

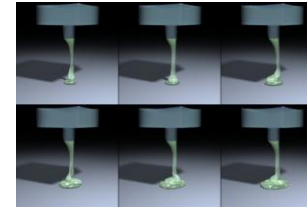
Physical basis of dental material science 9.

Mechanical properties 3.

1

Viscoelasticity:

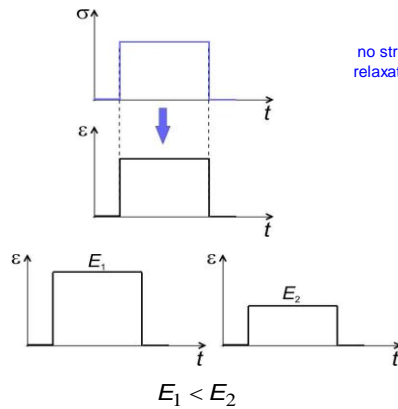
materials which exhibit both viscous and elastic characteristics when undergoing deformation.



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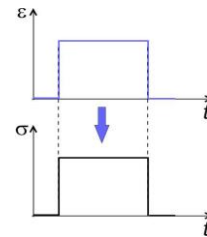
Ideal elastic body

Constant force (stress)



no stress relaxation!

Constant deformation



Hooke's law: $\sigma = E\varepsilon$
 $\sigma_{\text{shear}} = G\gamma$

Model:

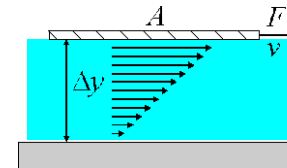


Hookean elastic spring

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Viscosity (η):

measure of the resistance of a fluid which is deformed by either shear stress or tensile stress.



A: surface
F: force
 Δy : layer thickness
v: speed

Newton's friction law:

$$F_s = \eta \cdot A \cdot \frac{\Delta v}{\Delta y}$$

viscosity (internal friction coefficient)

$$[\eta] = \text{Pa} \cdot \text{s}$$

$$\frac{F_s}{A} = \eta \cdot \frac{\Delta v}{\Delta y}$$

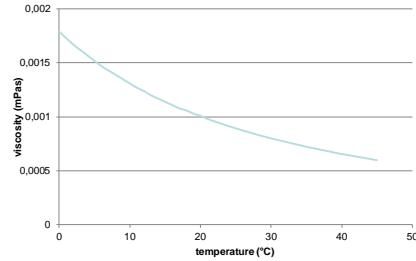
$$\sigma_{\text{shear}} = \eta \cdot \gamma_{\text{speed}}$$

velocity gradient

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Dependence on the temperature

viscosity of the water



honey in fridge or room



oil in winter and summer



strongly depends on the temperature.

$$\eta \sim e^{-bT}$$

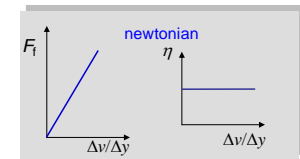
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e.g. at 20 °C:

material	air	water	blood (37°)	glycerine
η (mPa·s)	0.019	1	2–8	1490

Normal (or newtonian) fluid:

The viscosity depends only on the temperature (independent from e.g. velocity gradient or speed of flow).



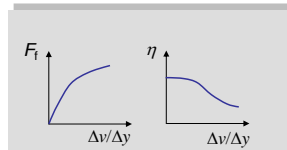
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Anomalous (or non-newtonian) fluids:

The viscosity depends on the **velocity gradient**.

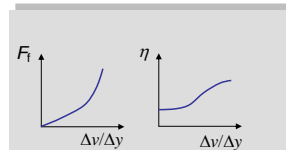
Pseudoplastic:

Viscosity decreases with the rate of shear.

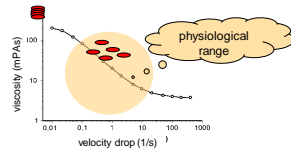


Dilatant:

Viscosity increases with the rate of shear.

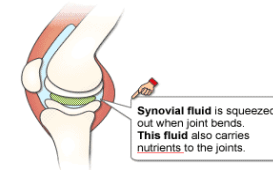
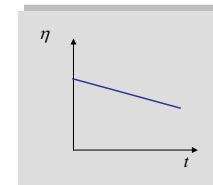


blood

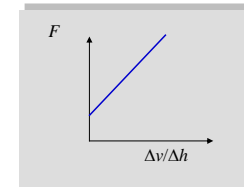


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Tixotropy: normally viscous, but becomes flow if stressed.



Bingham-fluid: behaves as a rigid body at low stresses but flows as a viscous fluid at high stress.



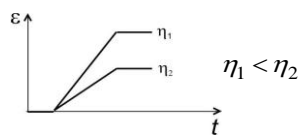
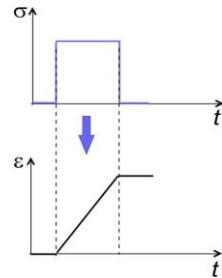
Tooth-paste



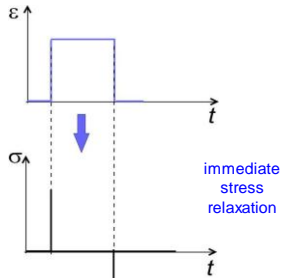
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Ideal viscous body

Deformation in the case of constant force (stress).



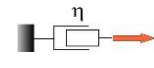
Constant deformation



Newton's law:

$$\sigma_{\text{shear}} = \eta \dot{\gamma}_{\text{speed}}$$

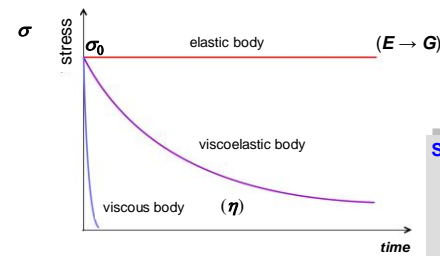
Model:



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Viscoelasticity:

After instant deformation:



Hooke's law

$$\sigma = E \epsilon$$

$$\sigma_{\text{shear}} = G \gamma$$

Stress relaxation:

$$\sigma = \sigma_0 e^{-\frac{t}{t_{\text{rel}}}}$$

$$t_{\text{rel}} = \frac{\eta}{G}$$

relaxation time

Newton's law

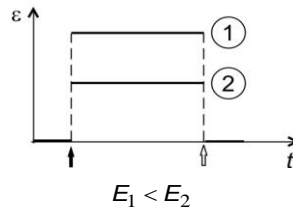
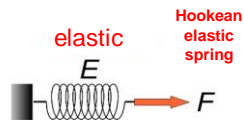
$$\sigma_{\text{shear}} = \eta \dot{\gamma}_{\text{speed}}$$



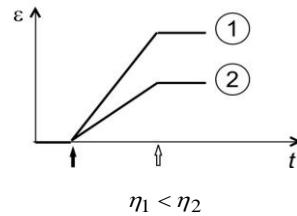
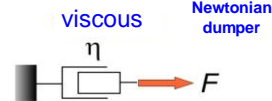
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Changing deformation in the case of constant force

Models:



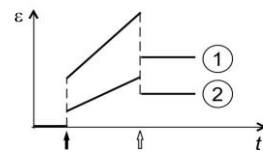
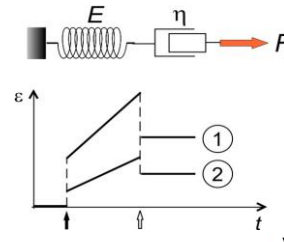
Hookean elastic spring



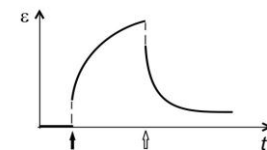
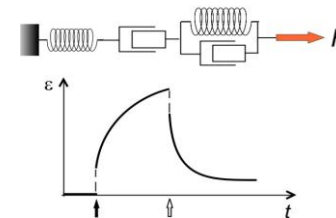
viscous Newtonian dumper

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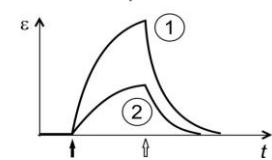
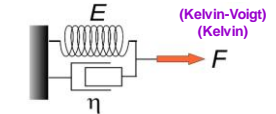
viscoelastic - Maxwell



viscoelastic - Burgers



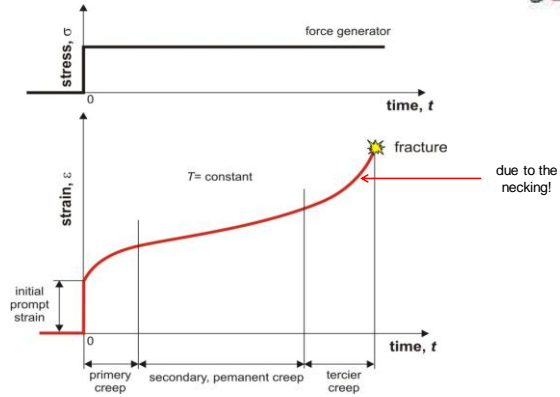
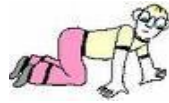
viscoelastic - Voigt



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Creep:

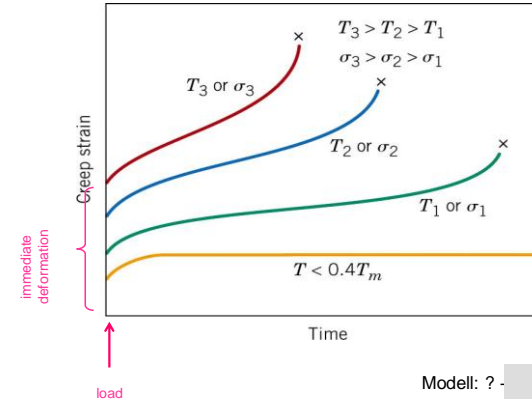
is the slow change in the dimensions of a material due to prolonged stress.



1-10⁷ s !!

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Effect of the stress and the temperature

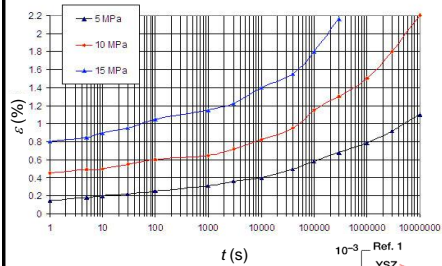


temperature!
e.g. metals
 $0.4T_m < T$

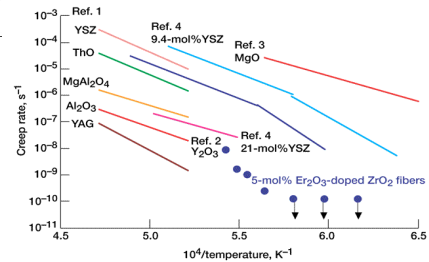
Modell: ?

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PP Creep Curve



Polypropylene (PP)

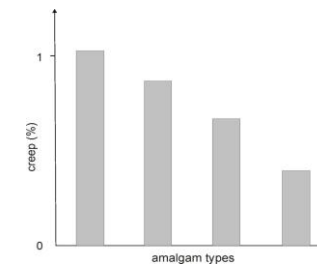


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Example: amalgam

Creep influences the marginal integrity of the filling.

melting point: 100 – 180 °C!



Increasing silver or copper content decreases the creep.

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Relaxation

shape recovery

recovery when the load stops.



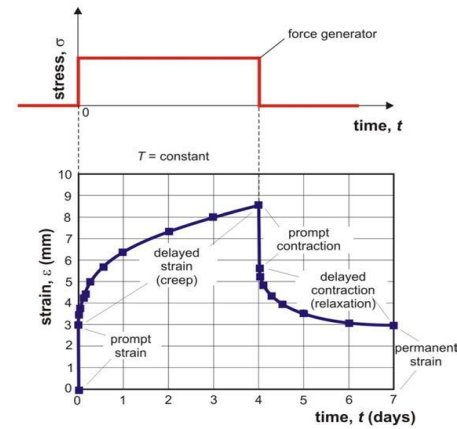
stress relaxation

decrease of the stress in constant deformation .



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Shape recovery after stress removed.



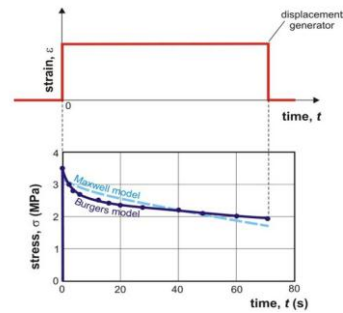
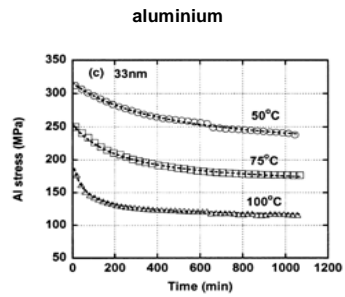
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Stress relaxation

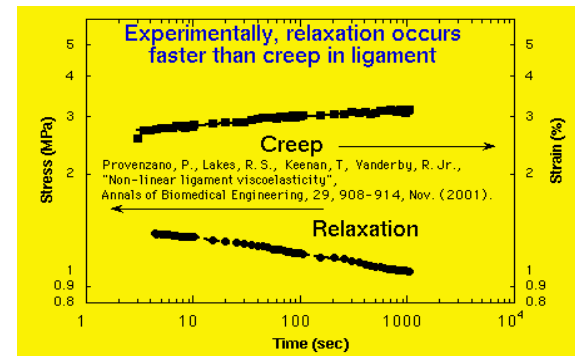
Decreasing of the inner stress in the case of constant deformation.



film made of myofibrillar proteins



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Fatigue



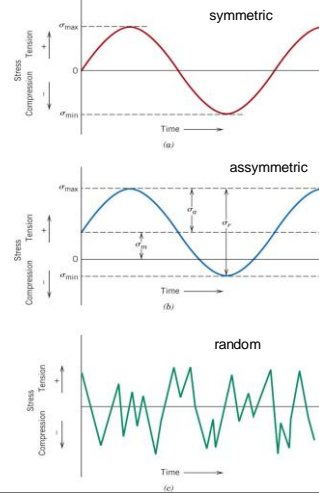
Long, repeated load

→ structural changes

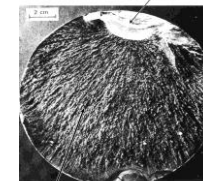
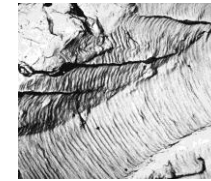
→ strength decreases

cracks!

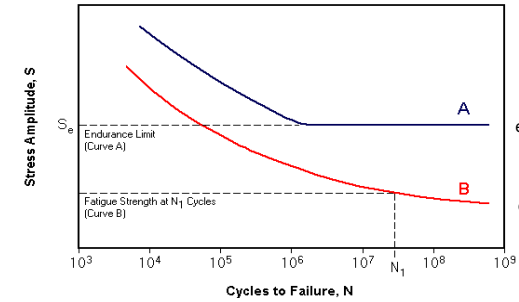
type of loads:



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Fatigue S-N curve:

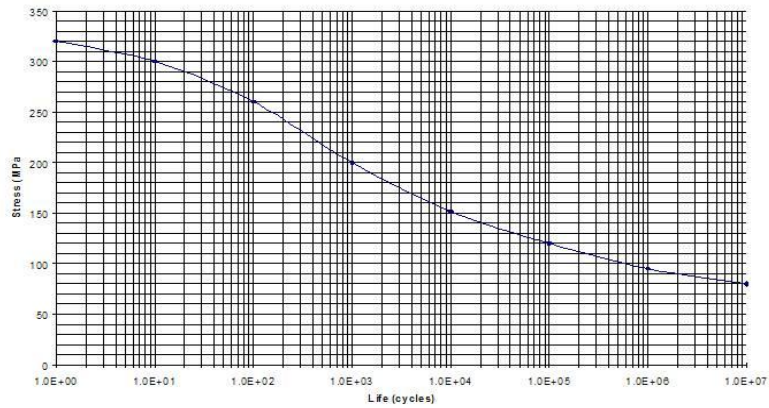


e.g. steel, titanium, ...

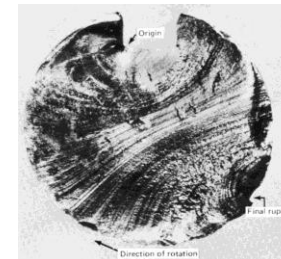
e.g. aluminium, copper, ...

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S-N CURVE FOR BRITTLE ALUMINIUM WITH A UTS OF 320 MPa



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a test equipment

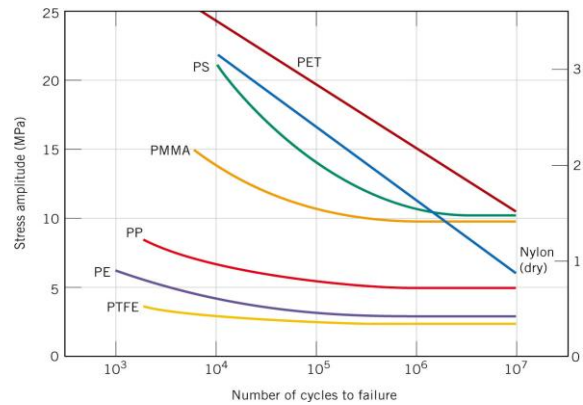


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S-N curves of different polymers

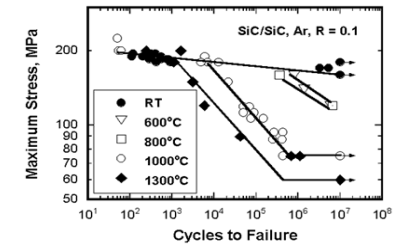
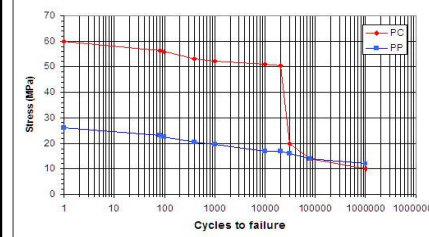
PET: Polyethylene terephthalate
PS: Polystyrene
PMMA: Poly(methyl methacrylate)

PP: Polyethylene terephthalate
PE: Polyethylene
PTFE: Polytetrafluoroethylene



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Dynamic fatigue at 0.5Hz, 20C



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Abrasion



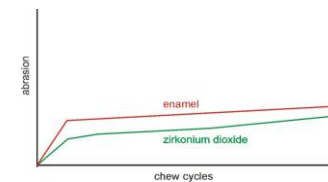
Loss of the structure by mechanical forces.

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Role of hardness

Most commonly affected: premolars and canines.

Cemento-enamel junction
(very thin enamel)



material	HV (MPa)	HK (MPa)
Enamel	≈ 3400	3400-4000
Dentin	≈ 600	≈ 700
Amalgam	≈ 1000	

(cementum a little bit less than the dentine.)

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