b> Technécium (98)	44 <b>Ru</b> Ruténium 101.07	45 <b>Rh</b> Ródium 102.90550	46 <b>Pd</b> Palládium 106.42	47 <b>Ag</b> Ezüst 107.8682	48 <b>Cd</b> Kadmium 112.411	49 <b>In</b> Indium 114.818	50 <b>Sn</b> Ón 118.710	51 <b>Sb</b> Antimon 121.760	52 <b>Te</b> Tellúr 127.60	53 <b>I</b> Jód 126.90447	54 <b>Xe</b> Xenon 131.29																												
55 <b>Cs</b> Cézium 132.90545	56 <b>Ba</b> Bárium 137.327	57 <b>La</b> Lantán 138.9055	72 <b>Hf</b> Hafnium 178.49	73 <b>Ta</b> Tantál 180.9479	74 <b>W</b> Wolfrám 183.84	75 <b>Re</b> Rénium 186.207	76 <b>Os</b> Ozmium 190.23	77 <b>Ir</b> Iridium 192.217	78 <b>Pt</b> Platina 195.078	79 <b>Au</b> Arany 196.96656	80 <b>Hg</b> Higany 200.59	81 <b>Tl</b> Tallium 204.3833	82 <b>Pb</b> Ólom 207.2	83 <b>Bi</b> Bismut 208.98038	84 <b>Po</b> Polónium (209)	85 <b>At</b> Asztácium (210)	86 <b>Rn</b> Radon (222)																												
87 <b>Fr</b> Francium (223)	88 <b>Ra</b> Rádium (226)	89 <b>Ac</b> Aktínium (227)	104 <b>Rf</b> Rutherfordium (261)	105 <b>Db</b> Dubnium (262)	106 <b>Sg</b> Seaborgium (263)	107 <b>Bh</b> Bohrium (262)	108 <b>Hs</b> Hassium (265)	109 <b>Mt</b> Meitnerium (266)	110 (269)	111 (272)	112 (277)	113	114																																
<table border="1"> <tbody> <tr> <td>58 <b>Ce</b> Cérium 140.116</td> <td>59 <b>Pr</b> Prazeodímium 140.90768</td> <td>60 <b>Nd</b> Neodímium 144.24</td> <td>61 <b>Pm</b> Prométium (145)</td> <td>62 <b>Sm</b> Szamárium 150.36</td> <td>63 <b>Eu</b> Eurórium 151.964</td> <td>64 <b>Gd</b> Gadolínium 157.25</td> <td>65 <b>Tb</b> Terbium 158.92534</td> <td>66 <b>Dy</b> Diszpródium 162.50</td> <td>67 <b>Ho</b> Holmium 164.93032</td> <td>68 <b>Er</b> Erbium 167.26</td> <td>69 <b>Tm</b> Tulium 168.93421</td> <td>70 <b>Yb</b> Itterbium 173.04</td> <td>71 <b>Lu</b> Lutecium 174.967</td> </tr> <tr> <td>90 <b>Th</b> Tórium 232.0381</td> <td>91 <b>Pa</b> Protaktínium 231.03588</td> <td>92 <b>U</b> Urán 238.0289</td> <td>93 <b>Np</b> Neptúnium (237)</td> <td>94 <b>Pu</b> Plutónium (244)</td> <td>95 <b>Am</b> Americium (243)</td> <td>96 <b>Cm</b> Kürium (247)</td> <td>97 <b>Bk</b> Berkélium (247)</td> <td>98 <b>Cf</b> Kalifornium (251)</td> <td>99 <b>Es</b> Einsteinium (252)</td> <td>100 <b>Fm</b> Fermium (257)</td> <td>101 <b>Md</b> Mendelevium (258)</td> <td>102 <b>No</b> Nobélium (259)</td> <td>103 <b>Lr</b> Laurencium (262)</td> </tr> </tbody> </table>																		58 <b>Ce</b> Cérium 140.116	59 <b>Pr</b> Prazeodímium 140.90768	60 <b>Nd</b> Neodímium 144.24	61 <b>Pm</b> Prométium (145)	62 <b>Sm</b> Szamárium 150.36	63 <b>Eu</b> Eurórium 151.964	64 <b>Gd</b> Gadolínium 157.25	65 <b>Tb</b> Terbium 158.92534	66 <b>Dy</b> Diszpródium 162.50	67 <b>Ho</b> Holmium 164.93032	68 <b>Er</b> Erbium 167.26	69 <b>Tm</b> Tulium 168.93421	70 <b>Yb</b> Itterbium 173.04	71 <b>Lu</b> Lutecium 174.967	90 <b>Th</b> Tórium 232.0381	91 <b>Pa</b> Protaktínium 231.03588	92 <b>U</b> Urán 238.0289	93 <b>Np</b> Neptúnium (237)	94 <b>Pu</b> Plutónium (244)	95 <b>Am</b> Americium (243)	96 <b>Cm</b> Kürium (247)	97 <b>Bk</b> Berkélium (247)	98 <b>Cf</b> Kalifornium (251)	99 <b>Es</b> Einsteinium (252)	100 <b>Fm</b> Fermium (257)	101 <b>Md</b> Mendelevium (258)	102 <b>No</b> Nobélium (259)	103 <b>Lr</b> Laurencium (262)
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## SÚRÚSÉG

elemek	$\rho$ (g/cm <sup>3</sup> )	összetett anyagok	$\rho$ (g/cm <sup>3</sup> )
alumínium (Al)	2,7	testszövet (lágy)	1,04
réz (Cu)	8,96	vér (átlagos)	1,05
ón (Sn)	5,75	levegő (0°C, 101 kPa)	0,00129
vas (Fe)	7,9	csont (átlagos)	1,7
ezüst (Ag)	10,5	zsírszövet (átlagos)	0,92
higany (Hg)	13,6	izom (átlagos)	1,06
arany (Au)	19,3	víz (4°C)	1,000
ólom (Pb)	11,3	jég (0°C)	0,92
szén (C, grafit)	2,23	etanol	0,8
szén (C, gyémánt)	3,51	cirkónium-dioxid (ZrO <sub>2</sub> )	6,0
szén (C, fullerén)	1,65	amalgám (átlagos)	12
titán (Ti)	4,51	Kvarc (SiO <sub>2</sub> )	2,65
		PMMA (poli(metil-metakrilát))	1,2

### FELÜLETI FESZÜLTSG

anyag	$\sigma$ (mJ/m <sup>2</sup> )
víz	73
higany	486
etilalkohol	22

### FAJLAGOS HŐKAPACITÁS

anyag	c (kJ/(kg·K))
volfrám (W)	0,132
víz	4,18
jég	2,094
etanol	2,4
izom	3,76
vér	3,9
tömör csont (átlagos)	1,3
zsírszövet	3
testszövet (átlagos)	3,5
oxigén (C <sub>v</sub> )	0,65
oxigén (C <sub>p</sub> )	0,92

### ÁTALAKULÁSI HŐ

anyag	q (kJ/kg)
jég (olvadáshő)	334,4
víz (párolgáshő (100°C, 101 kPa))	2257
víz (párolgáshő (30°C, 101 kPa))	2400

### FAJLAGOS VEZETŐKÉPESSÉG

anyag	$\sigma$ (S/m)
izomszövet	0,8

### LINEÁRIS HŐTÁGULÁSI EGYÜTTHATÓ

anyag	$\alpha$ (10 <sup>-6</sup> 1/K)
alumínium	24
acél	12
amalgám	25
jég	51
teflon	200

### ABSZOLÚT TÖRÉSMUTATÓ

anyag	n (589 nm, 20°C)
levegő	1
víz	1,333
cédrusolaj	1,505
gyémánt	2,417
üveg	1,5
flintüveg	1,6
prizma (refraktométerben)	1,739

### FAJLAGOS FORGATÓKÉPESSÉG

anyag	$[\alpha]_D^{20} \left( \frac{^\circ \cdot \text{cm}^3}{\text{g} \cdot \text{dm}} \right)$
D-glükóz (dextróz)	+52,7
D-szacharóz	+66,5
D-galaktóz	+80,2
D-laktóz	+55,3
D-fruktóz (levulóz)	-93,8
D-maltóz	+137,5

## HANGSEBESSÉG

anyag	c (m/s)
levegő	330
hélium	970
víz	1500
testszövet (lágy)	1600
csont	3600

## TÖMEGGYENGÍTÉSI EGYÜTTHATÓ

anyag	$\mu_m$ (cm <sup>2</sup> /g)
ólom ( <sup>24</sup> Na, $\gamma$ sugárzás)	0,05

## TESTSZÖVETI SÚLYTÉNYEZŐK ( $W_T$ )

szövetek	$W_T$
vörös csontvelő	0,12
vastagbél	0,12
tüdő	0,12
gyomor	0,12
emlő	0,12
gonádok	0,08
húgyhólyag	0,04
máj	0,04
nyelőcső	0,04
pajzsmirigy	0,04
bőr	0,01
csontfelszín	0,01
nyálmirigyek	0,01
agy	0,01
egyéb	0,12

## VISZKOZITÁS

anyag	$\eta$ (mPa·s)
víz (20°C)	1
víz (25°C)	0,85
vér (37°C, aortában)	4,5
levegő	0,02
éter	0,23
higany	1,55
glicerin	1500

## SUGÁRZÁSI SÚLYTÉNYEZŐK ( $W_R$ )

sugárzás és energiatartomány	$W_R$
Fotonok	1
Elektronok	1
Neutronok	5-20
Protonok, $E_p > 2$ MeV	5
$\alpha$ részecskék, nehéz magok	20

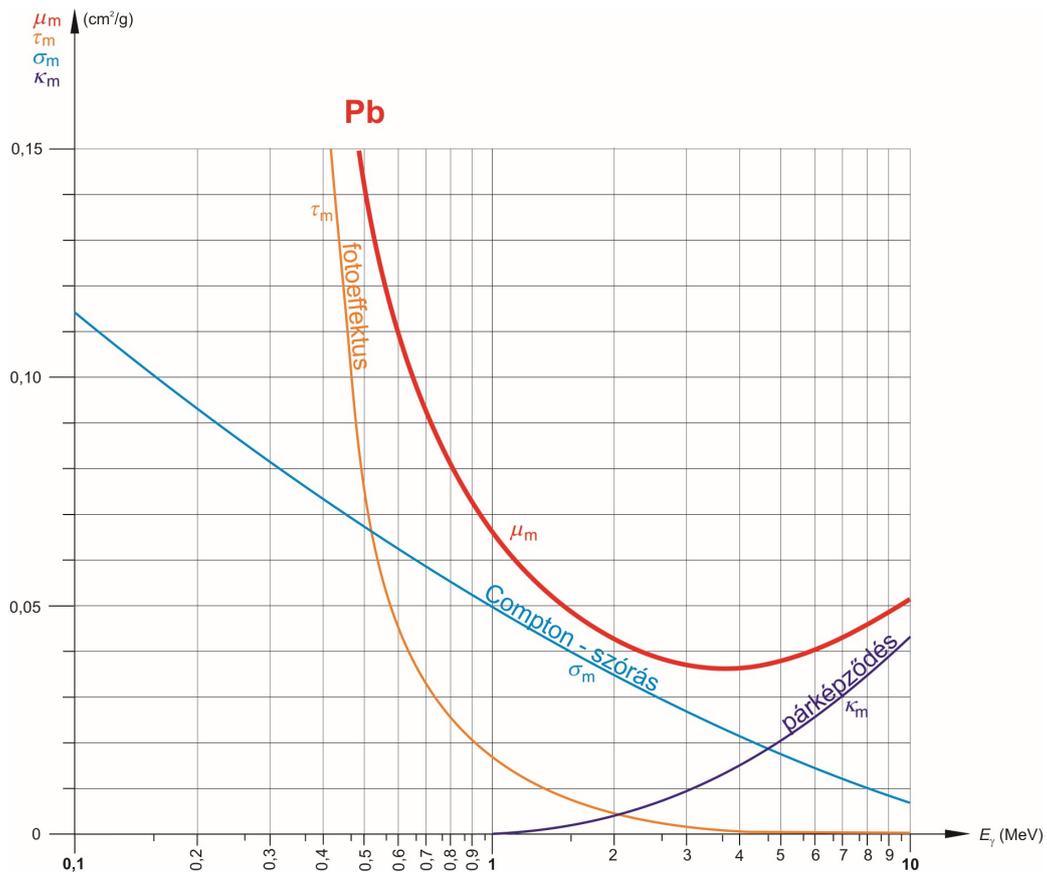
## OZMOTIKUS EGYÜTTHATÓ

anyag	$\varphi$
NaCl	0,92
CaCl <sub>2</sub>	0,85
glükóz	1,00
KCl	0,92
Na-laktát	0,98

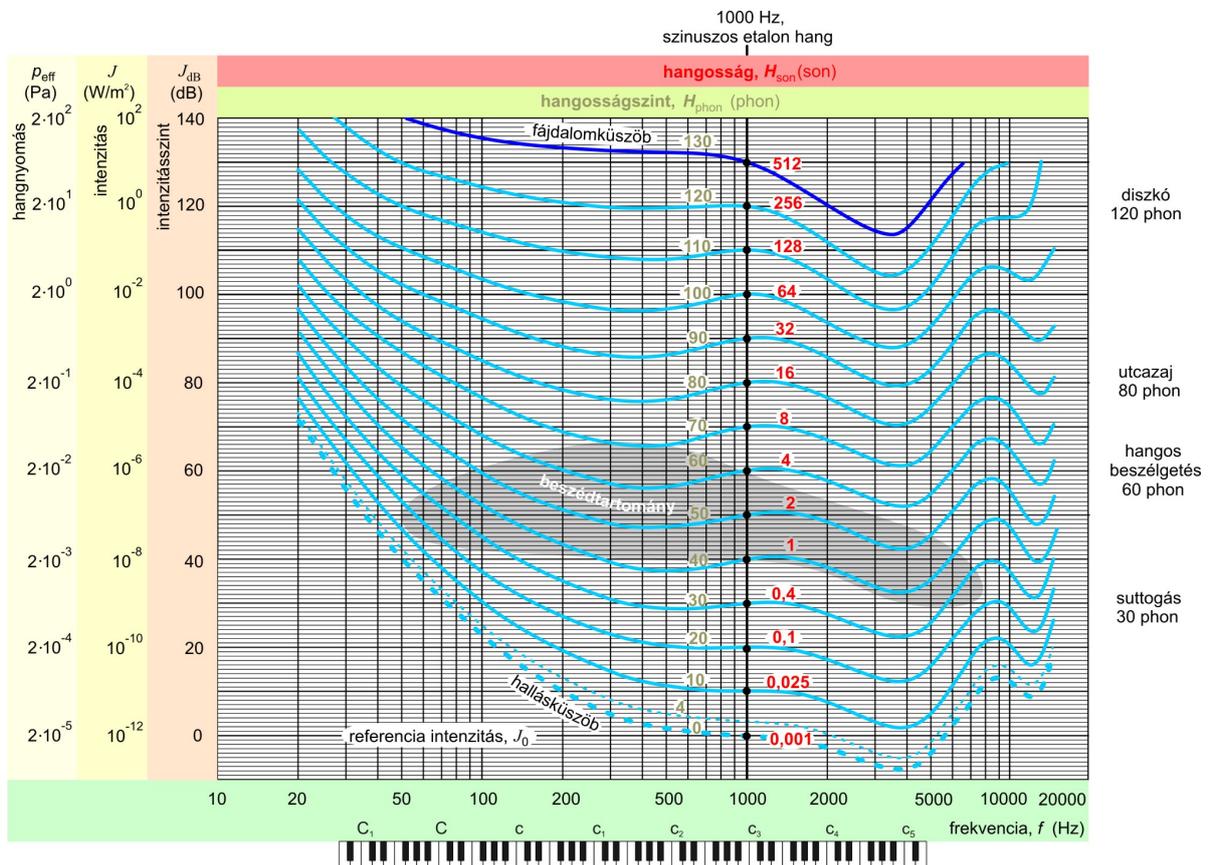
## A FONTOSABB RADIOAKTÍV IZOTÓPOK JELLEMZŐ ADATAI

kémiai elem és rendszáma		izotóp	felezési idő	bomlás módja	maximális részecske energiák (MeV)	$\gamma$ -energia (MeV)	$K\gamma$ dózis-konstans $\left( \frac{\mu\text{Gy}_{\text{lev}} \cdot \text{m}^2}{\text{GBq} \cdot \text{h}} \right)$
hidrogén	1	$^3\text{H}$	12,33 év	$\beta^-$	0,0186	–	
szén	6	$^{11}\text{C}$	20,4 perc	$\beta^+$	0,96	–	
		$^{14}\text{C}$	5760 év	$\beta^-$	0,155		
nitrogén	7	$^{13}\text{N}$	10 perc	$\beta^+$	1,19	–	
oxigén	8	$^{15}\text{O}$	2 perc	$\beta^+$	1,73	–	
fluor	9	$^{18}\text{F}$	109,8 perc	$\beta^+$	0,633	–	
nátrium	11	$^{24}\text{Na}$	15,02 óra	$\beta^-, \gamma$	1,392	2,754 1,369	444
foszfor	15	$^{32}\text{P}$	14,28 nap	$\beta^-$	1,710	–	
kén	16	$^{35}\text{S}$	87,2 nap	$\beta^-$	0,167	–	
kálium	19	$^{40}\text{K}$	$1,28 \cdot 10^9$ év	$\beta^-, \text{K} (10\%)$	1,31	1,46 K után	
		$^{42}\text{K}$	12,36 óra	$\beta^-, \gamma$	3,52 (75%) 1,99 (25%)	1,525	
kalcium	20	$^{45}\text{Ca}$	163 nap	$\beta^-$	0,257	–	
króm	24	$^{51}\text{Cr}$	27,7 nap	$\text{K}, e^-, \gamma$	0,315 ( $e^-$ )	0,320	
vas	26	$^{52}\text{Fe}$	8,2 óra	$\beta^+, \gamma$	0,8	0,5	160
		$^{59}\text{Fe}$	44,6 nap	$\beta^-, \gamma$	1,566	1,30 1,10	
kobalt	27	$^{60}\text{Co}$	5,272 év	$\beta^-, \gamma$	0,318	1,33 1,17	305
réz	29	$^{64}\text{Cu}$	12,74 óra	$\beta^- (39\%)$ $\beta^+ (19\%)$ $\text{K} (42\%)$ $\gamma (1\%)$	0,575 0,656	1,34	
kripton	36	$^{85}\text{Kr}$	10,73 év	$\beta^-, \gamma$	0,687	0,514	
rubídium	37	$^{81}\text{Rb}$	4,7 óra	$\beta^+, \gamma$	0,99	1,93 0,95	
		$^{86}\text{Rb}$	18,65 nap	$\beta^-, \gamma$	1,78	1,078	
stroncium	38	$^{90}\text{Sr}$	29 év	$\beta^-$	0,546	–	
ittrium	39	$^{90}\text{Y}$	64 óra	$\beta^-, \gamma (0,4\%)$	2,29	1,761	
technécium	43	$^{99}\text{Tc}^m$	6,02 óra	$\gamma$	–	0,140	
indium	49	$^{113}\text{In}^m$	1,658 óra	$\gamma$	–	0,391	
jód	53	$^{123}\text{I}$	13,3 óra	$\text{K}, \gamma$	–	0,16	54
		$^{125}\text{I}$	59,7 nap	$\text{K}, \gamma$	–	0,0355	
		$^{131}\text{I}$	8,04 nap	$\beta^-, \gamma$	0,606	0,364	
					0,25	0,080	
xenon	54	$^{133}\text{Xe}$	5,29 nap	$\beta^-, \gamma$	0,81	0,723	
					0,346	0,081	
cézium	55	$^{137}\text{Cs}$	30,1 év	$\beta^-, \gamma$	0,512 (92,6%) 1,173 (7,4%)	0,661	80
arany	79	$^{198}\text{Au}$	2,695 nap	$\beta^-, \gamma$	0,961	0,411	
higany	80	$^{203}\text{Hg}$	46,6 nap	$\beta^-, \gamma$	0,212	0,279	
radon	86	$^{222}\text{Rn}$	3,824 nap	$\alpha$	5,489	–	
rádiórium	88	$^{226}\text{Ra}$	1600 év	$\alpha, \gamma (6\%)$	4,784	0,186 0,260	
					4,598	0,609	
urán	92	$^{238}\text{U}$	$4,47 \cdot 10^9$ év	$\alpha, \gamma$	4,2	0,048	

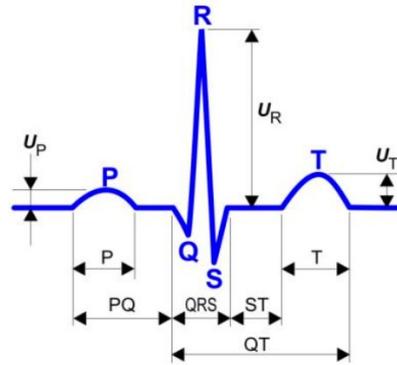
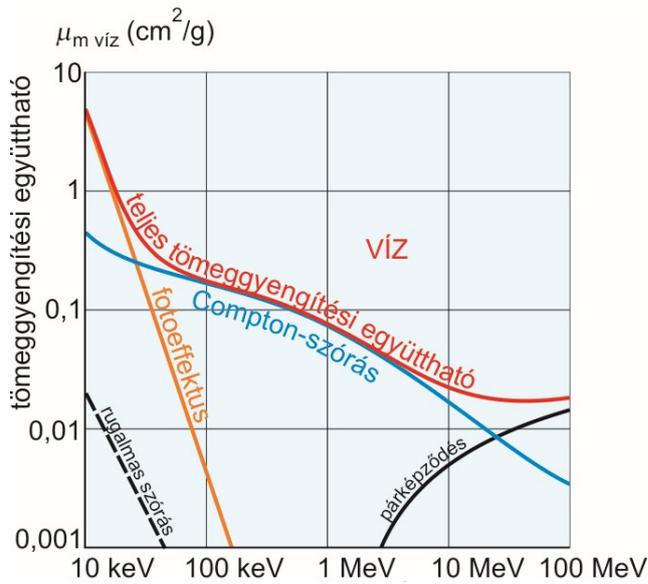
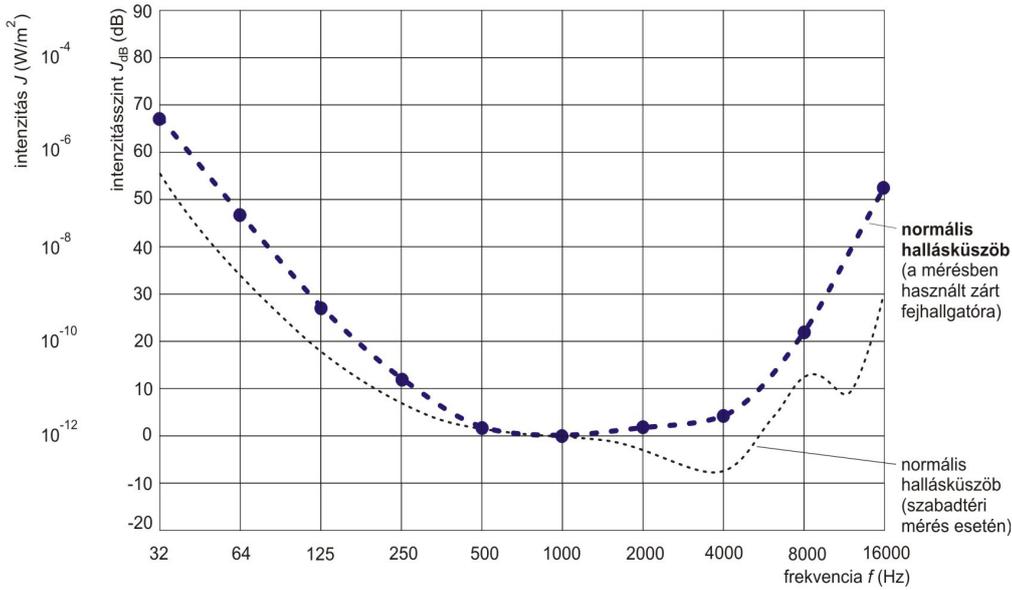
## AZ ÓLOM TÖMEGNYENGTÉSI EGYÜTTHATÓJÁNAK ÖSSZETEVŐI



## EGYENLŐ HANGOSSÁGSZINTŰ GÖRBÉK



Megújított gyakorlatokhoz kapcsolódó képletek, adatok  
**NORMÁLIS HALLÁSKÜSZÖBGÖRBE**  
 (a mérésben használt zárt fejhallgatóra - - - )  $J_{dB \text{ norm}}$



I.	II.	III.	IV.	V.
Szabályozott üreg	Érzékelt üreg	Érzékelésre adott válasz	Ritmus moduláció	Többhelyes ritmus-szabályozás
0 = Nincs	0 = Nincs	0 = Nincs	0 = Nincs	0 = Nincs
A = Pitvar	A = Pitvar	I = Nincs inger	R = Ritmus moduláció	A = Pitvar
V = Kamra	V = Kamra	T = Inger		V = Kamra
D = Duális (A+V)	D = Duális (A+V)	D = Duális (I+T)		D = Duális (A+V)

# STATISZTIKA

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{\sum_{i=1}^n x_i}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\bar{x} = \frac{\sum_{i=1}^n n_i x_i}{n}$$

$$s_{x,n-1} = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{Q_{xx}}{n-1}}$$

$$s_{\bar{x}} = \frac{S_x}{\sqrt{n}}$$

$$z = \frac{x - \mu}{\sigma}$$

$$\bar{x} \pm t_{\%} s_{\bar{x}}$$

$$\bar{x} \pm t_{\%} s_x$$

$$t_{[n-1]} = \frac{\bar{x}}{s_{\bar{x}}}$$

$$t_{[n-1]} = \frac{\bar{x} - \mu_0}{s_{\bar{x}}}$$

$$t_{[n_1+n_2-2]} = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{Q_1 + Q_2}{n_1 + n_2 - 2}}} \sqrt{\frac{n_1 n_2}{n_1 + n_2}}$$

$$Q_1 = \sum_{i=1}^{n_1} (x_{1i} - \bar{x}_1)^2 \quad \text{és} \quad Q_2 = \sum_{i=1}^{n_2} (x_{2i} - \bar{x}_2)^2$$

$$F_{[n_1-1; n_2-1]} = \frac{S_{\text{nagyobb}}^2}{S_{\text{kisebb}}^2}$$

$$s_g^2 = \frac{\sum_{j=1}^h n_j (\bar{x}_j - \bar{\bar{x}})^2}{h-1} = \frac{Q_g}{h-1}$$

$$s_i^2 = \frac{\sum_{j=1}^h Q_j}{N-h} = \frac{\sum_{j=1}^h \sum_{i=1}^{n_j} (x_{ij} - \bar{x}_j)^2}{N-h} = \frac{Q_i}{N-h}$$

$$t_{[n-1]} = \frac{\bar{R}}{\frac{s}{\sqrt{n}}}$$

$$Q(a, b) = \sum_{i=1}^n [y_i - (ax_i + b)]^2$$

$$a^* = \frac{Q_{xy}}{Q_{xx}} = \frac{s_{xy}^2}{s_x^2}$$

$$Q_{xy} = \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

$$Q_{xx} = \sum_{i=1}^n (x_i - \bar{x})^2$$

$$s_{xy}^2 = \frac{Q_{xy}}{n-1}$$

$$b^* = \bar{y} - a^* \bar{x}$$

$$r = \frac{Q_{xy}}{\sqrt{Q_{xx}Q_{yy}}} = \frac{s_{xy}^2}{s_x s_y}$$

$$t_{[n-2]} = r \sqrt{\frac{n-2}{1-r^2}}$$

$$\chi^2 = \sum_i \frac{(O_i - E_i)^2}{E_i}$$

$$\chi_{[1]}^2 = \frac{n(ad - bc)^2}{(a+b)(c+d)(a+c)(b+d)}$$

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$$\log(a \cdot b) = \log a + \log b$$

$$\log\left(\frac{a}{b}\right) = \log a - \log b$$

$$\log a^b = b \cdot \log a$$

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$$H = p \log_2\left(\frac{1}{p}\right)$$

$$I = \log_2\left(\frac{1}{p}\right)$$

$$p(A) = \frac{k}{n}$$

$$p(A \text{ vagy } B) = p(A) + p(B) - p(A \text{ és } B)$$

$$p(A|B) = \frac{p(A \text{ és } B)}{p(B)}$$

$$\text{odds} = \frac{p}{1-p} = \frac{p}{q}$$

$$p = \frac{\text{odds}}{1 + \text{odds}}$$

$$\text{logit}(A) = \ln(\text{odds}(A))$$

$$\text{logit}(\text{nem } A) = -\text{logit}(A)$$

$$\text{odds}(A) = e^{\text{logit}(A)}$$

$$\text{odds}(\text{nem } A) = \frac{1}{\text{odds}(A)}$$

$$\text{RR} = \frac{p(B_+|R_+)}{p(B_+|R_-)} = \frac{\frac{a}{a+b}}{\frac{c}{c+d}} = \frac{a(c+d)}{c(a+b)}$$

$$\text{OR} = \frac{\frac{p(B_+|R_+)}{p(B_-|R_+)}}{\frac{p(B_+|R_-)}{p(B_-|R_-)}} = \frac{ad}{bc}$$

$$\mu = E(\xi) = \sum_i x_i p_i$$

$$\sigma^2 = D^2(\xi) = E[(\xi - E(\xi))^2] = \sum_i (x_i - \mu)^2 \cdot p(x_i)$$

$$\eta = \xi + k \rightarrow E(\eta) = E(\xi) + k; \text{Var}(\eta) = \text{Var}(\xi)$$

$$\eta = \xi \cdot k \rightarrow E(\eta) = E(\xi) \cdot k; \text{Var}(\eta) = \text{Var}(\xi) \cdot k^2$$

$$\eta = \xi_{\text{norm}} \cdot \omega_{\text{norm}} \rightarrow E(\eta) = E(\xi) \cdot E(\omega)$$

$$\eta = \xi + \omega \rightarrow E(\eta) = E(\xi) + E(\omega); \text{Var}(\eta) = \text{Var}(\xi) + \text{Var}(\omega)$$

, ha függetlenek

$$\eta_{E=0; \text{Var}=1} = (\xi - E(\xi)) * \frac{1}{\sqrt{\text{Var}(\xi)}} = \frac{(\xi - E(\xi))}{\sqrt{\text{Var}(\xi)}}$$

$$p(x_i) = \frac{1}{n} \quad \mu = \frac{n+1}{2} \quad \sigma^2 = \frac{n^2-1}{12}$$

$$f(x) = \begin{cases} \frac{1}{b-a}, & \text{ha } a \leq x \leq b \\ 0, & \text{egyébként} \end{cases}$$

$$\mu = \frac{a+b}{2} \quad \sigma^2 = \frac{(b-a)^2}{12}$$

$$p_k = \binom{n}{k} p^k (1-p)^{n-k}$$

$$\mu = np \quad \sigma^2 = np(1-p)$$

$$p_k = \frac{\lambda^k}{k!} e^{-\lambda} \quad \mu = \lambda \quad \sigma^2 = \lambda$$

$$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} = N(\mu, \sigma)$$

$$\sum \frac{(x_i)^k}{n}$$

$$\sum \frac{(x_i - \mu)^k}{n}$$

$$w = \frac{\text{beteg}}{\text{összes}} = \frac{ÁN + VP}{VN + ÁP + ÁN + VP}$$

$$se = \frac{VP}{\text{beteg}} = \frac{VP}{ÁN + VP}$$

$$sp = \frac{VN}{\text{egészséges}} = \frac{VN}{VN + ÁP}$$

$$1 - se = \frac{ÁN}{\text{beteg}} = \frac{ÁN}{ÁN + VP}$$

$$1 - sp = \frac{ÁP}{\text{egészséges}} = \frac{ÁP}{VN + ÁP}$$

$$PPV = \frac{VP}{\text{összes pozitív}} = \frac{VP}{ÁP + VP}$$

$$NPV = \frac{VN}{\text{összes negatív}} = \frac{VN}{ÁN + VN}$$

$$1 - PPV = \frac{ÁP}{\text{összes pozitív}} = \frac{ÁP}{ÁP + VP}$$

$$1 - NPV = \frac{ÁN}{\text{összes negatív}} = \frac{ÁN}{ÁN + VN}$$

$$de = \frac{VP + VN}{\text{összes}} = \frac{VP + VN}{VP + ÁN + VN + ÁP}$$

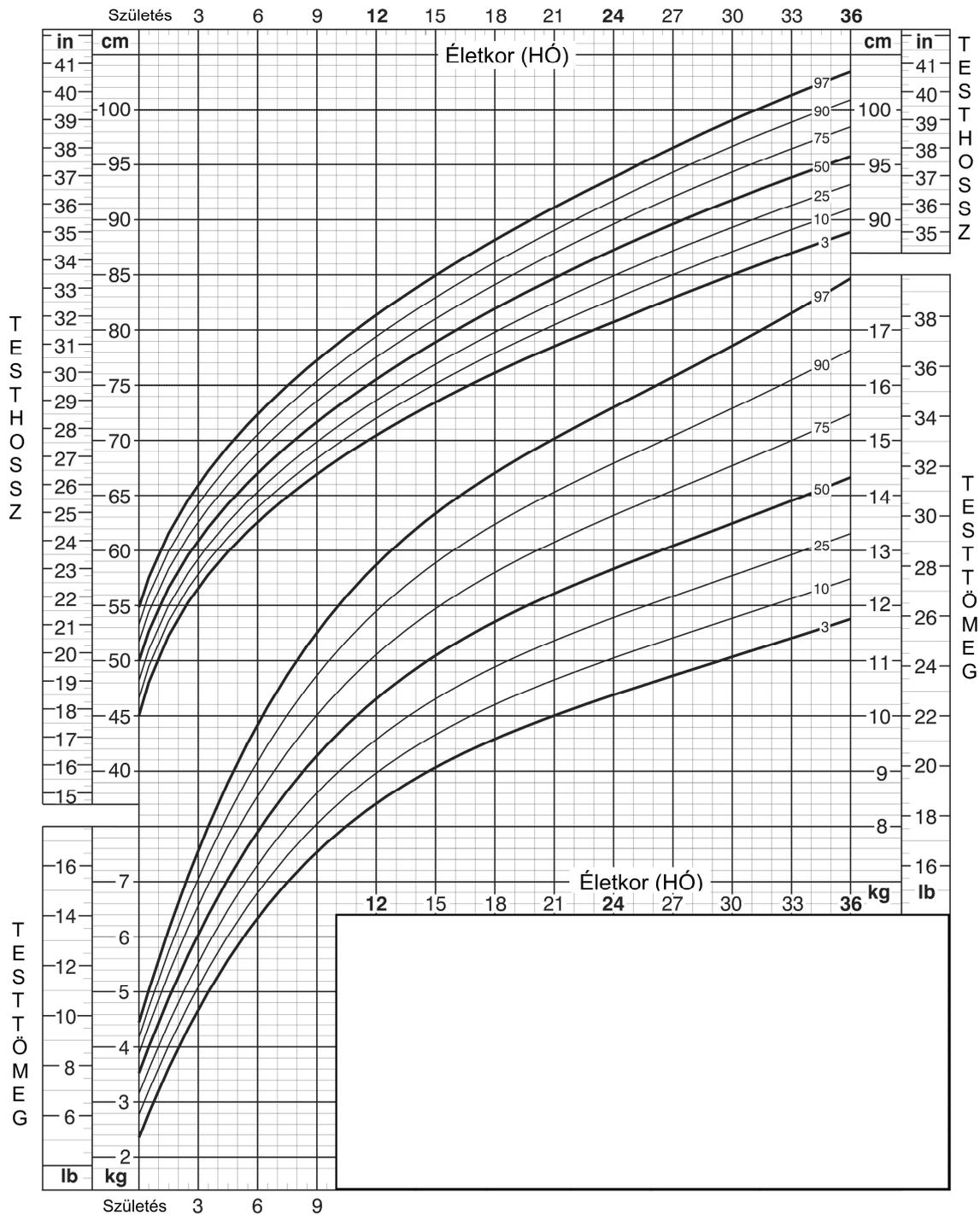
## T-ELOSZLÁS

szabadságfok	$p$ (valószínűség, kétszélű)							
	0,5	0,2	0,1	0,05	0,02	0,01	0,002	0,001
1	1,00	3,08	6,31	12,7	31,8	63,7	318,3	636,6
2	0,82	1,89	2,92	4,30	6,96	9,92	22,3	31,6
3	0,76	1,64	2,35	3,18	4,54	5,84	10,2	12,9
4	0,74	1,53	2,13	2,78	3,75	4,60	7,17	8,61
5	0,73	1,48	2,02	2,57	3,37	4,03	5,89	6,87
6	0,72	1,44	1,94	2,45	3,14	3,71	5,21	5,96
7	0,71	1,41	1,89	2,36	3,00	3,50	4,79	5,41
8	0,71	1,40	1,86	2,31	2,90	3,36	4,50	5,04
9	0,70	1,38	1,83	2,26	2,82	3,25	4,30	4,78
10	0,70	1,37	1,81	2,23	2,76	3,17	4,14	4,59
11	0,70	1,36	1,80	2,20	2,72	3,11	4,02	4,44
12	0,70	1,36	1,78	2,18	2,68	3,05	3,93	4,32
13	0,69	1,35	1,77	2,16	2,65	3,01	3,85	4,22
14	0,69	1,35	1,76	2,14	2,62	2,98	3,79	4,14
15	0,69	1,34	1,75	2,13	2,60	2,95	3,73	4,07
16	0,69	1,34	1,75	2,12	2,58	2,92	3,69	4,01
17	0,69	1,33	1,74	2,11	2,57	2,90	3,65	3,97
18	0,69	1,33	1,73	2,10	2,55	2,88	3,61	3,92
19	0,69	1,33	1,73	2,09	2,54	2,86	3,58	3,88
20	0,69	1,33	1,72	2,09	2,53	2,85	3,55	3,85
21	0,69	1,32	1,72	2,08	2,52	2,83	3,53	3,82
22	0,69	1,32	1,72	2,07	2,51	2,82	3,51	3,79
23	0,69	1,32	1,71	2,07	2,50	2,81	3,49	3,77
24	0,68	1,32	1,71	2,06	2,49	2,80	3,47	3,75
25	0,68	1,32	1,71	2,06	2,49	2,79	3,45	3,73
30	0,68	1,31	1,70	2,04	2,46	2,75	3,39	3,65
40	0,68	1,30	1,68	2,02	2,42	2,70	3,31	3,55
60	0,68	1,30	1,67	2,00	2,39	2,66	3,23	3,46
120	0,68	1,30	1,66	1,98	2,36	2,62	3,16	3,37
$\infty$	0,68	1,29	1,64	1,96	2,33	2,58	3,09	3,29

## $\chi^2$ (KHI-NÉGYZET)-ELOSZLÁS

szabadságfok	$p$ (valószínűség, jobbszélű)						
	0,99	0,975	0,95	0,05	0,025	0,01	0,001
1	0,0000157	0,0000982	0,000393	3,84	5,02	6,63	10,83

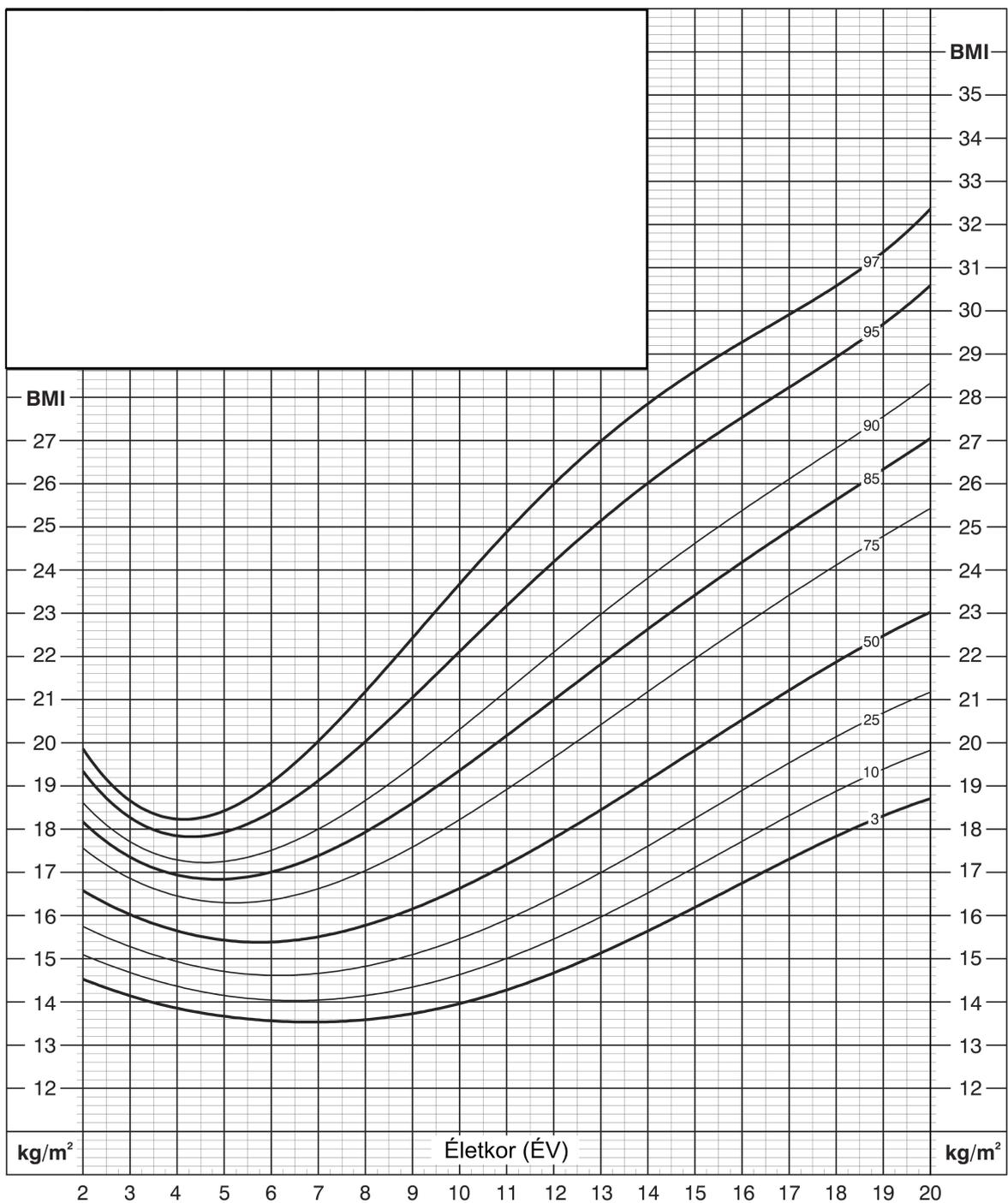
# TESTHOSSZ- ÉS TESTTÖMEG – ÉLETKOR PERCENTILISEK; FIÚK



Published May 30, 2000 (modified 4/20/01).  
 SOURCE: Developed by the National Center for Health Statistics in collaboration with  
 the National Center for Chronic Disease Prevention and Health Promotion (2000).  
<http://www.cdc.gov/growthcharts>



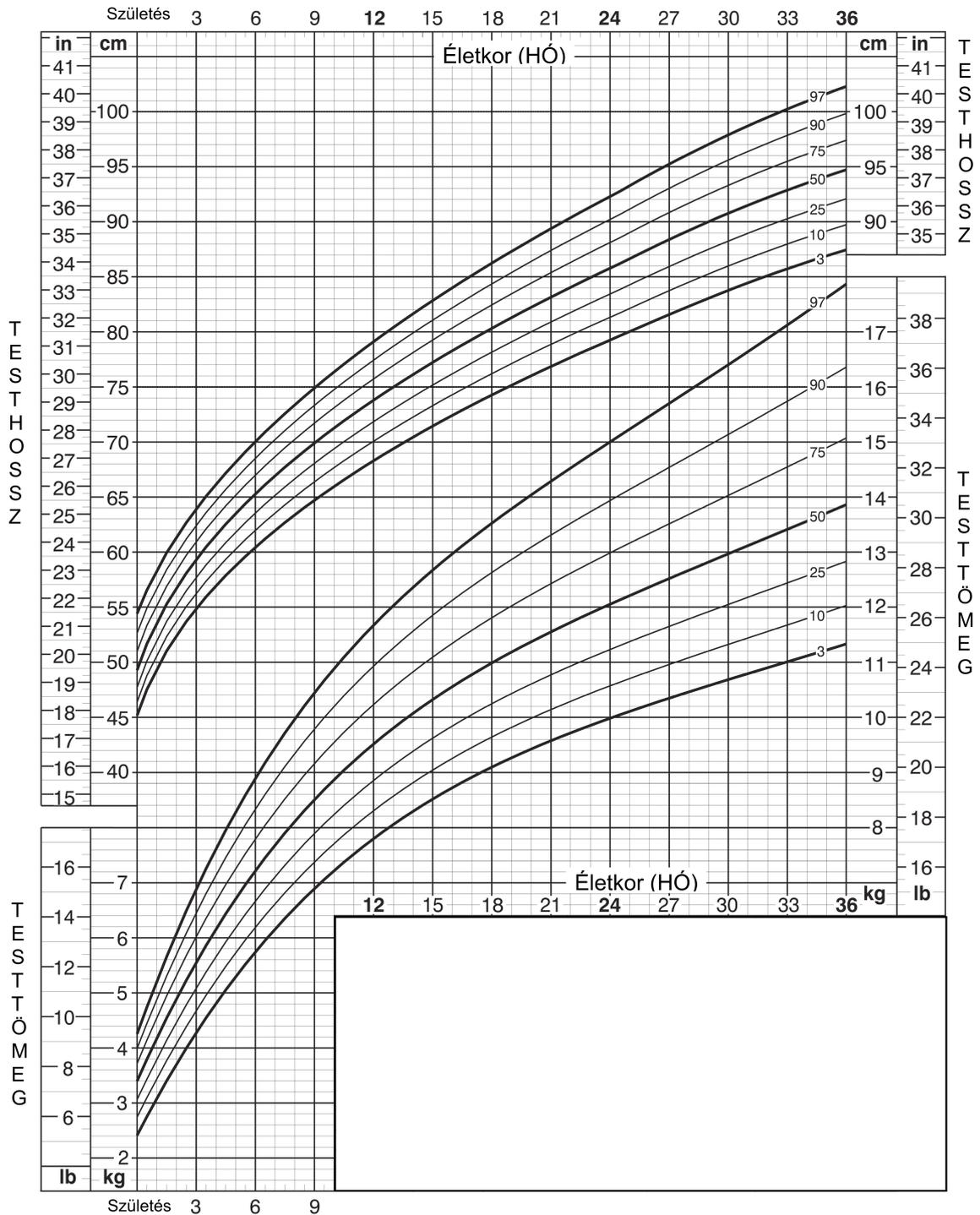
## BMI – ÉLETKOR PERCENTILISEK; FIÚK



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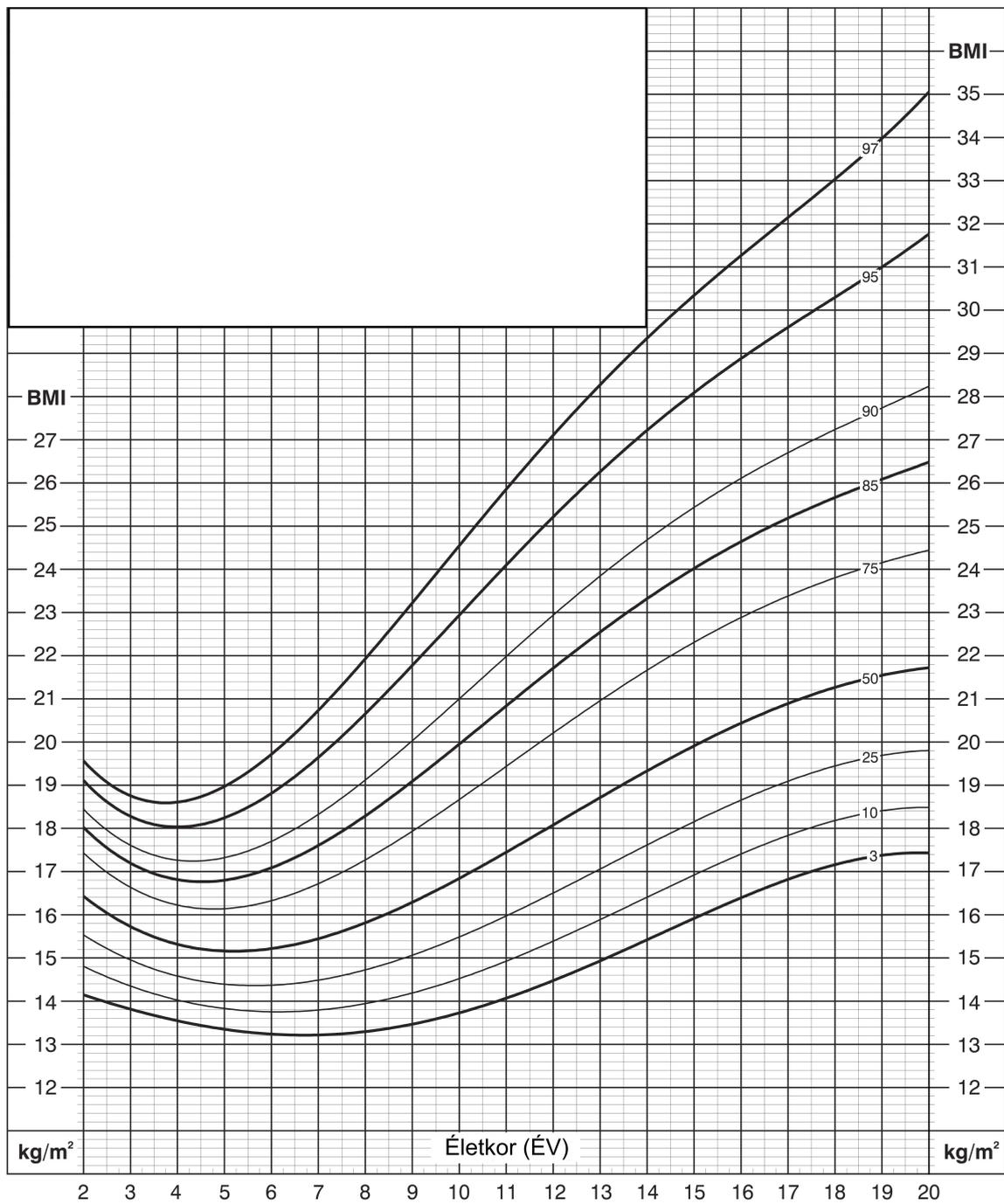
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