

Physical basis of dental material science

9.

Mechanical properties 3.

1

Materials

elastic material



force results reversible change.

elastic or viscous?



nor elastic and nor viscous.

viscoelastic material

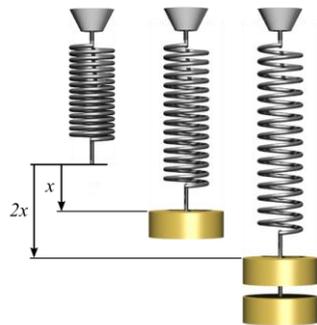
viscous material



force results flow, irreversible change.

2

Ideal elastic material



Hooke's law:

$$F = -D x$$

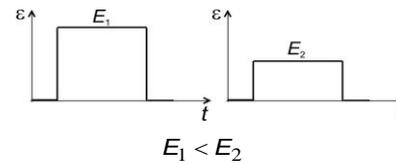
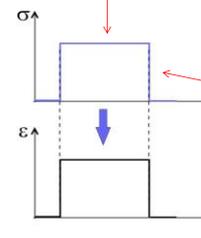
$$\sigma = E \epsilon$$

The deformation is proportional to the external force. Removing the load it recovers the original size.

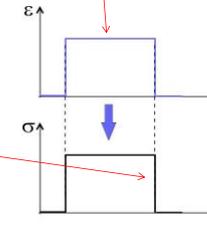
3

Ideal elastic body!

Constant force (stress)



Constant deformation



Hooke's law: $\sigma = E \epsilon$

$$\sigma_{\text{shear}} = G \gamma$$

Model:



4

Ideal viscous material



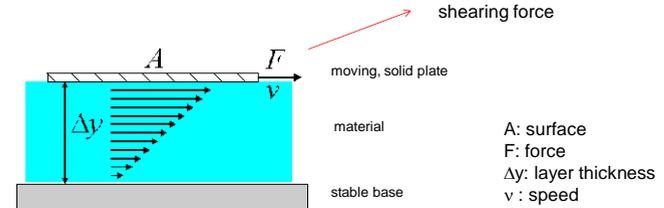
There is no any recovery.
The deformation is permanent.

Characteristic property:
Viscosity!

The measure of the resistance of a material that is deformed by either shear stress or tensile stress.

5

Viscosity (η):



The force is proportional to the speed, surface.

The resistance is due to the atomic interaction inside the material!

6

Description

Newton's friction law:

$$F_f = \eta \cdot A \cdot \frac{\Delta v}{\Delta y}$$

(rearrange)

viscosity (internal friction coefficient)

$$[\eta] = \text{Pa} \cdot \text{s}$$

velocity gradient

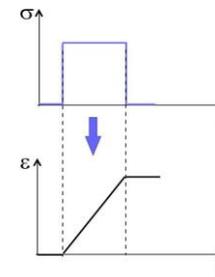
$$\frac{F_f}{A} = \eta \cdot \frac{\Delta v}{\Delta y} \quad = g \rightarrow \text{gradient}$$

$$\sigma_{\text{shear}} = \eta g_{\text{speed}}$$

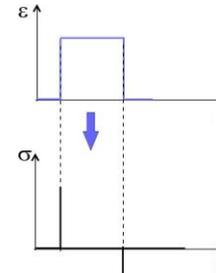
7

Ideal viscous body

Deformation in the case of constant force (stress).



Constant deformation

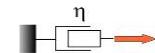


Newton's law:

$$\sigma_{\text{shear}} = \eta g_{\text{speed}}$$

Model:

Newtonian dumper,
dashpot

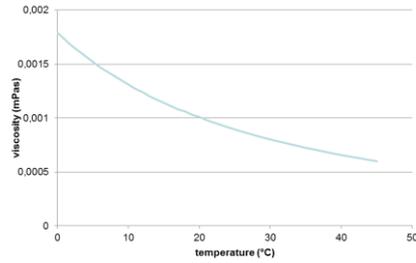


$$\eta_1 < \eta_2$$

8

Dependence on the temperature

viscosity of the water



honey in fridge or room



oil in winter and summer



Strongly depends on the temperature!

$$\eta \sim e^{-bT}$$

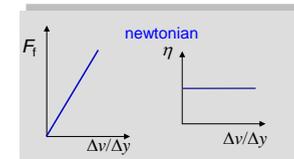
9

e.g. at 20 °C:

| material | air | water | blood (37°) | glycerine |
|----------------|-------|-------|-------------|-----------|
| η (mPa·s) | 0.019 | 1 | 2–8 | 1490 |

Normal (or newtonian) fluid:

The viscosity depends only on the temperature (independent from e.g. velocity gradient or speed of flow).



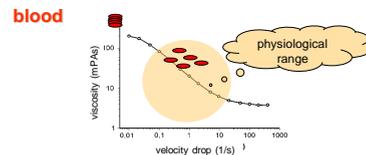
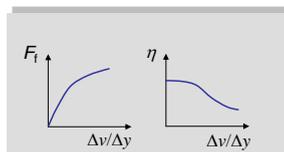
10

Anomalous (or non-newtonian) fluids:

The viscosity depends on the **velocity gradient**.

Pseudoplastic materials:

Viscosity decreases with the rate of shear.



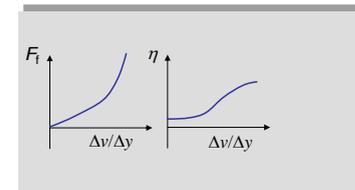
It is also a common property of polymer solutions and molten polymers.

11

Dilatant material

Viscosity increases with the rate of shear.

Walking on wet sand, a dry area appears underneath your foot.



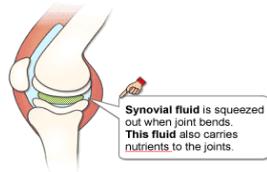
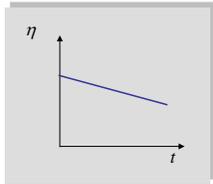
Silly Putty



12

Thixotropic material

Normally viscous, but becomes flow if stressed.

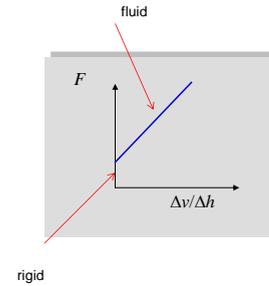


Another examples:
cytoplasm, semen.

13

Bingham-fluid (plastics)

Behaves as a rigid body at low stresses but flows as a viscous fluid at high stress.



Mayonnaise

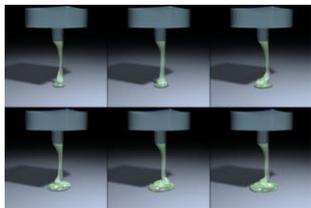


Tooth-paste

14

Viscoelasticity:

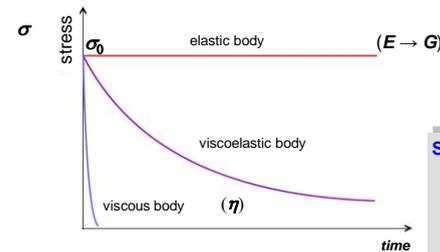
materials which exhibit both viscous and elastic characteristics when undergoing deformation.



15

Viscoelasticity:

After instant deformation:



Hooke's law

$$\sigma = E\varepsilon$$

$$\sigma_{\text{shear}} = G\gamma$$



Stress relaxation:

$$\sigma = \sigma_0 e^{-\frac{t}{t_{\text{rel}}}}$$

$$t_{\text{rel}} = \frac{\eta}{G}$$

relaxation time

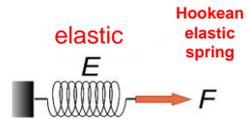
Newton's law

$$\sigma_{\text{shear}} = \eta g_{\text{speed}}$$

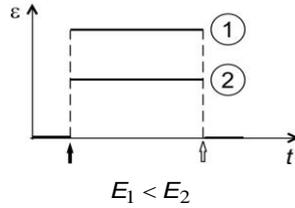
16

Changing deformation in the case of constant force

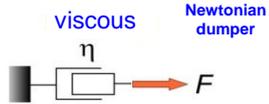
Base models:



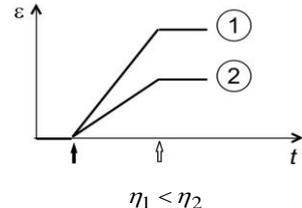
Hookean elastic spring



$E_1 < E_2$

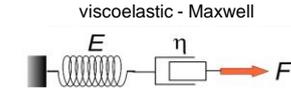
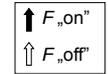


Newtonian dumper



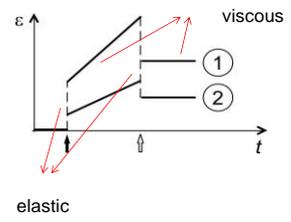
$\eta_1 < \eta_2$

Viscoelastic materials



viscoelastic - Maxwell

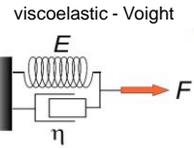
2 different material



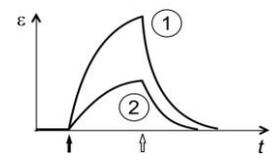
$E_1 < E_2$
 $\eta_1 < \eta_2$

Viscoelastic materials

$E_1 < E_2$
 $\eta_1 < \eta_2$

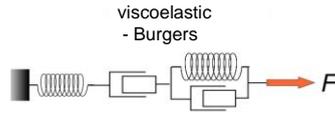


viscoelastic - Voigt

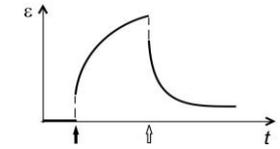


Viscoelastic materials

$E_1 < E_2$
 $\eta_1 < \eta_2$



viscoelastic - Burgers



Long-term phenomena

Change in:

shape:
 → slow increase: **creep**
 → slow decrease: **shape recovery**

integrity:
 → fracture: **fatigue**
 → surface: **abrasion**

stress: → slow decrease: **stress relaxation**

21

Creep



This is the slow change in the dimensions of a material due to prolonged stress.

Time interval

Stress is below the yield strength!

Definition

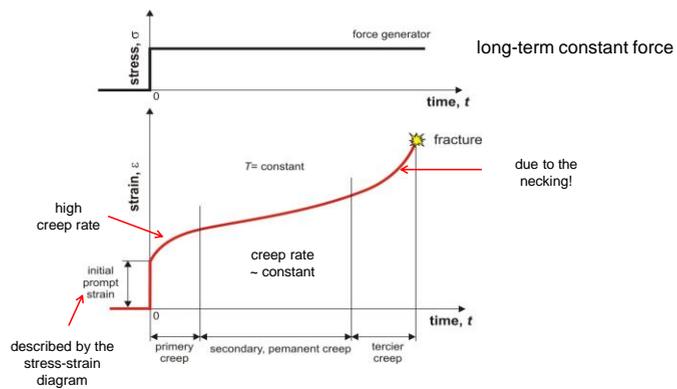
creep rate: deformation during unit time.



1-10⁷ s !!

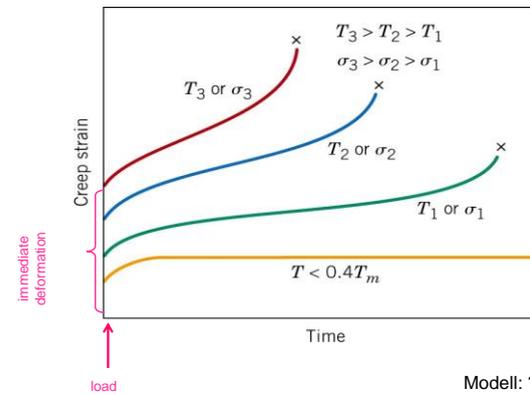
22

Creep components



23

Effect of the stress and the temperature



temperature!
 e.g. metals
 $0.4T_m < T$
 T_m : melting point

Modell: ? - []

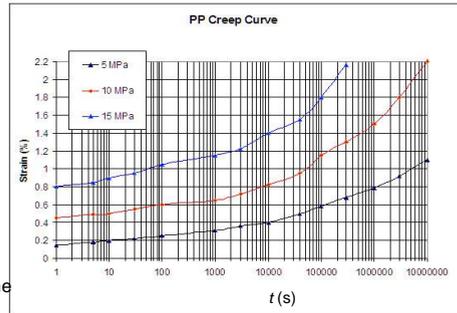
24

Effect of the stress

Polipropilene (PP)

creep rate:

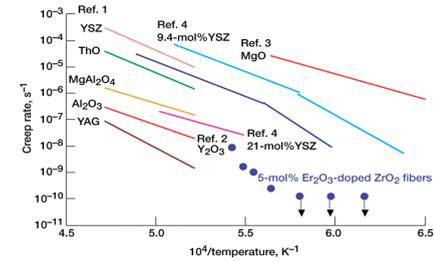
deformation during unit time



25

Effect of the temperature

ceramics

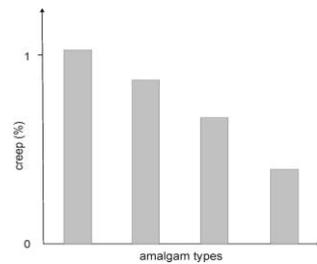


26

Example: amalgam

Creep influences the marginal integrity of the filling.

melting point: 100 – 180 °C!



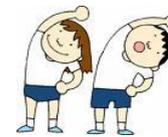
Increasing silver or copper content decreases the creep.

27

Relaxation

shape recovery

recovery when the load stops.

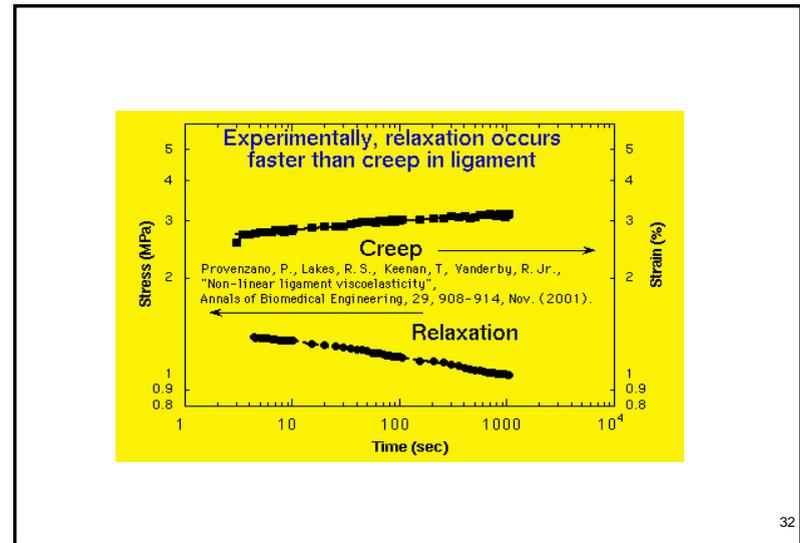
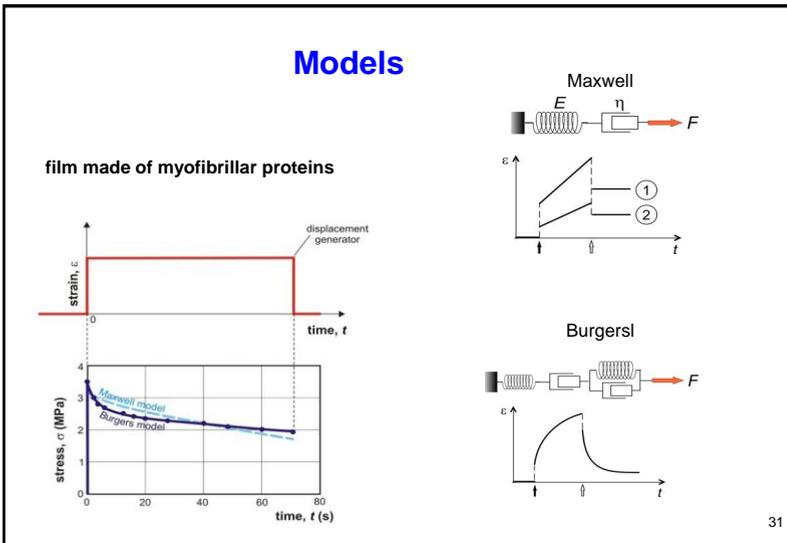
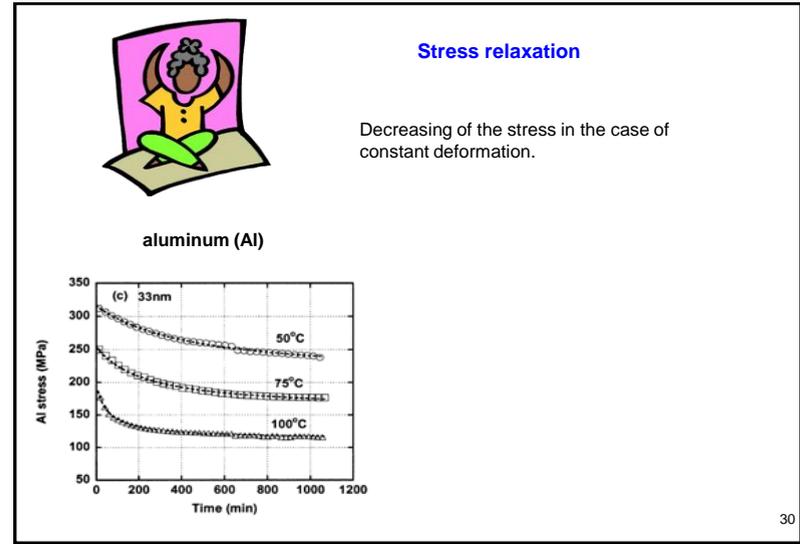
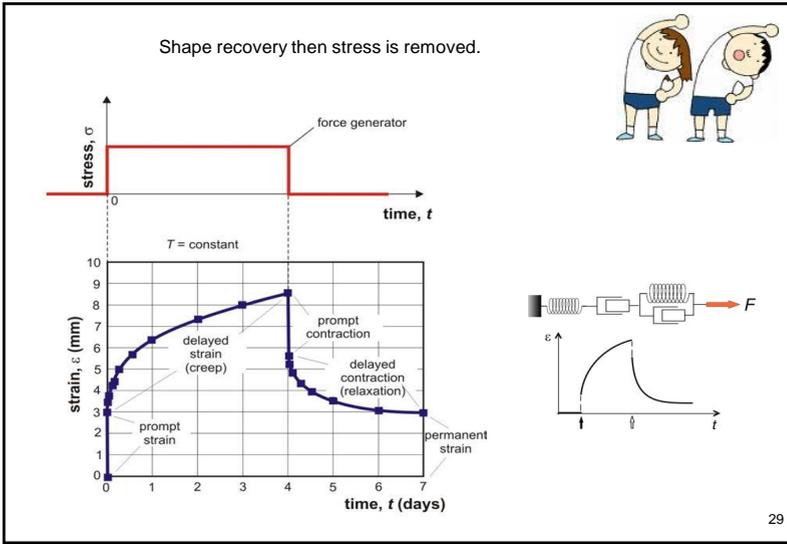


stress relaxation

decrease of the stress at constant deformation .



28



Fatigue

This is the progressive and localized structural damage that occurs when a material is subjected to cyclic loading.

Stress is below the strength!
There is no immediate fracture.



Fatigue is a **stochastic process**.

Damage is cumulative.

Fatigue is usually associated with tensile stresses.

Long, repeated load

→ structural changes

→ strength decreases

↓
cracks!

Short-term strength > long-term strength.

33

Type of loads

Static fatigue:

Long-term stress results decrease in strength finally fracture.

A test equipment

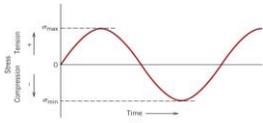


testing a dental implants



34

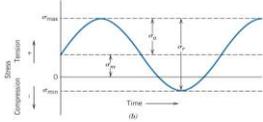
Type of loads



symmetric

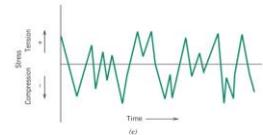
Dynamic fatigue

Dynamically changing force.



asymmetric

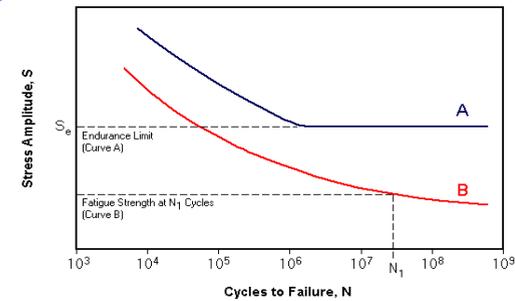
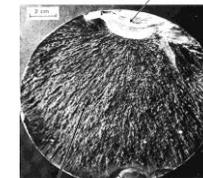
Asymmetric tension and compression behavior of materials due to the asymmetric atomic forces.



random

35

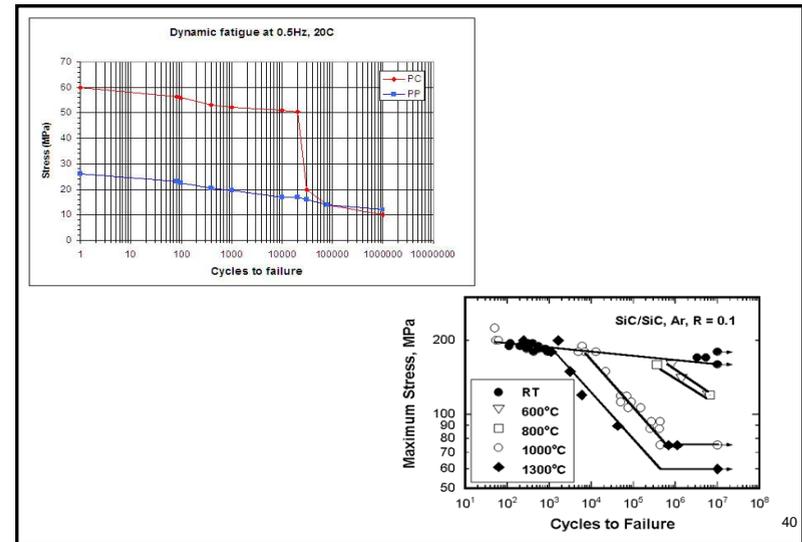
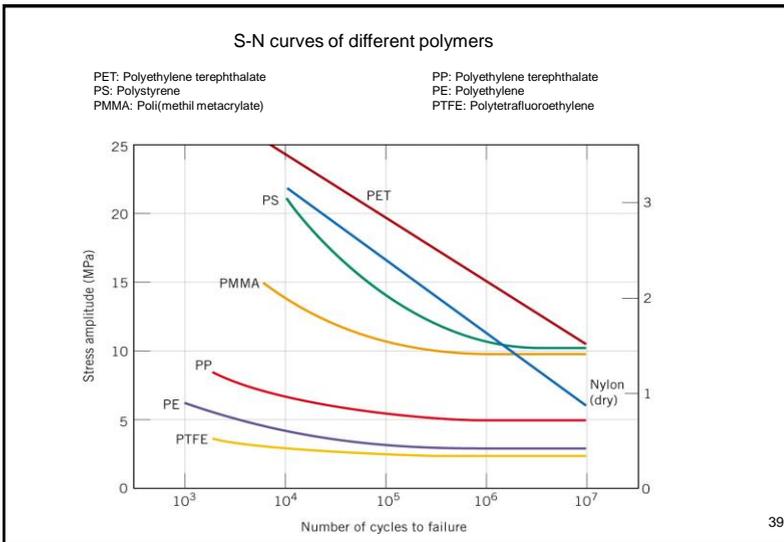
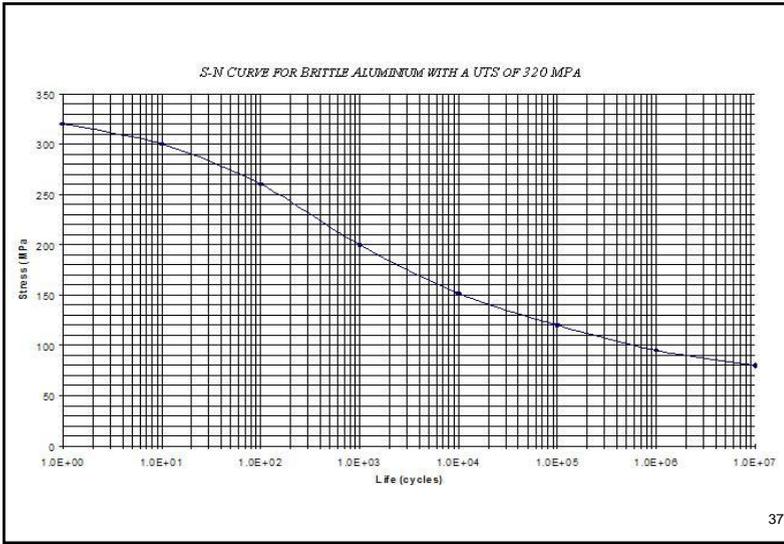
Fatigue S-N curve:



e.g. steel, titanium, ...

e.g. aluminium, copper, ...

36



Some factors

Geometry: Notches and variation in cross section.

Surface quality: Surface roughness.

Material type: E.g. composites and polymers differ markedly from metals.

Grain size: For most metals, smaller grains yield longer fatigue lives.

Temperature: Extreme high or low temperatures can decrease fatigue strength.

Prevention: E.g. stress should be below threshold of fatigue limit.

41

Abrasion



Loss of the structure by **mechanical forces**.

E.g.: toothbrush abrasion causes V-shaped notches

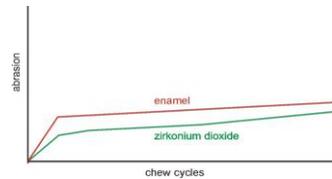
(Erosion a chemical event!)

42

Role of hardness

Most commonly affected: premolars and canines.
(position)

Cementoenamel junction
(very thin enamel)
is very sensitive.



| material | HV (MPa) | HK (MPa) |
|----------|----------|-----------|
| Enamel | ≈ 3400 | 3400-4000 |
| Dentin | ≈ 600 | ≈ 700 |
| Amalgam | ≈ 1000 | |

(cementum a little bit less hard than the dentine.)

43