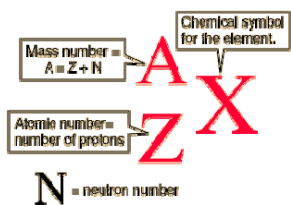


Radioactivity in Medicine

Some medical applications of nuclear radiation



Reminder: basic definitions



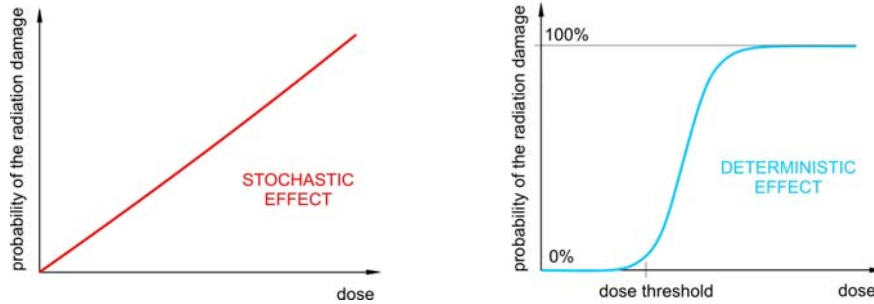
mass number (A)
atomic number (Z)
 $A = Z + N$

- Nuclides with equal proton number (Z), but different neutron numbers (N) are called **isotopes** of an element.
- Unstable isotopes (=radioactive isotopes) decay:
- Decay types:** α , β^- , β^+ , electron-capture, isomeric transition
- Nuclear radiations:** α (He^{2+}), β^- (e^-), β^+ (e^+), γ (electromagn.)

Biological effects of ionizing radiation



Stochastic and deterministic damages



Deterministic effects

- Large number of cells killed – physiological effect, e.g.
 - **Erythema, epilation, cataracts, “radiation sickness”**
- No risk below threshold doses, e.g.
 - Opacities = 500 mGy
 - Transient erythema = 2 Gy



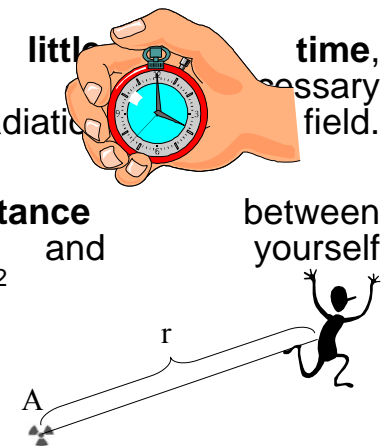
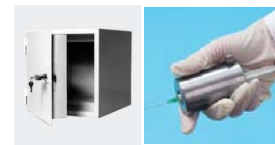
Stochastic damage

- can be caused by a single photon
- the **severity is not effected by the dose**
- with increasing dose only the **probability increases** (somatic cells: cancer, reproductive cells: hereditary effects)

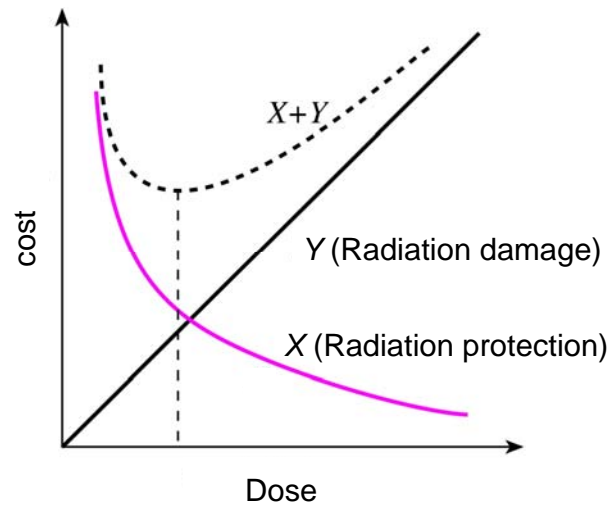
*1 gamma photon: the probability to cause cancer is 3×10^{-16}
(1: 3,000 billion, but this is the Russian roulette!)*

Basic radiation protection strategies

- spend as little time, as possible in the radiation field.
- keep the distance between yourself and the radiation source as large as possible. Dose $\sim 1/r^2$
- use shielding.



ALARA principle (as low as reasonably achievable)



Imaging using radioactive nuclides



Basic steps of the isotope diagnostics

Radioactive material introduced into the patient

Distribution and alteration of activity is detected

Monitoring of physiological pathways and/or identification and localization of pathological changes

Information from various medical imaging techniques

Structure



X-ray

Ultrasound

MRI

differences according to the different physical parameters / properties of tissues

Function



Isotope diagnostics

MRI

dynamic physiological / metabolic processes of different body organs can be followed



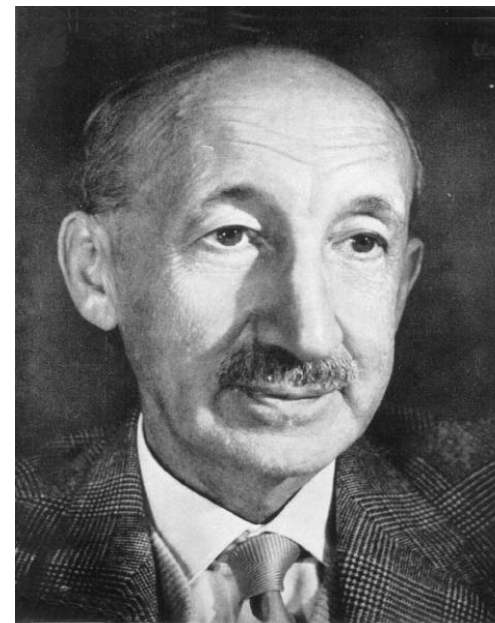
X-ray

Shows the structure



Isotope diagnostics

*Reports the
metabolic activity*



Georg Charles de Hevesy

Father of Nuclear Medicine

Georg Charles de Hevesy
(1885 - 1966)

Nobel Prize in Chemistry
1943

**for his work on the use of
isotopes as tracers in the
study of chemical
processes**

The choice of the appropriate radioisotope for nuclear imaging

Maximise the information

Minimise the risk.

For that find the optimal

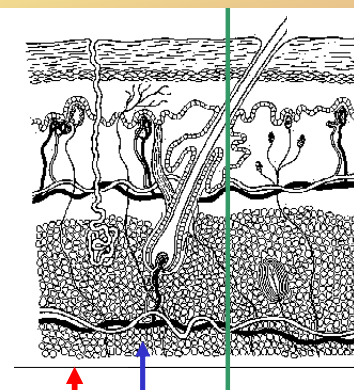
type of radiation

photon energy

half life

radiopharmakon

Type of radiation



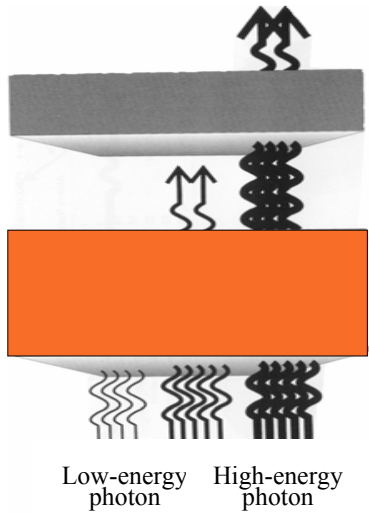
α β γ

Only **γ -radiation** has
sufficient penetration
distance .

Decay via photon emission
is needed to minimize
absorption (radiation
damage) in body tissue

purely gamma-emitting isotope would be preferable

Photon energy



Photon must have sufficient energy to penetrate body tissue with minimal attenuation

BUT!

Photon must have sufficiently low energy to be registered efficiently in detector and to allow the efficient use of lead collimator systems (must be absorbed in lead)

Suitable physical half-life

$$\Lambda = \lambda N = \frac{0,693}{T} N$$

smaller is better
but
the value is limited from below
e.g., by the sensitivity of the detector

smaller is better
dosimetric considerations for patients

shorter is better
but

- it has to be long enough for monitoring the physiological organ functions to be studied
- short lifetime isotopes cannot be transported

Optimal activity for diagnostic procedure

Maximize the information

Minimize the risk

$$\Lambda \sim 100 \text{ MBq}$$

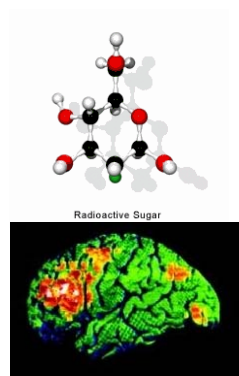
How to reach the target organ?

- Use the isotope of an element, which is accumulating in the target organ under physiological conditions (e.g. I for thyroid gland)
- Use carrier molecules.
Radiopharmaceutical = a radioactive tracer atom (isotope) which emits the signal + a pharmaceutically-active molecule (carrier) which selects the target organ.

Radiopharmaceuticals:

FDG (Fluoro-deoxyglucose)

Tc99m-Phosphonates (bone imaging)

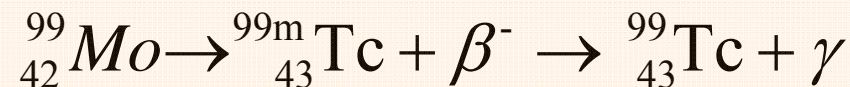


Basic requirements:

specific localizing properties;
high *target : nontarget* ratio

have no pharmacological or
toxicological effects which may
interfere with the organ function
under study.

Isomeric transition



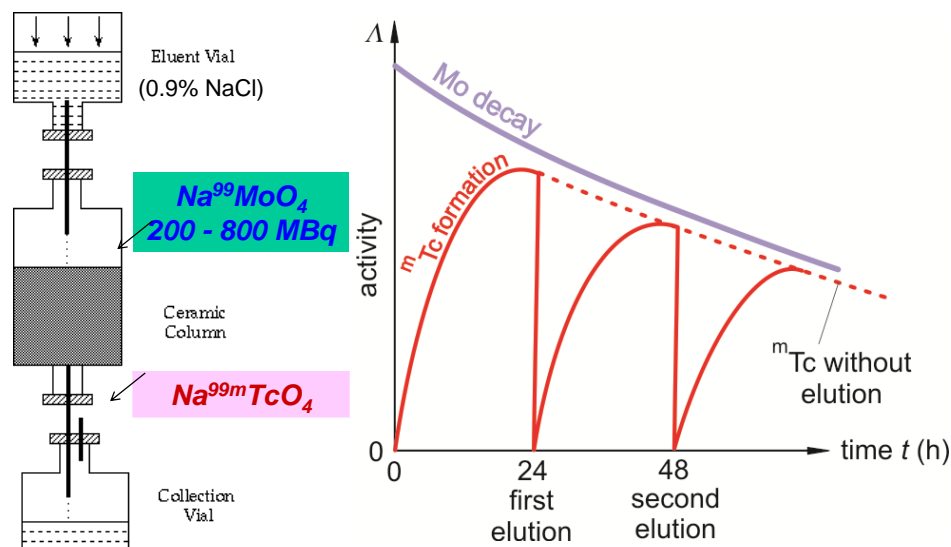
$T_{1/2}=67$ hours

$T_{1/2}=6$ hours

$hf=140$ keV

One of the features that makes **Tc-99m** such an ideal radioisotope for diagnostic imaging is its ability to **readily bind to a wide variety of compounds** under physiological conditions.

Technetium-99m generator



Examples

pharmaceutical	radioisotope	activity (MBq)	target organ
Pertechnetate	${}^{99\text{m}}\text{Tc}$	550 - 1200	brain
Pirophosphate	${}^{99\text{m}}\text{Tc}$	400 - 600	heart
Diethylene Triamine Penta Acetic Acid (DTPA)	${}^{99\text{m}}\text{Tc}$	20 - 40	lung
Mercaptoacetyltriglycine (MAG3)	${}^{99\text{m}}\text{Tc}$	50 - 400	kidney
Methylene Diphosphonate (MDP)	${}^{99\text{m}}\text{Tc}$	350 - 750	bones

Types of images

Static picture
spatial distribution of
isotope/activity at a
certain time

Dynamic picture
variation of the amount
of isotope/activity as a
function of time

Static and dynamic picture – series of static recordings

Types of images

Summation image

γ -camera

Tomographic image
Emission CT

- SPECT (Single Photon Emission Computed Tomography)
- PET (Positron Emission Tomography)



Hal Anger
1920-2005



Hal Anger and coworkers
1952



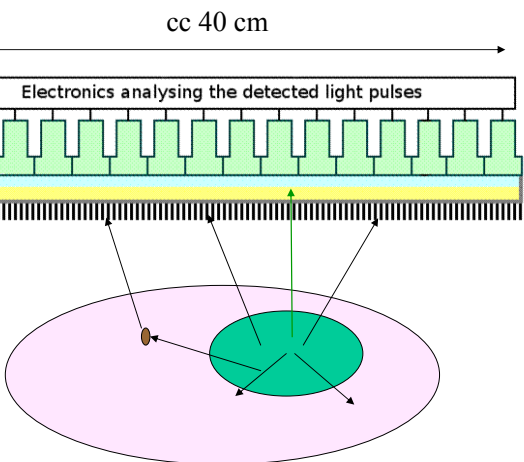
Gamma
camera

Photomultiplier tubes

Light guide

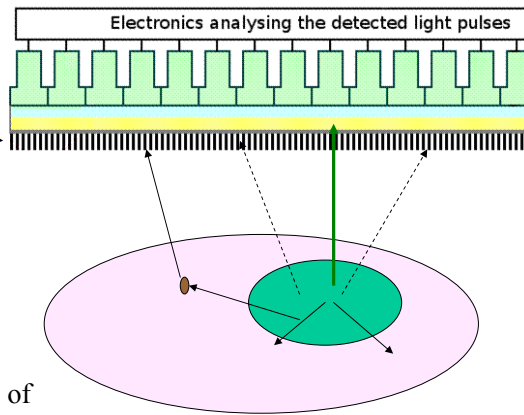
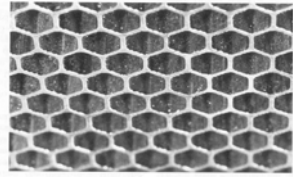
Scintillation crystal

Collimator



A radioactive source emits gamma ray photons in all directions.

collimator

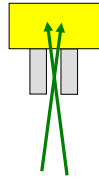


Collimators are composed of thousands of precisely aligned **channels** made of lead.

The collimator conveys only those photons traveling directly **along** the long axis of each **hole**.

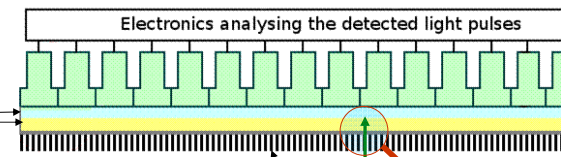
Photons emitted in other directions are absorbed by the septa between the holes.

Size and geometry of holes are essential for the **resolution**.



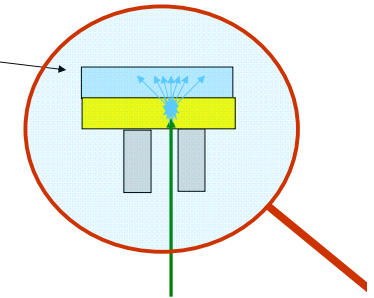
Scintillation crystal

Na(Tl)

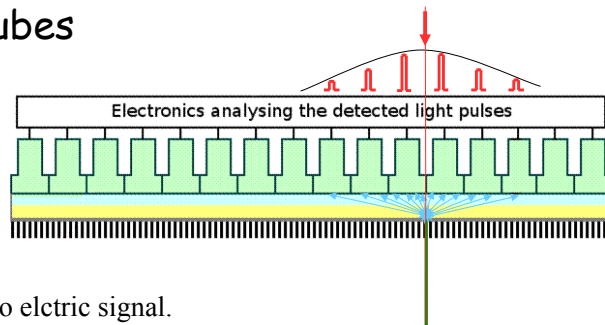
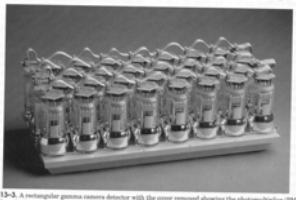


Light guide

Distribution of the light for the photomultipliers

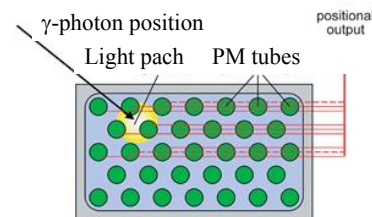


Photomultiplier tubes

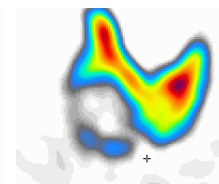
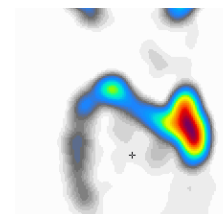
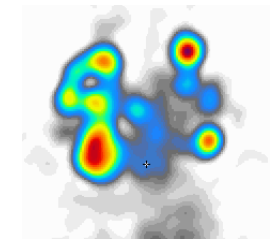
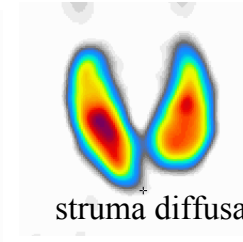
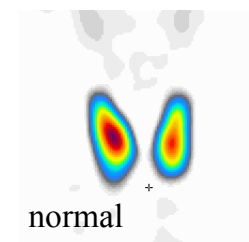


Transformation of light pulses to electric signal.

Typically 37-91 tubes,
5-7 cm diameter each

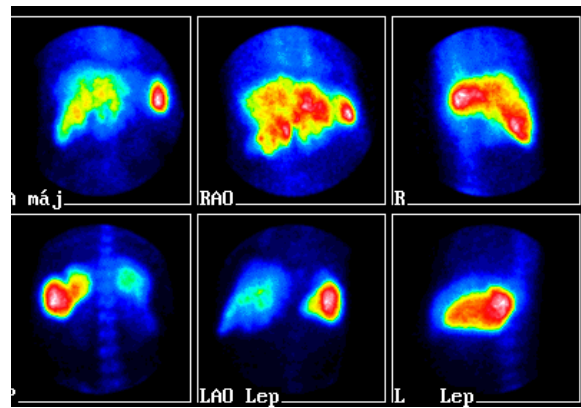


Pertechnetate (intravenous 80 MBq) distribution in thyroid glands



Cold nodules

Liver lesion nodules



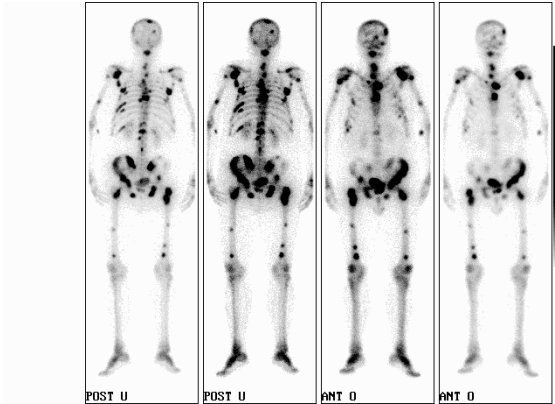
^{99m}Tc- fyton

Bone scintigraphy

^{99m}Tc-MDP: 600 MBq



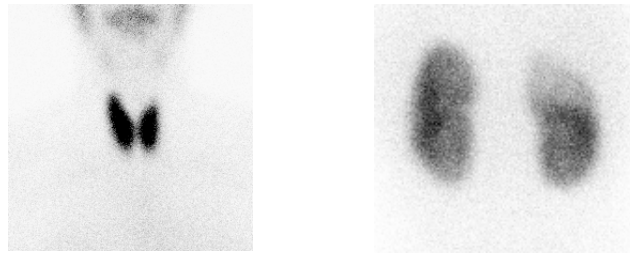
normal



imaging in bone metastases

Static picture

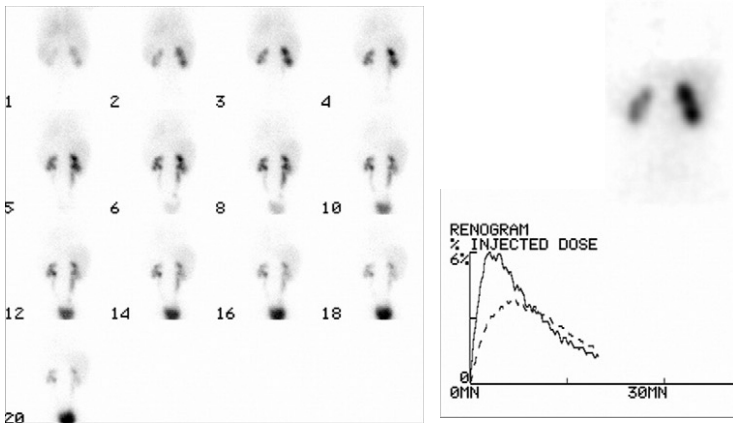
Static picture – spatial distribution of isotope / activity
at a certain time



Isotope accumulation in
thyroid glands kidneys

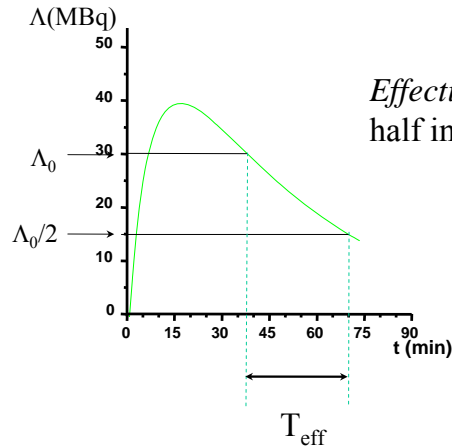
Static and dynamic picture

Dynamic picture – variation of the amount of isotope /
activity in time

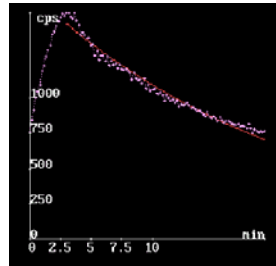


Static and dynamic picture

Dynamic picture – variation of the amount of isotope / activity in time

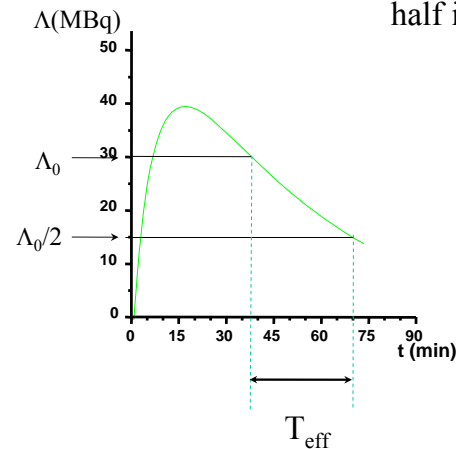


Effective half-life – activity decreases by half in the target organ



Effective half life

Effective half life – activity decreases by half in the target organ



$$\Lambda = \Lambda_0 e^{-(\lambda_{phys} + \lambda_{biol})t}$$

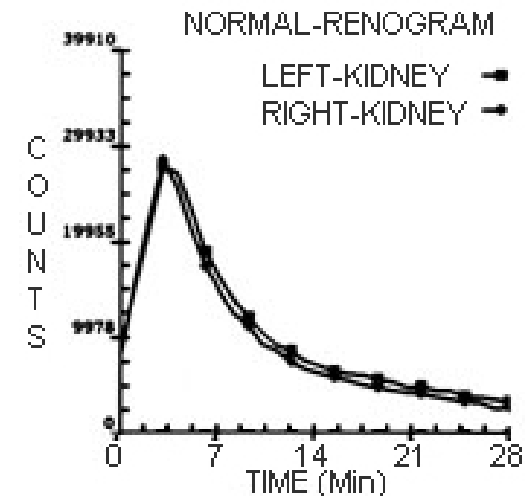
$$\lambda_{effective} = \lambda_{phys} + \lambda_{biol}$$

$$\frac{1}{T_{eff}} = \frac{1}{T_{phys}} + \frac{1}{T_{biol}}$$

Biological half life

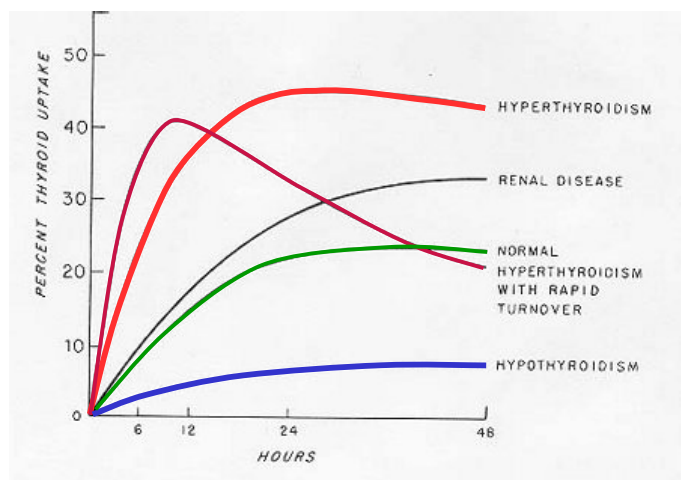
The final fate of the radiotracer depends on how the addressed organ deals with the molecule, whether it is absorbed, broken down by intracellular chemical processes or whether it exits from the cells and is removed by kidney or liver processes. These processes determine the **biological half-life** T_{biol} of the radiopharmaceutical.

example



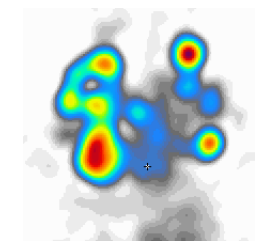
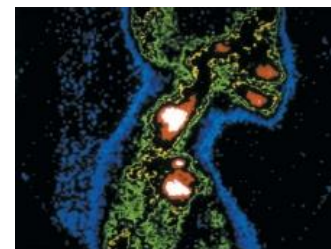
Isotope accumulation in kidney

example



Thyroid glands
Isotope accumulation

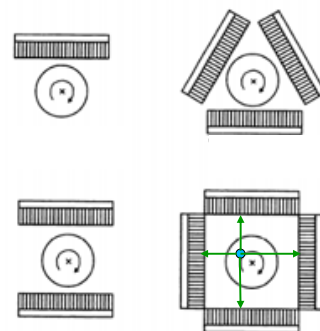
Gamma camera image:
summation image



For depth resolution: tomographic device is necessary

SPECT

Single Photon Emission Computed
Tomography



Various camera arrangements

SPECT

Tomographic application of γ -cameras – data collection in 360° .

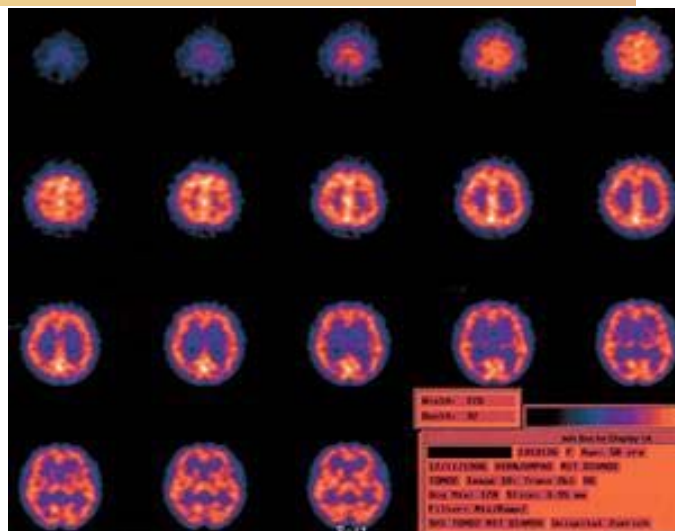
Cross-sectional image can be reconstructed.

Measurement from a series of projections.

Computer directs the movement of the detector, stores the data,
reconstruct the cross-sectional image

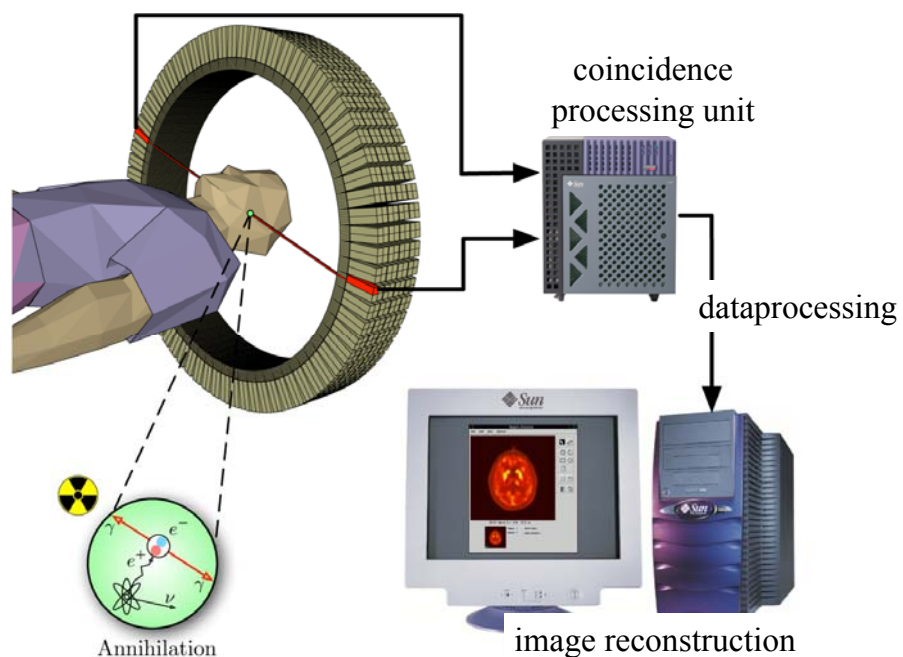
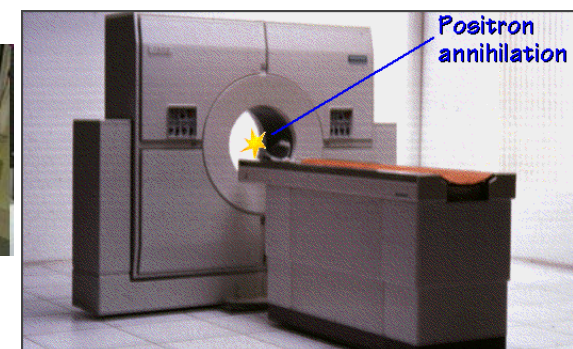
SPECT – images of scalp

^{99m}Tc - HMPAO



PET

Positron Emission Tomography



The most frequently used radionuclides in PET are radioisotopes of structural elements of natural organic molecules.

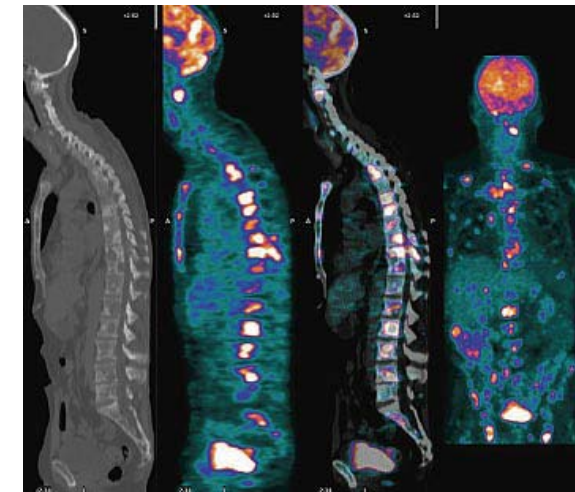
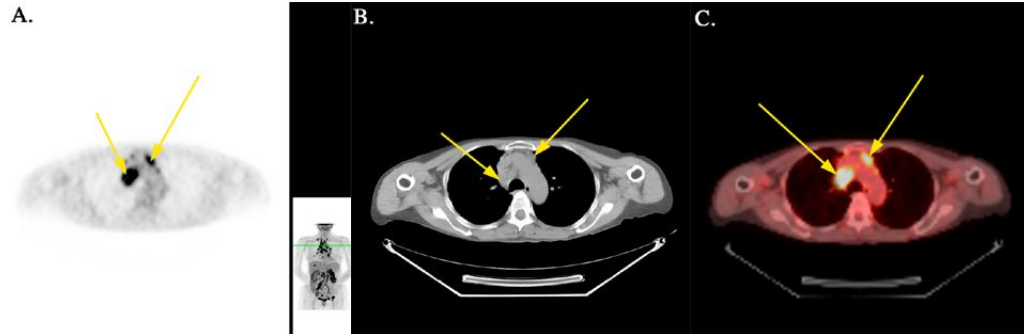
Isotope	β^+ energy (MeV)	β^+ range (mm)	1/2-life	Applications
^{11}C	0.96	1.1	20.3 min	receptor studies
^{15}O	1.70	1.5	2.03 min	stroke/activation
^{18}F	0.64	1.0	109.8 min	oncology/neurology
^{124}I	2.1350/1.5323	1.7/1.4	4.5 days	oncology

Isotope manufacturing nearby the site of application (see half-lives).



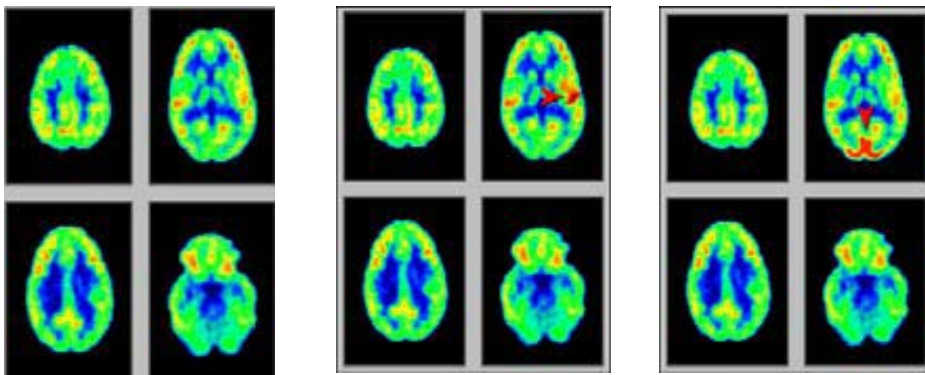
PET/CT

Combination of structural and functional imaging



CT PET PET/CT PET

Activity of brain areas



Radiation therapy



Radiotherapy : ionizing radiation induces damages at molecular and cellular level. This can be beneficial against tumour tissues

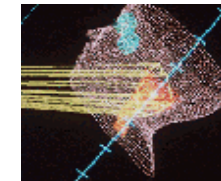
1. Which radiation is the best?
2. What is the optimal dose of radiation?
3. What is the best technique for generation radiation?
4. Irradiation selectivity – protection of healthy structures?

Approaches

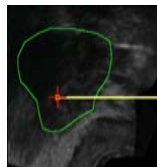
Palliative radiotherapy to reduce pain and address acute symptoms – e.g. bone metastasis, spinal cord compression etc.,

Radical radiotherapy as primary modality for cure – e.g. head and neck

Adjuvant treatment in conjunction with surgery – e.g. breast cancer



α



Internally deposited radioactivity

β^- ,

e^- ,

γ ,

Rtg,

p

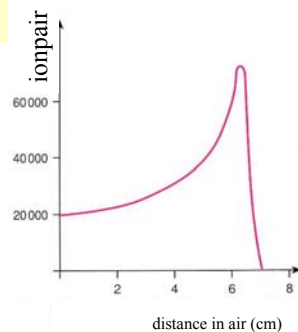
n

Linear ion density:

the amount of ion pairs in a line generated in a unit distance (n/l)

LET (Linear Energy Transfer) : the energy transferred to the material surrounding the particle track, by means of secondary electrons. ($nE_{ionpair}/l$)

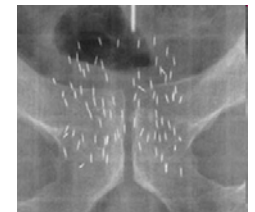
In the air: $E_{ionpair} = 34 \text{ eV}$



α

Particle energy is not optimal
continuous energy spectrum
typical energy: few MeV

β^-



Internally seeded radioactivity

e^-

accelerated electron - 10-20 MeV

γ ,

production: linear accelerator

Rtg,

Efficient distance! $\approx 1 \text{ cm}/3 \text{ MeV}$

p

In the practice 6-21 MeV \Rightarrow 2-7 cm

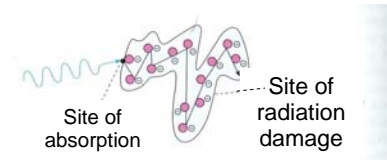
n

treatment of superficial tumours

γ : external radiation source

Site of absorption \neq sites of ionization = site of radiation damages

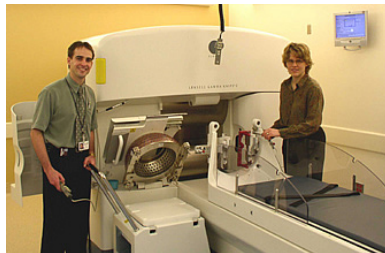
Penetration distance
is energy dependent



γ -knife: focused dose of radiation

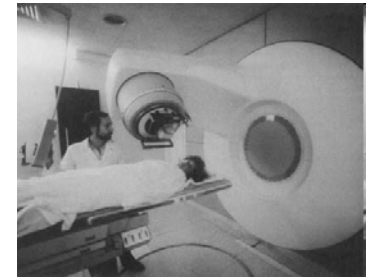
about 200 portals in a specifically
designed helmet

e.g., ^{60}Co $E_\gamma \approx \text{MeV}$,
about TBq activity



Treat tumours and lesions in the brain

X/ray:



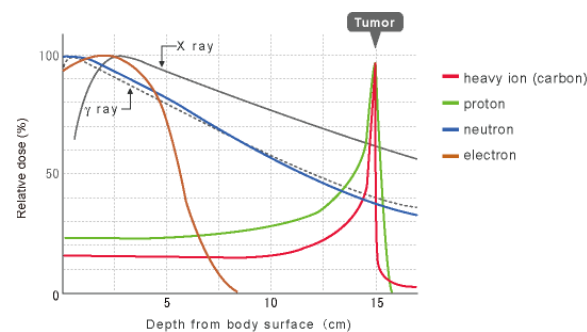
The X-rays are generated by a linear accelerator .

Few MeV photon energy.



Would be ideal, but very expensive!

γ ,
 R_{tg} ,
 p :
 n



Dosimetry

How can we quantify the effects caused by ionizing radiations?

Pharmacological and radiation dose concepts are different!

Physical doses: absorbed dose

Absorbed dose (D)

$$D = \frac{\Delta E}{\Delta m} = \frac{1}{\rho} \frac{\Delta E}{\Delta V}$$

$$1 \text{ Gy} = 1 \text{ J/kg}$$

- absorbed energy in unit mass of absorbing medium
- applicable: X-ray, α , β , γ radiations, neutrons, accelerated charged particles etc.
- disadvantage: hard to measure directly

Absorbed dose, typical values

Chest X-ray = 160 μ Gy skin dose

Background radiation 2.4 mGy/year

Typical 1 minute screening = 20 mGy skin dose

LD₅₀ = 4 Gy to whole body (single dose)

Threshold for transient erythema = 2 Gy .

Radiotherapy dose = 40 Gy to tumour (over several weeks)

Absorbed dose is used for prediction of biological consequences in case of **acute irradiation** (i.e. *large* amount of radiation over a *short* period of time).
Deterministic effect!

Physical doses: Exposure (X)

Exposure (X):

$$X = \frac{\Delta Q}{\Delta m} = \frac{1}{\rho} \frac{\Delta Q}{\Delta V}$$

$$(C / kg)$$

- valid for only X-, γ -rays (< 3 MeV)
- characterizes the ionizing power of radiation in air, instead of the absorbed energy in tissue

Calculation of the absorbed dose

$$D_{air} = f_0 X \quad f_0 = 34 \text{ Gy} / \text{C kg}^{-1}$$

$$D_{tissue} = D_{air} \frac{\mu_{m,tissue}}{\mu_{m,air}} \quad E < 0.6 \text{ MeV}$$

Biological doses: equivalent dose

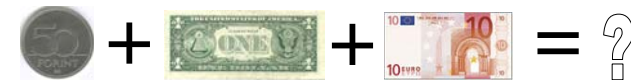
Equivalent dose (H_T)

Sum of absorbed doses weighted according to type of radiation

$$H_T = \sum_R w_R D_{T,R}$$

Unit: J / kg with special name: sievert, Sv

$D_{T,R}$... the absorbed dose averaged over the tissue (T) due to radiation (R)



Radiation weighting factor

represents the effectiveness of radiation inducing stochastic effect at low doses

Weighting factors of different radiations and energies

Radiation and energy range	Radiation weighting factor
Photons, at every energy	1
Electrons, muons, at every energy	1
Neutrons, if the energy is	
<10 keV	5
10 keV–100 keV	10
100 keV–2 MeV	20
2 MeV–20 MeV	10
> 20 MeV	5
Protons, if the energy is	
> 2 MeV	5
α -particles, nuclear fission products, heavy nuclei	20

Biological doses: effective dose

Effective dose (E)

the sum of weighted H_T in all tissues and organs in the body

$$E = \sum_T w_T H_T$$

$$\sum_T w_T = 1$$

Unit: Sv (J / kg)

provide a basis for estimating the **probability** of **stochastic effects** for doses well below the threshold of deterministic effects

Tissue weighting factors

represent the relative contribution of that organ or tissue to the total damage due to the total of stochastic effects resulting from uniform irradiation of the whole body

Weighting factors of various tissues and organs

Tissue/Organ	Weighting factor, w_T
Gonads	0.20
Red bone marrow	0.12
Large intestine	0.12
Lungs	0.12
Stomach	0.12
Bladder	0.05
Breast	0.05
Liver	0.05
Oesophagus	0.05
Thyroid gland	0.05
Skin	0.01
Surface of the bones	0.01
Other	0.05

Approximate effective doses

Examination	E (mSv)
Chest X-ray	0.04
Chest CT	7.8
Cranial CT	1.8
Abdominal X-ray	1.2
Abdominal CT	7.6
X-ray of the dorsal vertebrae	1.0
X-ray of the lumbar vertebrae	2.1
Barium enema with fluoroscopy	8.7



Risk – loss of life expectancy

Days of average life expectancy
lost due to various causes

Being an unmarried male	3500
Smoking (1 pack/day)	2250
Being an unmarried female	1600
Being a coal miner	1100
25% overweight	777
Alcohol abuse (U.S. average)	365
Being a construction worker	227
Driving a motor vehicle	207
All industries	60
Radiation: 1 mSv/yr x 70 years	10
Coffee	6



Relative risk of dying: 1 in a million odds

- Smoking 1.4 cigarettes (lung cancer)
- Eating 40 tablespoons of peanut butter
- Eating 100 charcoal broiled steaks
- 2 days in New York City (air pollution)
- Driving 40 miles in a car (accident)
- Flying 2500 miles in a jet (accident)
- Canoeing for 6 miles
- Receiving 0.10 mSv radiation dose (cancer)



Radiation protection

Aim: users of the sources and the members of the public are not irradiated above acceptable risk.

1. Prevention of deterministic effects (except in radiotherapy)
2. Reduction of the probability of stochastic effects

Acceptable risk: radiation illness due to the received ionizing radiation cannot be shown statistically unambiguously.

Medicine: cost-benefit