

Biophysics

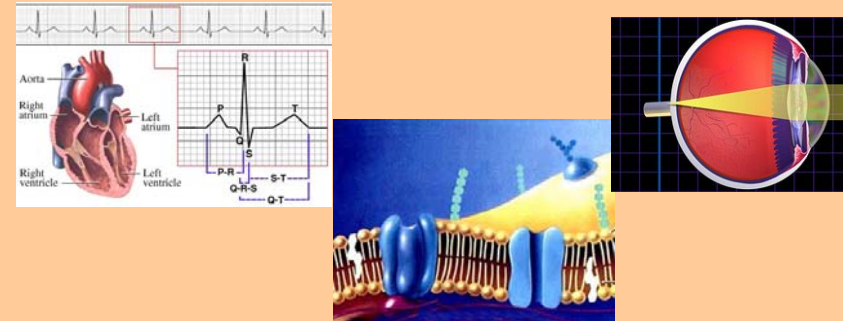
Gabriella Csik

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What is the subject of biophysics?

Physical aspects/background of biological processes

E.g., Electrophysiology of heart, structure and functioning of membranes, sensory function stb.



What is the subject of biophysics?

Physical methods in biology and medicine

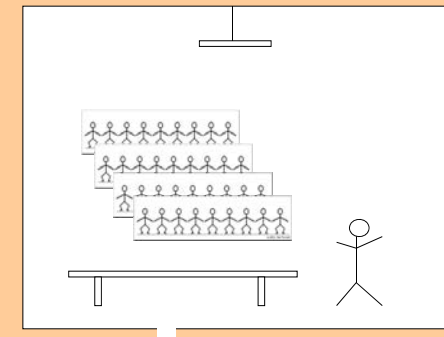
E.g., ECG, X-ray diagnostics, microscopy....



Radiation

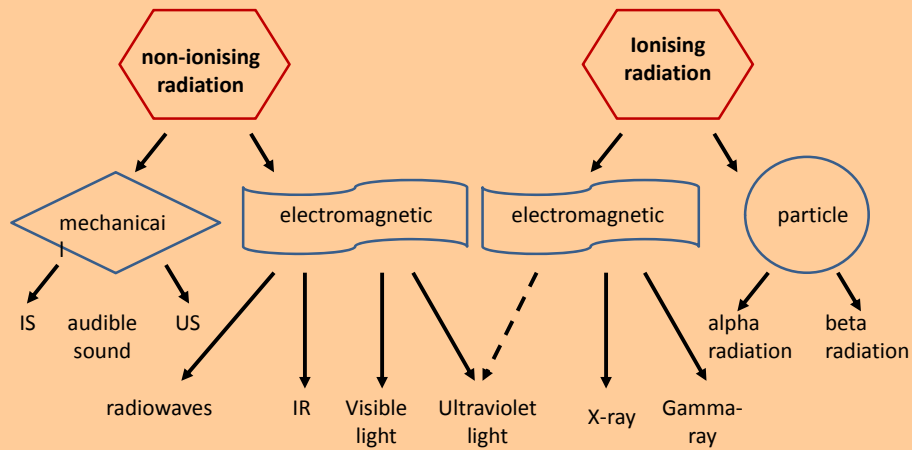
Examples around us

sound
light
radiowaves
nuclear radiation



Radiation: emission and propagation of energy

Radiation



Nature of light

Wave?



Christiaan Huygens

(1629 - 1695)

Traité de la lumière
1690

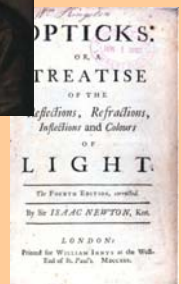
Particle?



Isaac Newton

(1642 - 1727)

Opticks
1704



Natur of waves

periodic disturbance in space and time, possibly transferring energy to or through a spacetime region.



Waves differ in
type of energy
amplitude
mechanism of propagation

Characteristic values

Period in space— *wavelength*

λ [m] or [nm]

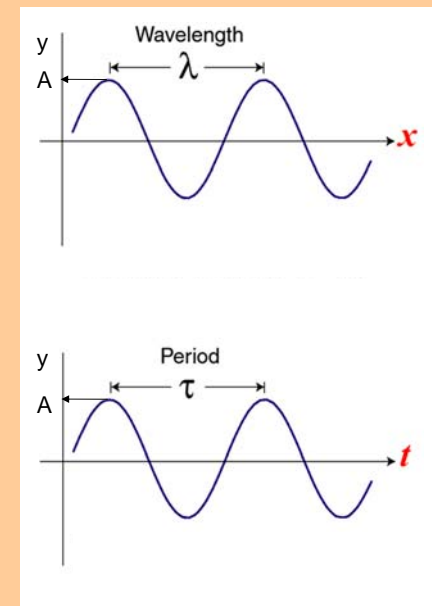
Highest displacement — *amplitude*

$$E \sim A^2$$

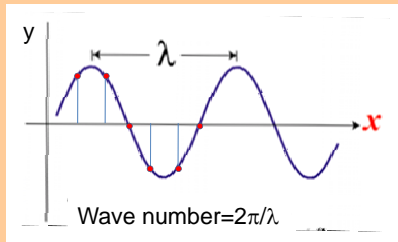
Period in time

— *period*
— *frequency*

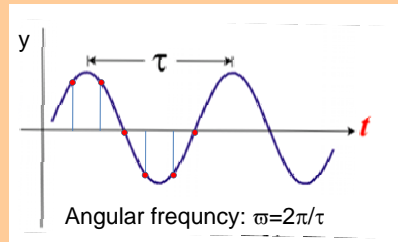
$$f = \frac{1}{\tau} \left[\frac{1}{s} \right]$$



Phase: the initial angle of a sinusoidal function at its origin



$$\phi(x) = kx + \phi_0$$



$$\phi(t) = \omega t + \phi_0$$

$$\phi = \omega t + kx + \phi_0$$

Nature of light

Wave?



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(1629 - 1695)

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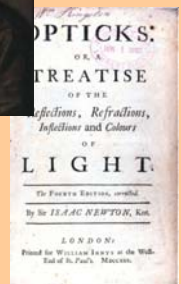
Particle?



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Opticks
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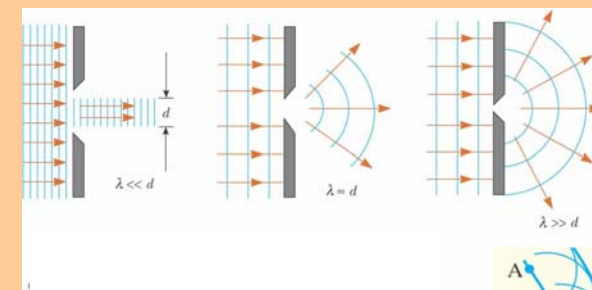


Indication of wave nature

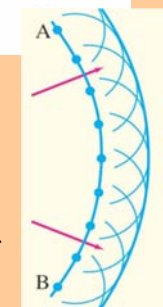
- diffraction
- superposition/interference
- polarization



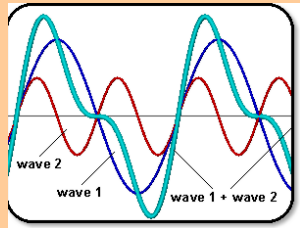
Diffraction



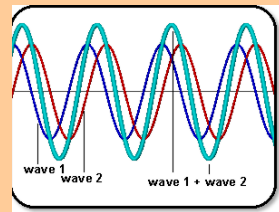
Huygens-principle: every point on a propagating wavefront serves as the source of spherical secondary wavelets, such that the wavefront at some later time is the envelope of these wavelets.



Superposition: The principle of superposition may be applied to waves whenever two (or more) waves travelling through the same medium at the same time. The net displacement of the medium at any point in space or time, is simply the sum of the individual wave displacements.

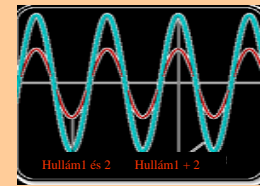


Un-equal frequencies



Equal frequencies

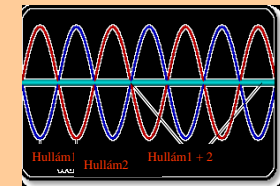
Interference: superposition of coherent waves



Similar phase

Constructive interference

$$\Phi = 0^\circ$$



Opposite waves

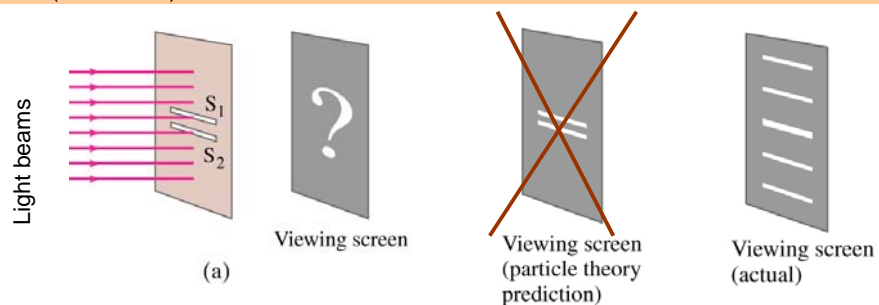
Destructive interference

$$\Phi = 180^\circ$$



Thomas Young
(1773-1829)

Thomas Young's
double-slit experiment

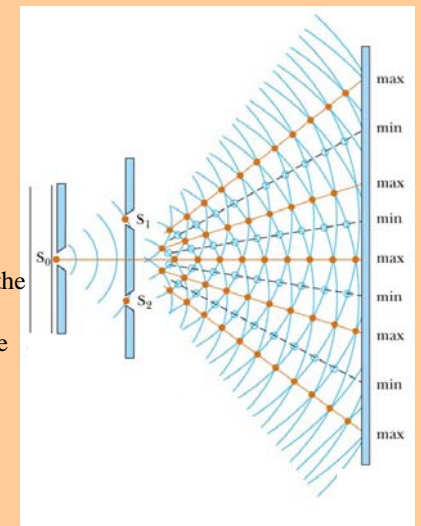


*Interpretation of Thomas Young's
double-slit experiment*

S₁ and S₂ slits are wave sources

Two waves from S₁ and S₂ originates from the same wave front that is they are in the same phase.

↓
↓
interference

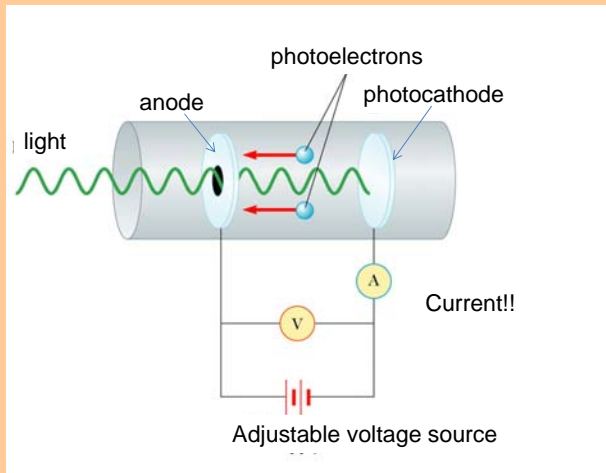


Interference fringes on a screen

Photoelectric effect



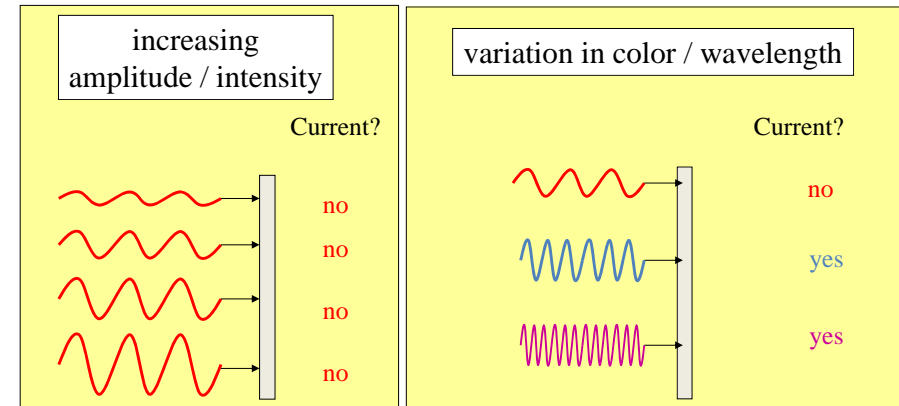
Heinrich Hertz
1887



Light irradiation

Similar color / wavelength

Similar amplitude



No current up to a critical value of frequency

Interpretation of photoelectric effect

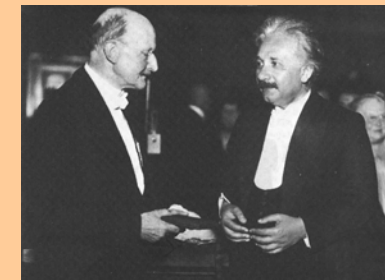
- Based on the wave character it is not possible.

- Planck – foundation of quantum physics

$$E = hf$$

- Einstein's concept is based on the quantum theory

Max Planck



Albert Einstein

Nobel Prize in physics 1918

*"in recognition of the services he rendered to the advancement of Physics by his **discovery of energy quanta**".*

Nobel Prize in physics 1921

*for his services to Theoretical Physics, and especially for his **discovery of the law of the photoelectric effect**".*

Einstein interpretation

- Light consists of a finite number of energy quanta - photons
- The energy of photon: $E = hf$
- Photon can be absorbed or generated only as complete units.
- A photon transfer its energy to one electron if the photon energy is equal or higher than the work function (A).
- No interaction, if the photon energy is smaller than the work function.
- 1 photon– 1 electron interaction
- Kinetic energy of the electron: $E_{kin} = hf - A$

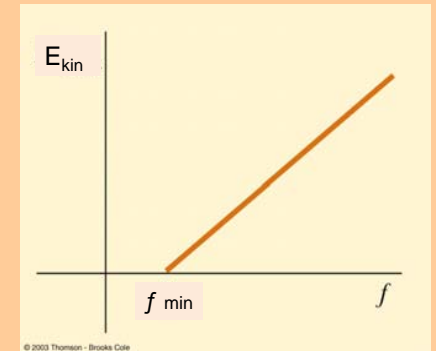
Einstein interpretation and the frequency limit

Kinetic energy of electron proportional to the frequency.

Intercept with the x axis is the smallest frequency inducing photoelectric effect

f_{min} depends on the cathode material:

$$A = hf_{min}$$



Dual nature of light

Particle – its energy is quantised; a photon is an elementary particle, the quantum of the electromagnetic interaction

Energy of photon: $E = hf = h \frac{c}{\lambda}$

Planck constant: $h = 6.62 \cdot 10^{-34} \text{ Joule} \cdot \text{s}$

It has no resting mass

Propagates in vacuum

Calculation of photon energy

$$E = h \times \frac{c}{\lambda}$$

If $\lambda = 400 \text{ nm}$

$$E = 6.6 \times 10^{-34} \text{ Js} \times \frac{3 \times 10^8 \frac{\text{m}}{\text{s}}}{4 \times 10^{-7} \text{ m}} = 4.95 \times 10^{-19} \text{ J}$$

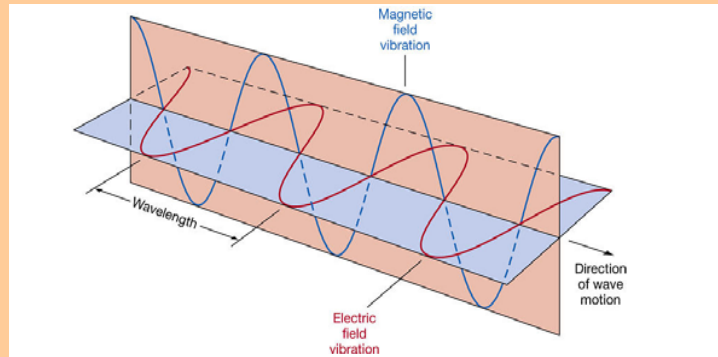
$$E = \frac{4.95 \times 10^{-19} \text{ J}}{1.6 \times 10^{-19}} = 3.1 \text{ eV}$$

$$E_{vis} = 1.6 - 3.1 \text{ eV}$$

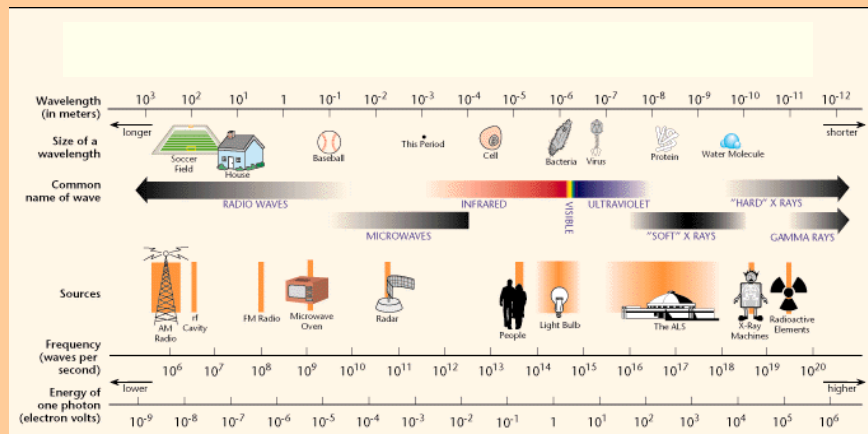
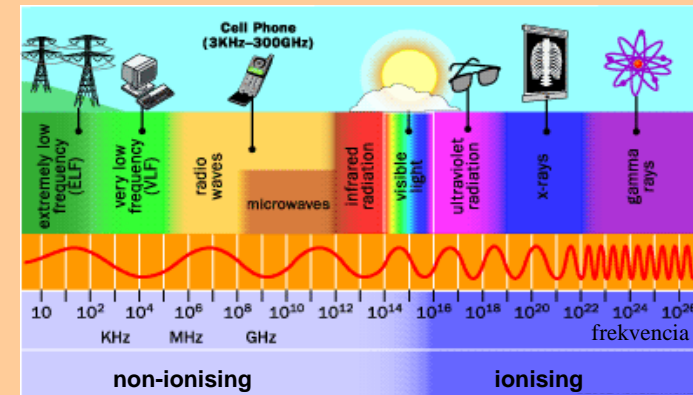
Dual nature of light

Wave – electric and magnetic fields vary sinusoidally

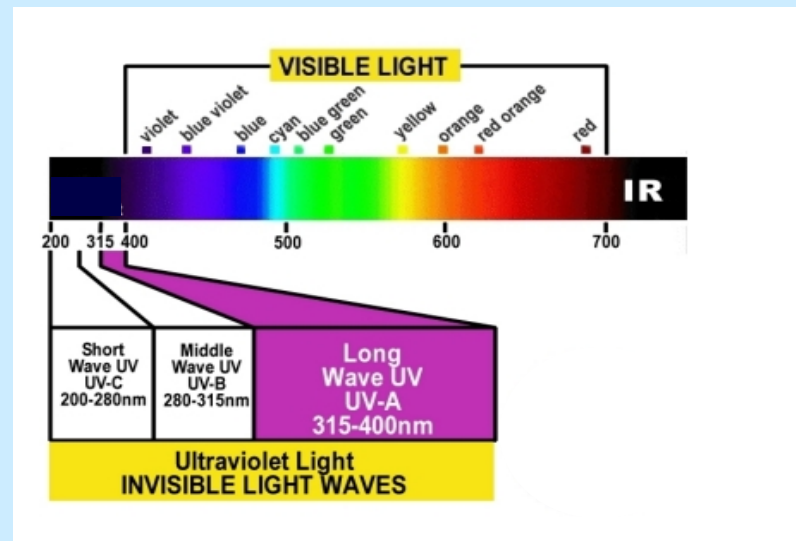
Electromagnetic radiation



Ranges of electromagnetic radiation

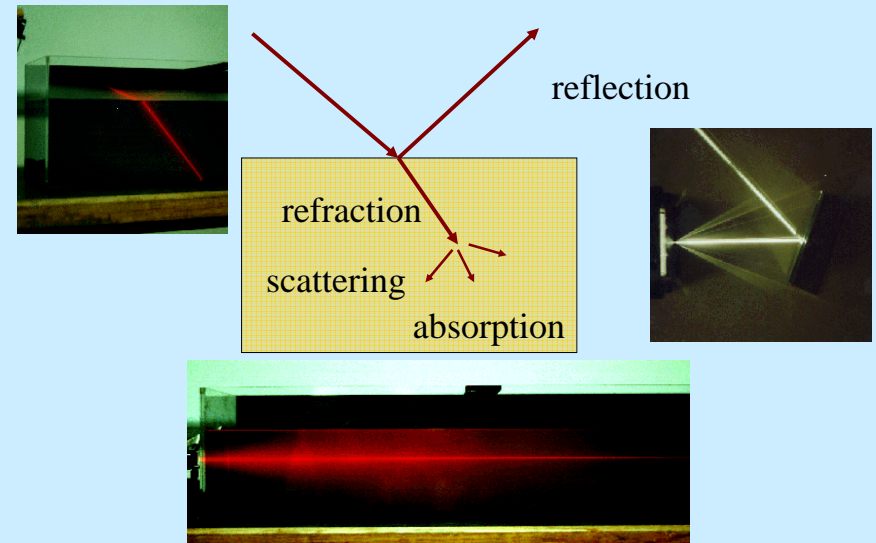


Optical range



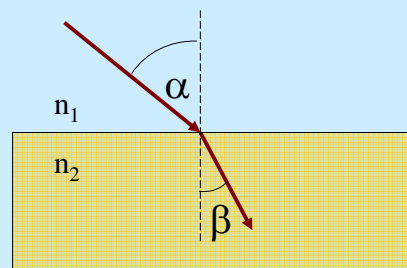
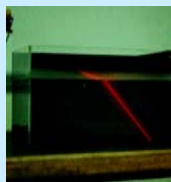
Interaction of light with matter

Interaction of light with matter



Refraction of light

Fermat's Principle: Light follows the path of least time



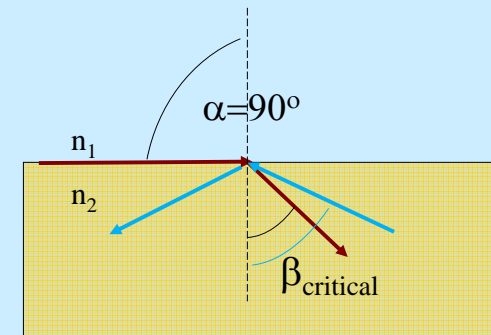
$$n_1 < n_2$$

$$\alpha > \beta$$

Snell's Law

$$\frac{\sin \alpha}{\sin \beta} = \frac{c_1}{c_2} = \frac{n_2}{n_1} = n_{21} \quad \text{The index of refraction}$$

Critical angle – total reflection



$$\beta > \beta_{\text{critical}}$$



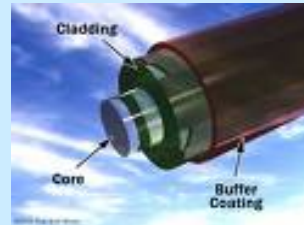
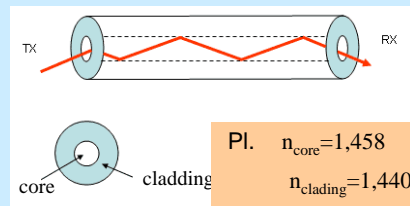
Medical application

Determination of concentration – refractometry

Concentration of solutions is proportional
with their index of refraction .



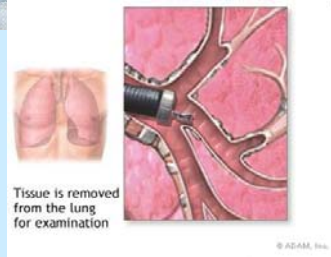
Optical fibers



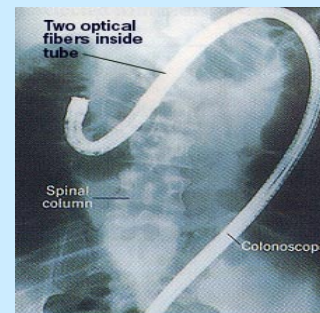
Application in dentistry



Other medical applications



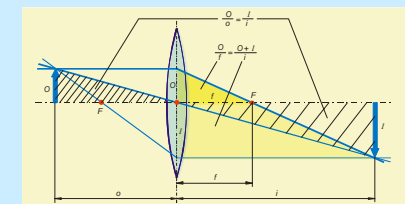
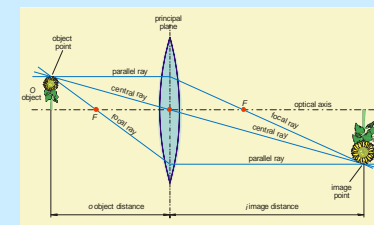
Bronchoscopy



Colonoscopy

Image formation (thin lens approximation)

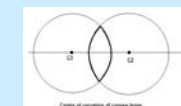
Image construction
by principal rays



lensmaker's formula.

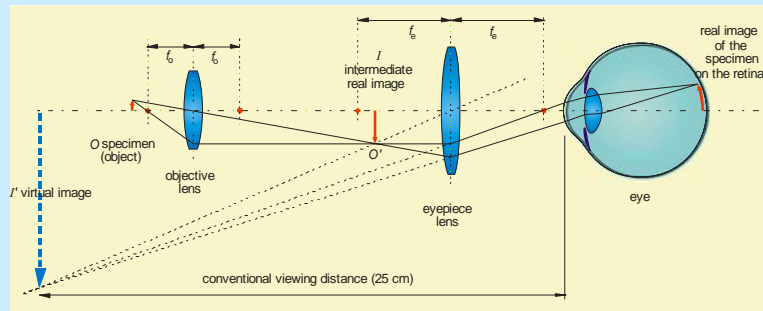
$$D = \frac{1}{f} = \frac{1}{o} + \frac{1}{i} = (n-1) \left(\frac{1}{r_1} + \frac{1}{r_2} \right)$$

the radii of curvature



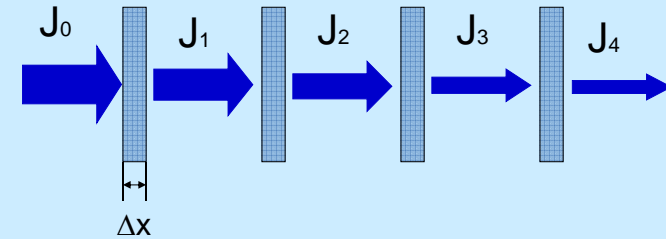
D - diopter: measure of the optical power of a lens, which is equal to the reciprocal of the focal length measured in meters

Image formation – compound microscope



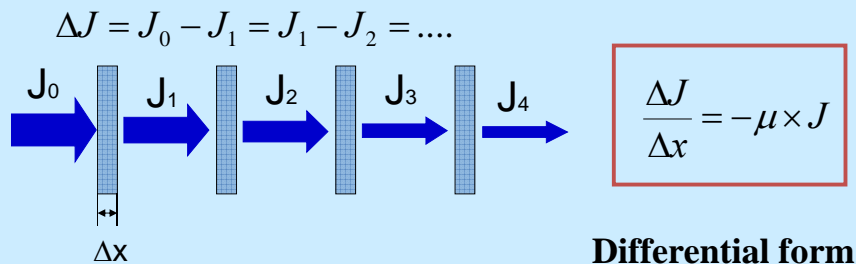
The image is magnified
reversed
virtual

Absorption



Intensity of radiation is attenuated when passing through material

Law of attenuation



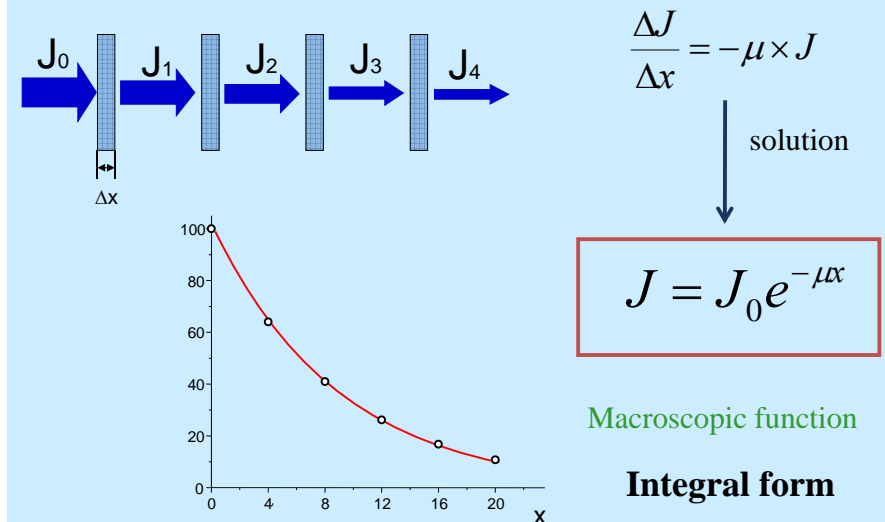
J : incident intensity [W/m^2]

ΔJ : change of intensity after passing through Δx thickness

μ : attenuation coefficient [$1/\text{m}$]

The decrease is proportional to the thickness of absorber Δx and J what is the initial intensity.

Law of attenuation



Exponential law of radiation attenuation

$$J = J_0 e^{-\mu x}$$

J is exponential function of the thickness of the layer.

J_0 : incident intensity [W/m²]

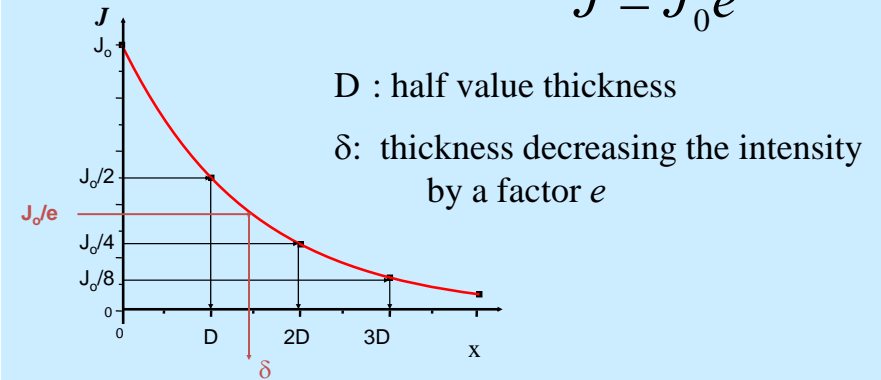
J : intensity after passing through x thickness

μ : attenuation coefficient [1/m]

Linear attenuation (absorption) coefficient depends on
 photon energy
 quality (atomic number) of absorber
 density of absorber

Graphical representation

$$J = J_0 e^{-\mu x}$$



Both D and δ depend on photon energy, quality (atomic number) of absorber, density of absorber

Definition of attenuation coefficient

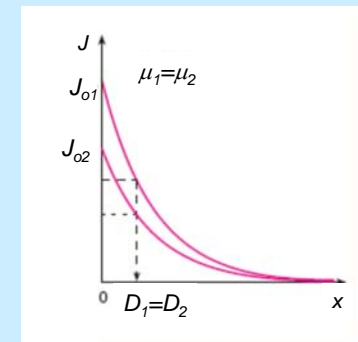
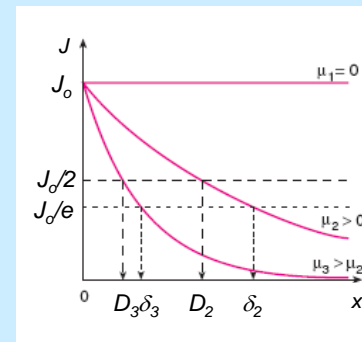
$$J = J_0 e^{-\mu x}$$

If $x = D \longrightarrow J_0 / 2 = J_0 e^{-\mu D}$

$$\mu = \frac{\ln 2}{D} = \frac{0.693}{D}$$

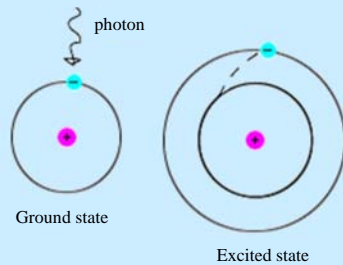
If $x = \delta \longrightarrow J_0 / e = J_0 e^{-\mu \delta}$

$$\mu = \frac{1}{\delta}$$



Mechanism of light absorption

Repetition: structure of atom



$$hf = \Delta E = E_{n+1} - E_n$$

$$E_{\text{VIS}} = 1.6 - 3.1 \text{ eV}$$

Excitation of outer shell electrons

Laboratory application of light absorption

$$J = J_0 \cdot e^{-\mu x}$$

$$\lg \frac{J_0}{J} = \mu \cdot x \cdot \lg e$$

in dilute solutions :
 $\mu \sim \text{concentration}$

$$\mu \lg e = \varepsilon_{(\lambda)} c$$

$$\lg \frac{J_0}{J} = \varepsilon_{(\lambda)} \cdot c \cdot x$$

Lambert – Beer law

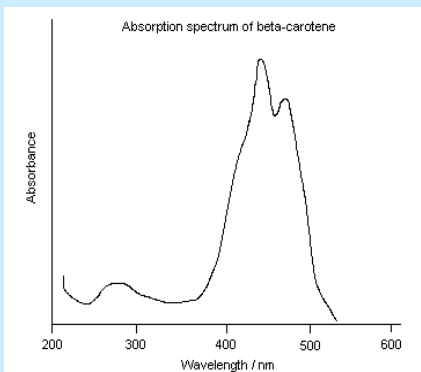
Absorbance
or
Optical density

decadic molar
extinction coefficient

molar concentration

$$\lg \frac{J_0}{J} = \varepsilon_{(\lambda)} \cdot c \cdot x$$

Absorbance – is the function of the wavelength

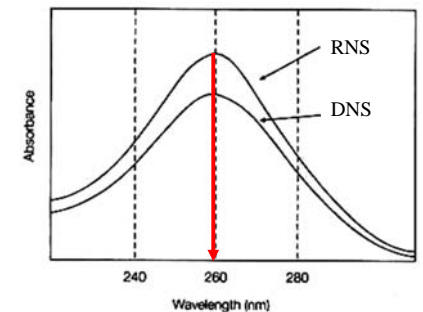
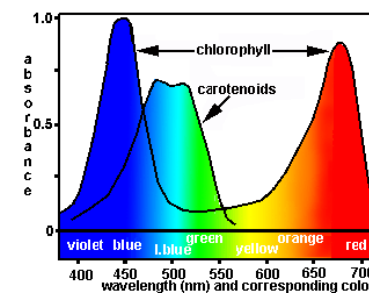


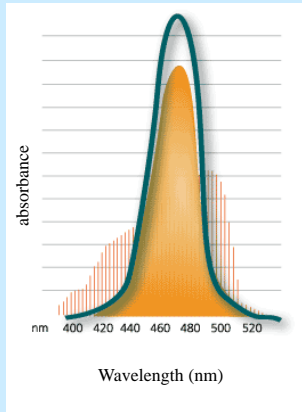
Absorption spectrum:

Absorbance as the function of the wavelength.

“Band” spektrum

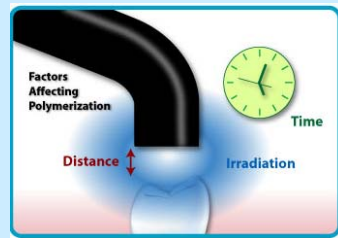
absorption spectrum of some biological macromolecules





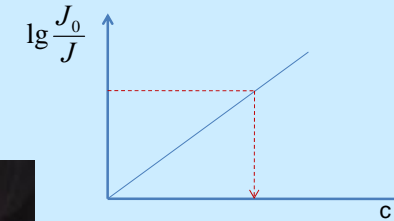
Camphor chinone

Application in dentistry



$$\lg \frac{J_0}{J} = \epsilon_{(\lambda)} \cdot c \cdot x$$

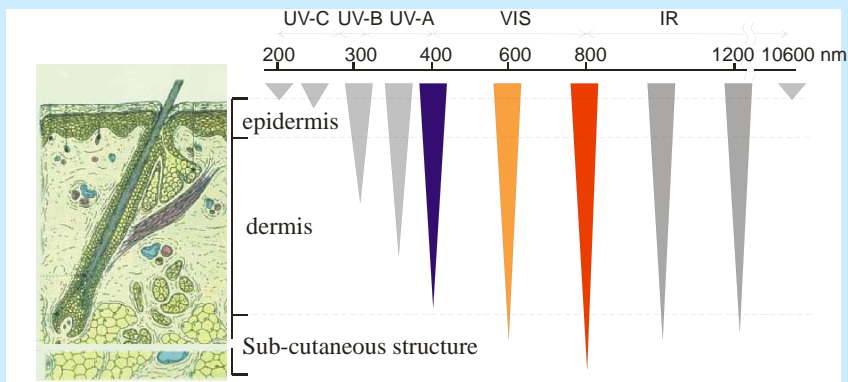
in dilute solutions absorbance is proportional to the concentration



Absorption based determination of concentration



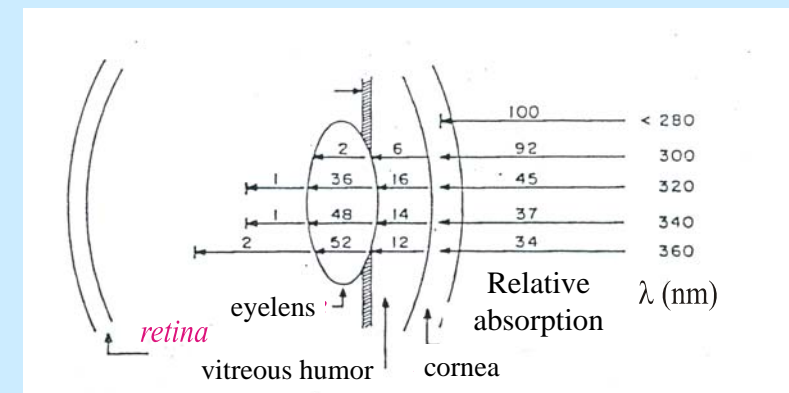
Penetration of light into the skin



Light intensity is attenuated due to absorption, reflection, refraction.

Penetration depth depends on the wavelength.

Penetration of light into the skin



Damjanovich, Fidy, Szöllősi: Medical Biophysics

II. 1.1.

1.1.1

1.1.3

II. 2. 1.

2.1.1

2.1.2

2.1.3

2.1.4

2.1.5

2.1.8

VI.3

3.1.1

3.1.2