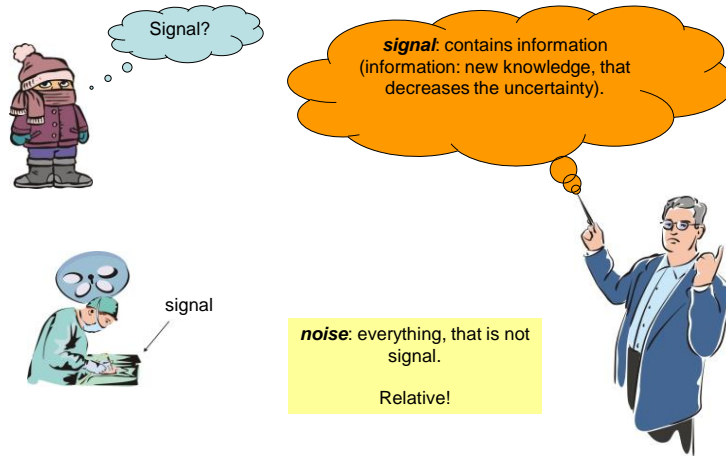


## Medical signal processing



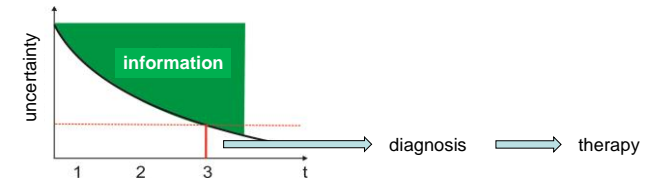
## Information



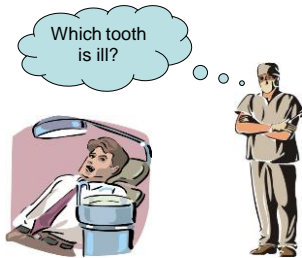
1. Enters.
2. Complaint?
3. Which?

information:

1. A patient.
2. I've a toothache.
3. Third molar.



## Information content



32 possible answers! The uncertainty is enough large.

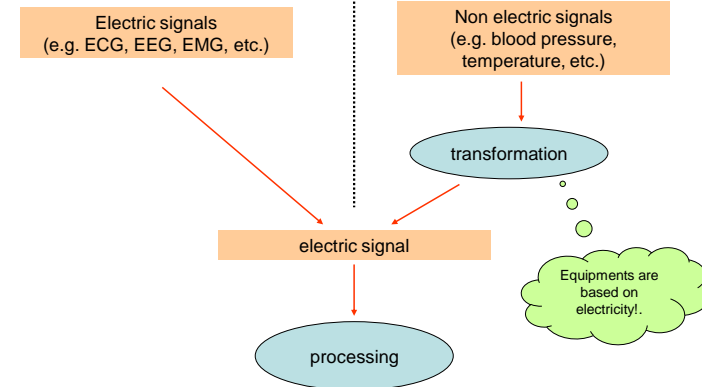
1. Upper? - not. Only 16 possible places. Decreasing uncertainty.
2. On the left? - not. 8 possible places.



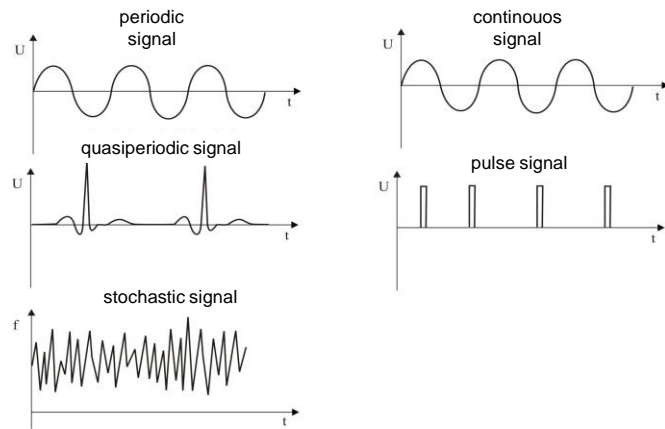
Five right questions are necessary to identify the place!  
**Information content: 5 bit** ( $2^5 = 32$ )

Bit: unit of the information.

## Classification of the signals 1.

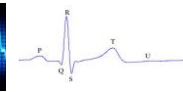


## Classification of the signals 2.



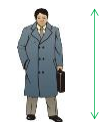
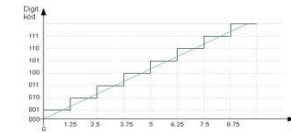
## Classification of the signals 3.

### analog signal



In a certain range every value is possible.

### digital signal



height:  
analog signal

measurement



height:  
175 cm  
(only discrete values)

## Signal and noise

**Noise is random normally!**

Ideal case: there is no noise!

Real measurements: noise is always present!

Signal to noise ratio:

The ratio of the quantity used to characterize the strength of the signal and the noise.

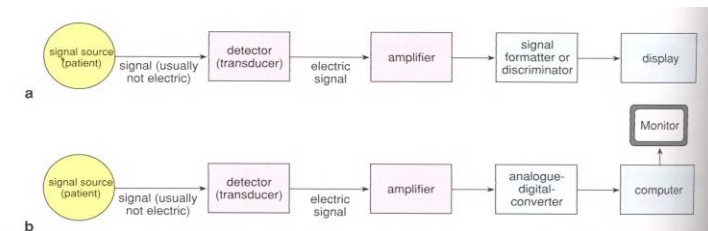
Higher value is better!

How can we increase?

increasing the signal

decreasing the noise

## Signal processing



## Elements in a electric circuit

### passive



resistor



capacitor



inductivity

### active



diode

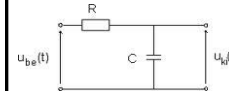


transistor

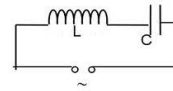
## Electric circuits

A unit consists of elements.

### simple (consists of passive elements)



RC circuit



LC circuit

### complex (consists of passive and active elements)



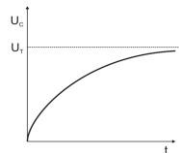
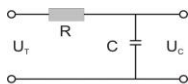
integrated circuit



amplifier

## DC behavior of a RC-circuit

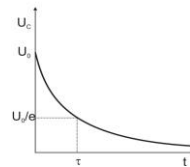
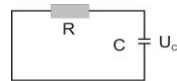
### charging



$$U_C = U_T \cdot \left(1 - e^{-\frac{t}{RC}}\right)$$

$$\tau = RC$$

### discharging

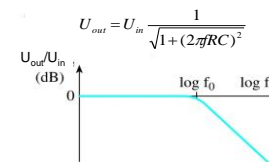
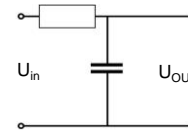


$\tau$  = time constant

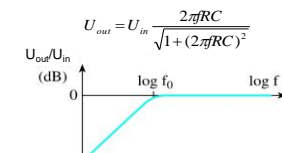
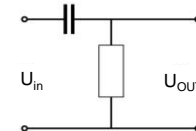
$$U_C = U_0 \cdot e^{-\frac{t}{RC}}$$

## AC behavior of a RC-circuit

### Lowpass filter

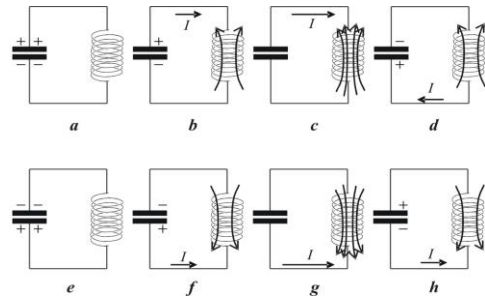


### Highpass filter



## Resonant circuit (LC-circuit)

Electric (in the capacitor) and  
magnetic (in the coil) field



The electric and  
the magnetic field  
periodically are  
built up and  
destroyed.

$$f = \frac{1}{2\pi\sqrt{LC}}$$

## Resonance

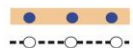
Energy exchange between two oscillating systems is possible only if the resonant frequency of the two systems is enough close to each other.

Tacoma bridge (1940)



## Semiconductors

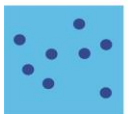
n-type



conductance band

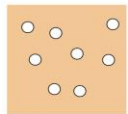
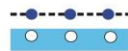


valence band



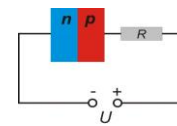
the net charge  
is zero!

p-type

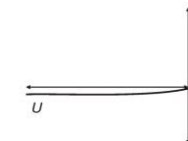
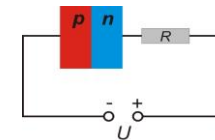


## Working of a diode

forward direction

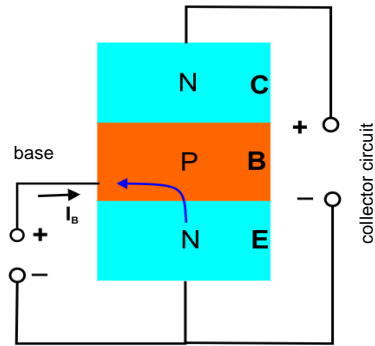


reversed direction



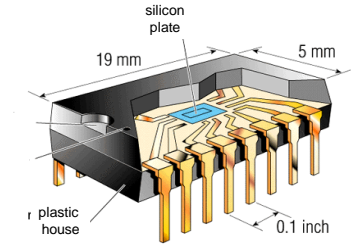
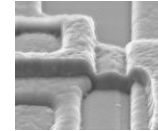
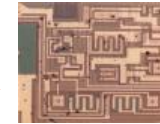
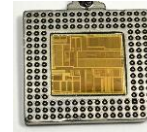
## The transistor

It is built up from 3 layers.



NPN transistor (there is PNP too)

## Integrated circuits (IC)

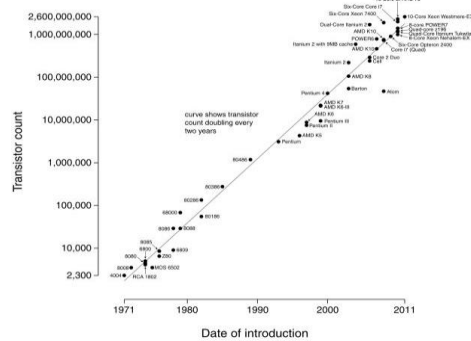


Transistors, diodes, resistors and capacitors are formed on a semiconductor plate producing a complicated electric circuit.

## The development



Microprocessor Transistor Counts 1971-2011 & Moore's Law



There are about  $10^{11}$  neurons in the brain.

## Detectors

sound



microphone

pressure



blood pressure monitor

light



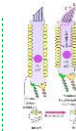
photodiode

scintillation head

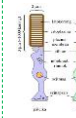


electric signal

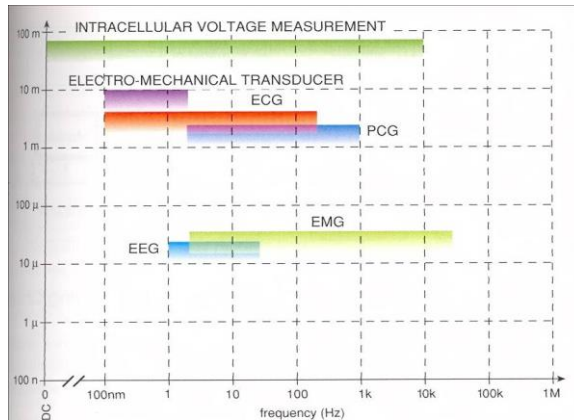
hair cells



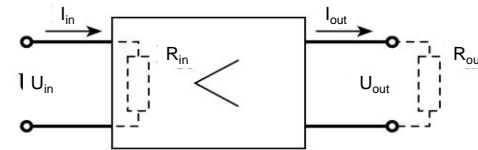
cones and rods



## Biological signals



## Amplifier



**Amplifier if**  
 $P_{out} > P_{in}$

Power gain: ( $A_P$ )

Voltage gain: ( $A_U$ )

$$A_P = \frac{P_{out}}{P_{in}}$$

$$A_U = \frac{U_{out}}{U_{in}}$$

## The decibel scale

Instead of the simple proportion we use frequently the logarithmic of them. This is the decibel-scale.

$$n = 10 \cdot \lg \frac{P_{out}}{P_{in}} \text{ (dB)}$$

$$P = \frac{U^2}{R}$$

$$A_P = \frac{U_{out}^2 / R_{out}}{U_{in}^2 / R_{in}} = \frac{U_{out}^2}{U_{in}^2} \cdot \frac{R_{in}}{R_{out}} = A_U^2 \cdot \frac{R_{in}}{R_{out}}$$

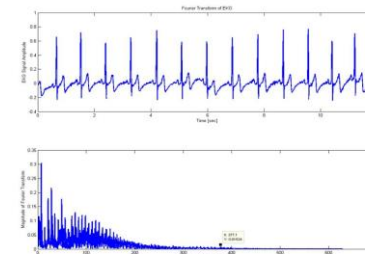
$$n(\text{dB}) = 10 \cdot \lg A_U^2 + 10 \cdot \lg \frac{R_{in}}{R_{out}} = 20 \cdot \lg A_U + 10 \cdot \lg \frac{R_{in}}{R_{out}}$$



## Fourier theoreme

$$y(t) = \sum_k a_k \sin(k \cdot \omega_0 \cdot t + \Phi_k)$$

Every periodic signal may be decomposed into the sum of sinusoidal signals.

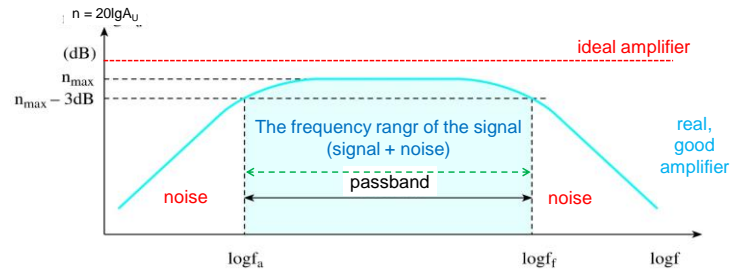


An ecg signal and it's frequency components.

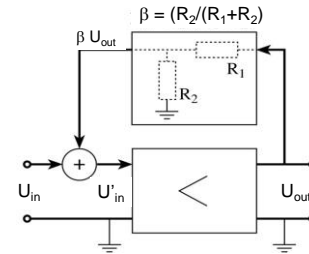
## Transfer characteristics

The amplification (in decibel) as the function of the frequency.

In the presence of the noise the real amplifier is better.

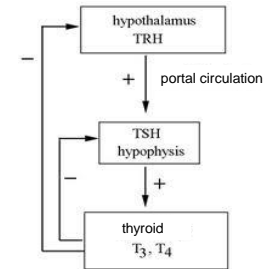


## Feed-back



$$U'_{in} = U_{in} \pm \beta \cdot U_{out}$$

$$A_{U,F} = \frac{U_{out}}{U_{in}} = \frac{A_U}{1 \pm \beta \cdot A_U}$$

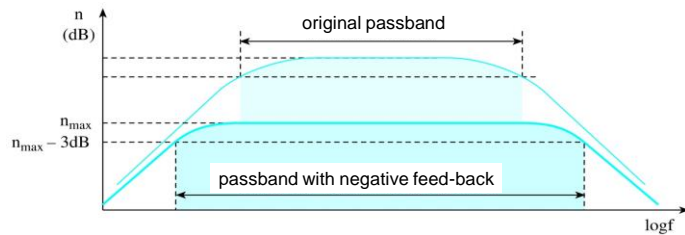


feed-back  
in the body

## Negative feed-back

The feed-backed part of the output is added to the input after inversion.

$$A_{U,NF} = \frac{U_{out}}{U_{in}} = \frac{A_U}{1 + \beta \cdot K_U}$$



## Advantage of the negative feed-back

$$A_{U,F} = \frac{U_{out}}{U_{in}} = \frac{K_U}{1 + \beta \cdot K_U} \text{ usually } \beta \cdot K_U \gg 1, \text{ so } K_{U,F} \approx \frac{K_U}{\beta \cdot K_U} = \frac{1}{\beta}$$

The properties (gain, transfer band) depend on feed-back elements only.

Consequences:

1. The parameters (gain, transfer band) are well defined.
2. Noise level decreases on the output.
3. Stability increases.

## Pozitive feed-back

The feed-backed part of the output is added to the input.

$$A_{U,PF} = \frac{U_{out}}{U_{in}} = \frac{A_U}{1 - \beta \cdot A_U}$$

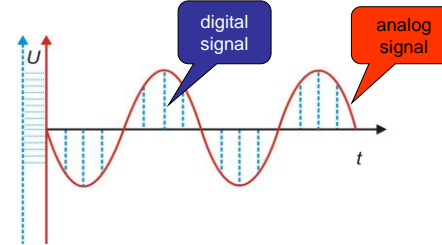
if  $\beta A_U = 1$  the system is unstable, oscillation.



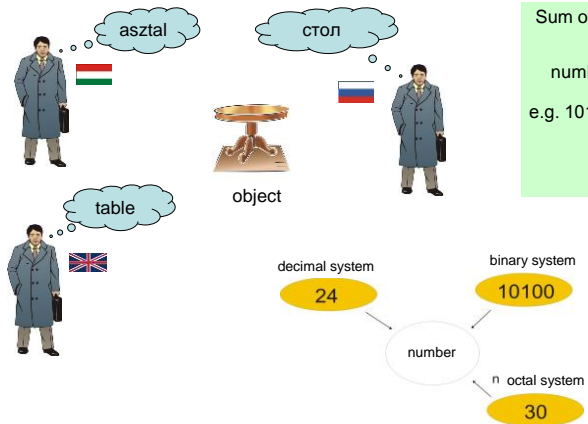
**Oscillators:** used to produce electric signal.

## Digitizing the signal

Digital signal: a signal characterized by digital value and determined at a given time periodically (sampling).



## Binary system of the numbers



Sum of the powers of 2.

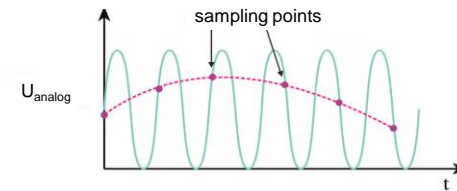
numbers: 0 and 1.

$$\begin{aligned} \text{e.g. } 101 &= 1 \cdot 2^2 \\ &+ 0 \cdot 2^1 \\ &+ 1 \cdot 2^0 \end{aligned}$$

## Shannon principle

$$f_{\text{sampling}} \geq 2 \cdot f_{\text{signal}}$$

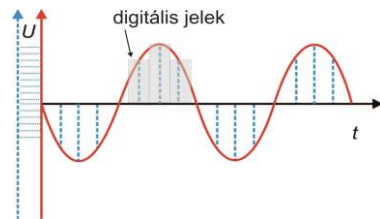
If the sampling doesn't fulfill this requirement, false frequencies appear.





## Role of the resolution

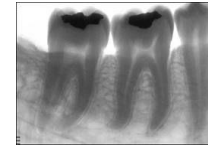
quantization noise:  
noise due to the quantization.



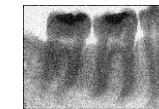
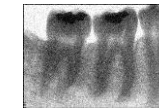
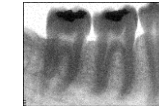
Due to the quantization series of square pulses appear. The frequency range of them is different from the original one. Higher resolution decreases this noise.

## Role of the noise level

original image



Richly detailed images,  
sufficient information.



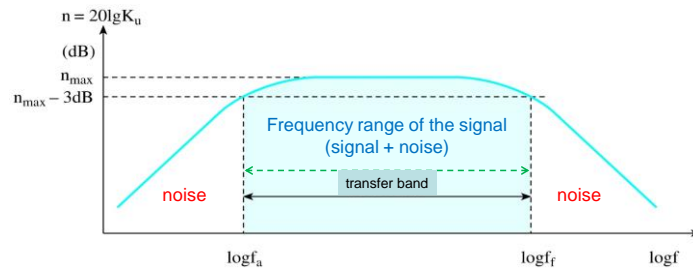
noise level

Increasing noise level  
decreases the  
information obtained  
from the image.

To decrease the noise  
level is an important  
part of the signal  
processing.

## Planning a good amplifier

Base: Noise is present in the whole frequency range.

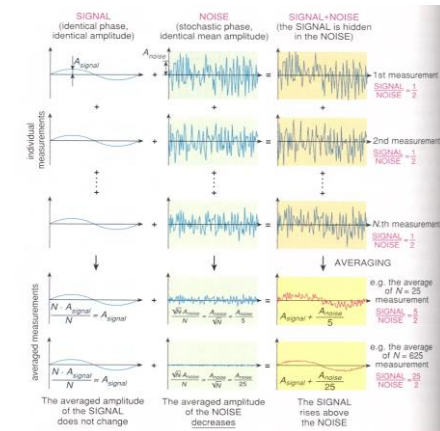


The signal to noise ratio increases  
due to the decreasing amplification out of the transfer band.

## Decreasing the noise by averaging

Base:

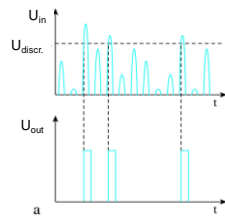
Noise is random while the  
signal is not.



## Pulse signals

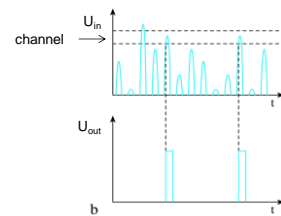
Base: The amplitude of the noise pulses is different in average.

Integral discriminator (ID)



Signal is produced only over a certain level.

Differential discriminator (DD)



Signal is produced if the amplitude is in the channel.

## Displays

CRT (not frequently used nowadays)



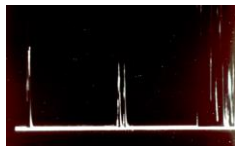
LCD

OLED



XEL-1

## Displaying a time process



Time is on the horizontal axis and amplitude of the signal is on the vertical axis.

## Information in an image

What is on the photo?

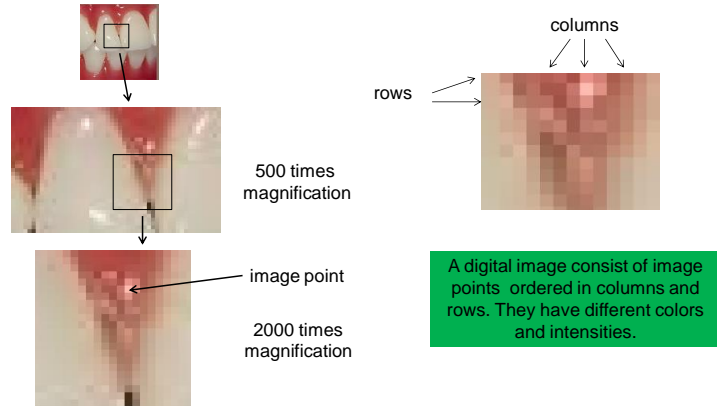
„A landscape, a beautiful garden.“



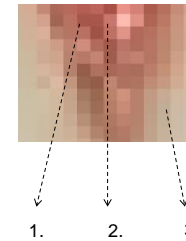
In fact:

How much is the absorption ability and the reflectivity of the different objects.

## Structure of an image



## Physical content of an image



Every image point corresponds to a small part of the body. This part normally is a square. This is a **pixel**. The pixel is considered to be homogeneous. The properties of an image point are related to some physical characteristics of the pixel.

The 1. and the 2. pixel have the same absorption ability, but the reflectivity is different.

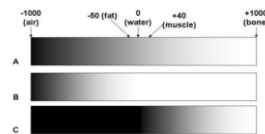
The absorption ability of the 3. pixel is different, too.

## X-ray image



What information is in this image?  
The x-ray absorption ability of the pixel is recorded in the image point.  
Practically the  $\mu$  value.

Gray scales of a CT image at different „windows“.



## 3D image

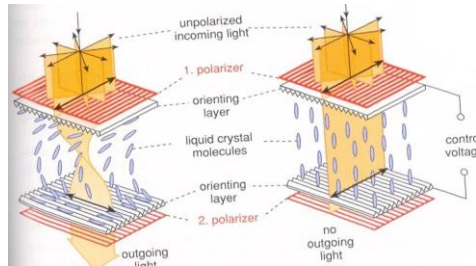


Every image point corresponds to a certain volume of the body. This volume normally a cube. this is the **voxel**.

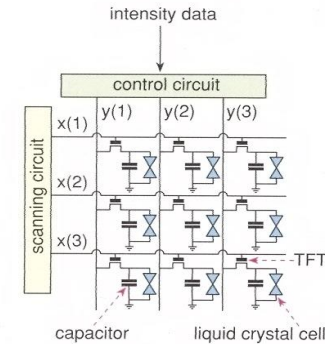
The properties of an image point are related to some physical characteristics of the voxel.

## LCD (Liquid Crystal Display)

Structure and working of a single pixel (cell)

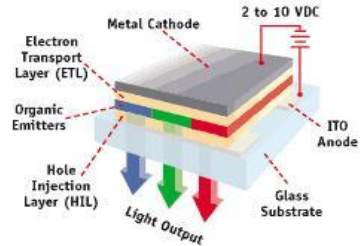


## TFT (-LCD) display



A very thin (transparent) transistor layer switches each pixel. This improves the speed.

### OLED Structure



LED: Light Emitting Diode

## O<sub>(rganic)</sub>LED displays

This is the structure of a unit cell (an image point) of the display. The recombination of the electrons and holes produces the light. The color corresponds to the energy difference of them.  
(Of course one of the electrodes must be transparent.)

## Comparison of displays

	CRT	LCD	TFT-LCD (LED)	Plasm	OLED
brightness (cd/m <sup>2</sup> )	~100	200-300	200-300	400-1000	A few 100
Contrast ratio	> 1000:1	~ 600:1	600:1 (but LED: 1000000:1)	> 1000:1	> 1000:1
Viewing angle	whole range	~140-160 degree	~140-160 degree	~160 degree	whole range
Frame rate	<1 ms	8-20 ms	<8 ms	<1 ms	<1 ms

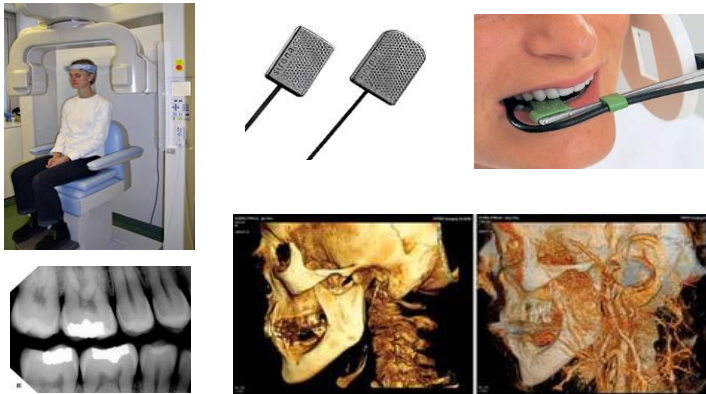
## Flexible displays



## Transparent displays



## Application of the CCD



## Unit cell of a CCD

