

## Interaction between living organism and the environment

Open system: free material and energy exchange.

## Properties of the living organism

**Separation from the  
enviroment:**

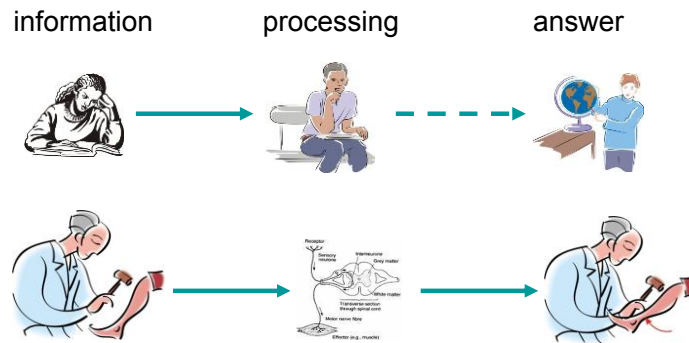
Strictly controlled  
energy and material transport.

**Changing in the  
enviroment:  
accomodation**



Condition: information from the environment, right and fast processing and adequate response.

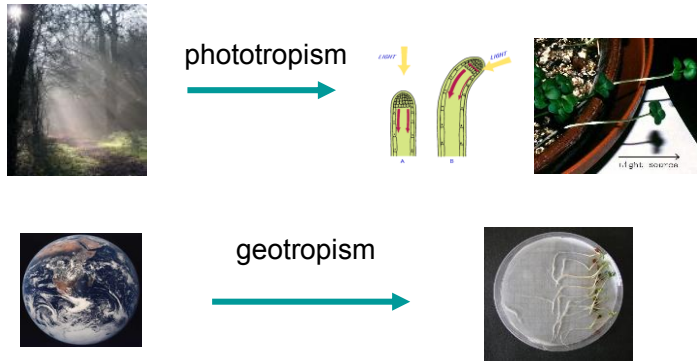
## Processing informations



## Definitions

- **stimulus**: any effects on the organism (signal and noise)
- **outer stimulus** from the enviroment (e.g. light, sound etc.)
- **inner stimulus**: from the organism (glucose concentration, pH of the blood etc.)

## Simple responses in plants

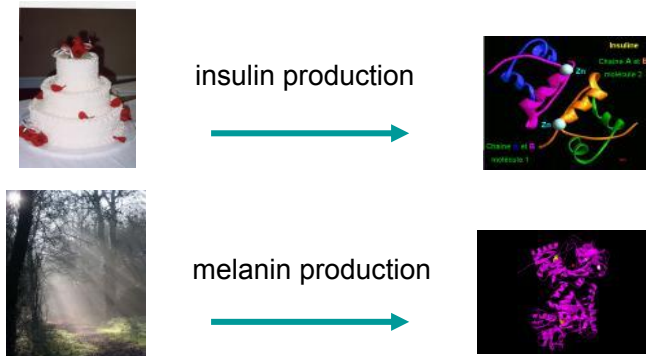


## „Fast” motion in plants



Sensitive plant

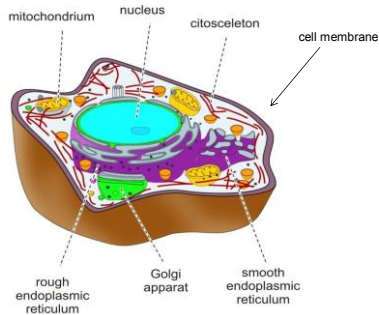
## Simple responses in animals



## Animals and the human beings

- Motion (requires fast processes)
- Chemical system : hormones
- More complex and faster system: nerves and muscles

## Membranes in the cell



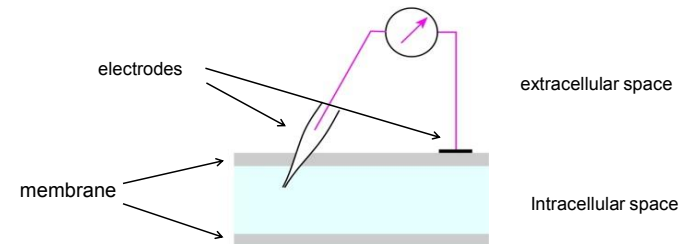
Role of the cell membrane:  
separation and controlled  
interaction to the environment

Inner membranes:  
formation of intracellular spaces  
(compartments). Several basic  
processes take place on the  
membrane.

## Resting membrane potential

### observation

In resting state about  
-30 és -90 mV voltage may be  
measured between the extra-  
and intracellular space.



## Typical ion distributions

### observation

The ion concentrations are different on  
the two sides of the membrane.

#### Intracellular space (mM/l)

	Na <sup>+</sup>	K <sup>+</sup>	Cl <sup>-</sup>
Squid giant axon	72	345	61
Frog muscle	20	139	3.8
Rat muscle	12	180	3.8

#### Extracellular space(mM/l)

	Na <sup>+</sup>	K <sup>+</sup>	Cl <sup>-</sup>
Squid giant axon	455	10	540
Frog muscle	120	2.5	120
Rat muscle	150	4.5	110

## Diffusion of the ions

Diffusion of neutral particles.

Intensive quantity: chemical potential

In the case of charged particles the electric  
work must be taken into the consideration!

Intensive quantity: electrochemical potential

z: no. of charges  
F: Faraday constant.  
 $\varphi$ : electric potential

$$\mu^e = \mu + zF\varphi$$

equilibrium:

$$\mu_1^e = \mu_2^e$$

Nernst-equation

$$\Delta\varphi = -\frac{RT}{zF} \ln \frac{c_1}{c_2}$$

## Diffusion through the membrane

Use the permeability constant as characteristic quantity!

$$p = D/d$$

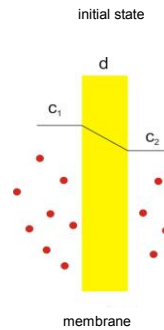
D – diffusion constant  
d – thickness of the membrane

mobile ions (permeable membrane), final state equilibrium.

**equilibrium:**

$$c(1) = c(2)$$

$$\Delta\phi = 0 !!!$$



## Donnan-equilibrium

Initial conditions:

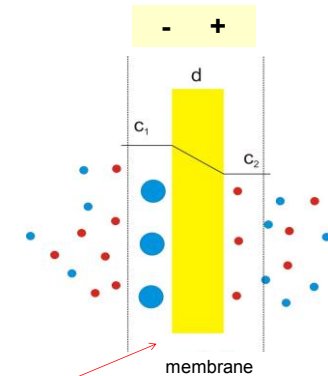
There are non permeable ions. Electric neutrality both sides (the sum of charges is zero)

$$c(1) \neq c(2)$$

$$\Delta\phi \neq 0$$

Right solution?

electric bilayer



## Ratio of concentrations (extracell./intracell.)

Ion	Na <sup>+</sup>	K <sup>+</sup>	Cl <sup>-</sup>
squid	6.3	0.029	8.9
frog	6.0	0.018	31.6
rat	12.5	0.025	29.0

## Calculated potentials on the basis of Nernst-equation for different ions and the measured potential (mV)

	membrane-potential (meas.)	Na <sup>+</sup>	K <sup>+</sup>	Cl <sup>-</sup>
Squid giant axon	-62	+46	-89	-55
Frog muscle	-92	+45	-101	-87
Rat muscle	-92	+64	-93	-85

**Significant differences** between the measured and calculated values!  
Main difference in the case of Na<sup>+</sup>.

### ***Typical values for the heart***

ion	Extracell. space (mM)	Intracell. space (mM)	ratio (extra/intra)
Na <sup>+</sup>	145	15	9.7
K <sup>+</sup>	4	150	0.027
Cl <sup>-</sup>	120	5-30	4-24
Ca <sup>2+</sup>	2	10 <sup>-7</sup>	2·10 <sup>4</sup>

### ***Calculated membrane potential***

ion	Na <sup>+</sup>	K <sup>+</sup>	Cl <sup>-</sup>	Ca <sup>2+</sup>
Membrane potential (mV)	61	-96	-(37-85)	

### ***Donnan-equilibrium***

- In the case of the phenomenon described by Donnan constant potential difference may be observed between two sides of the membrane.
- There are mobile and immobile ions.
- In the case of equilibrium the electrochemical potential is same.

### ***Conclusion***

On the basis of the measured values there is no Donnan-equilibrium between two sides of the membrane. (The concentration difference of the Na<sup>+</sup> is too high for example!)

- The biological system is not in equilibrium!
- Passive process (diffusion) may change the state to the equilibrium.
- Active (energy consumption) processes are necessary to keep steady state.

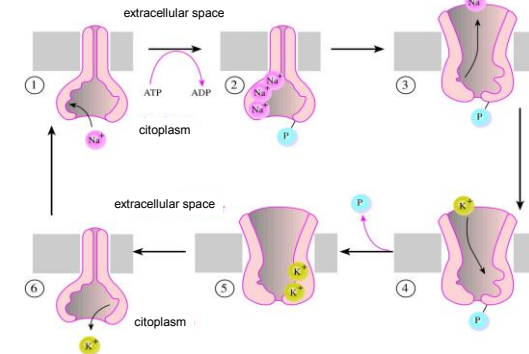
## The role of active transport

- Charge and material transport exist, the concentration were not constant, e.g. slow inflow of  $\text{Na}^+$  into the cell.
- Different, energy consumer mechanisms, so-called pumps ensure the steady state.
- (e.g.  $\text{Na}^+$ - $\text{K}^+$  pump,  $\text{Na}^+$ - $\text{Ca}^{++}$  etc.)

## Na-K pump

3  $\text{Na}^+$  ion and 2  $\text{K}^+$  exchange

requires ATP!



## Ion flow in the membrane

neutral particles



$$J = -p \cdot \Delta c$$

$J$  – flux  
 $p$  – permeability constant  
 $\Delta c$  – concentration gradient

(single) charged particles



$$J = -p \left( \Delta c + c \frac{F}{RT} \Delta \phi \right)$$

$J$  – flux  
 $p$  – permeability constant  
 $\Delta c$  – concentration gradient  
 $F$  – Faraday constant  
 $T$  – temperature  
 $\Delta \phi$  – potential difference  
 $R$  – gas constant

## The basis of the transport-model

- The membrane is in rest but there is no equilibrium between two sides.
- The membrane potential is constant  $\Rightarrow$  the net ion flow through the membrane is zero.
- The potential gradient in the membrane is constant  $\Rightarrow d\phi/dx = \text{const.}$

## Goldman-Hodgkin-Katz (GHK) potential equation

condition of steady state:  
(the net flux is zero)

$$\sum_k J_k = 0$$

$$\Delta\varphi = -\frac{RT}{F} \ln \frac{p_{Na}c_{Na}^e + p_Kc_K^e + p_{Cl}c_{Cl}^i}{p_{Na}c_{Na}^i + p_Kc_K^i + p_{Cl}c_{Cl}^e}$$

p – permeability constant of an ion  
e – extracellular space  
i – intracellular space

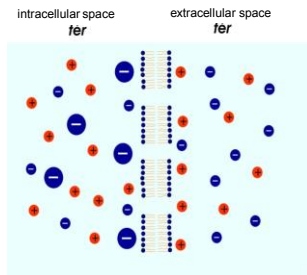
## Simplified GHK equation

$$\varphi = -\frac{RT}{F} \ln \frac{pc_{Na}^e + c_K^e}{pc_{Na}^i + c_K^i}$$

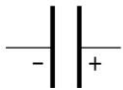
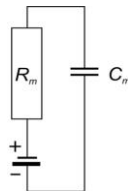
(p = relative permeability constant, compared to the K<sup>+</sup>)

	p	φ(calc.) (mV)	φ(meas.) (mV)
Squid giant axon	0,04	-63	-62
Frog muscle	0,01	-91	-92

## Electric model of the membrane

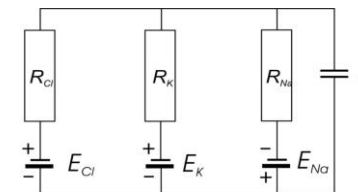


The model describing the resting potential and the ion current:



## According to the main ions

model for resting potential

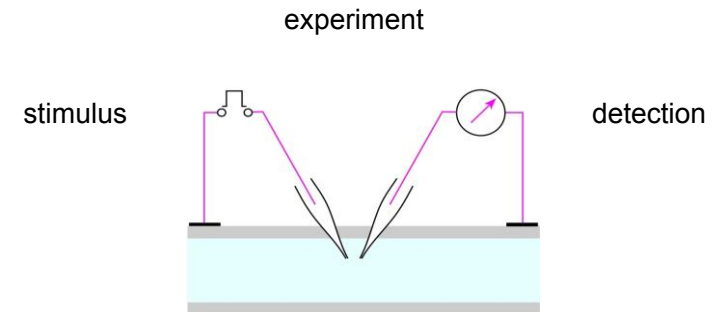


C – represents the membrane capacity,  
R – characterizes the resistance against the flow of the given ion,  
E – voltage source representing the membrane potential

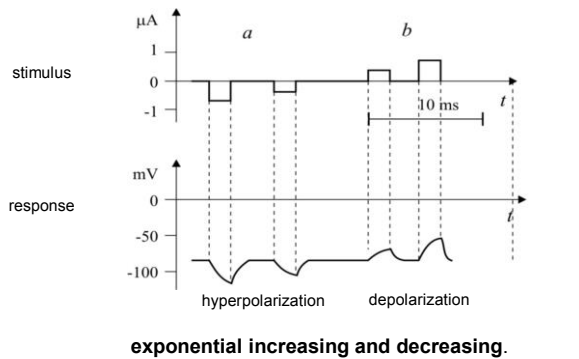
## Changing of the membrane potential

- The definition of the stimulus:  
changing of the membrane potential transmits the information.
- Changing of the resting potential is due to the specific ion flow through the membrane.

## Changing the membrane potential

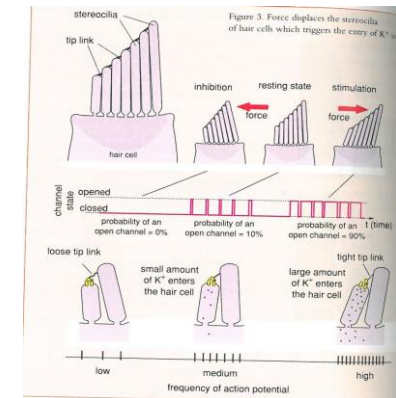


## Depolarization, hyperpolarization



## Depolarization (example)

hair cells in the ear:  
Mechanical effect - membrane depolarization.



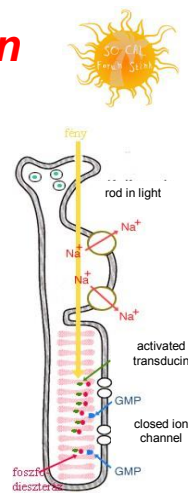
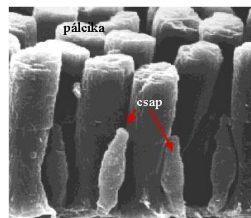
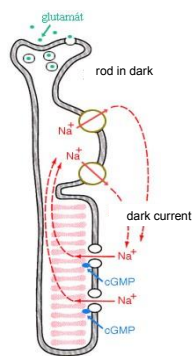


## Hyperpolarization

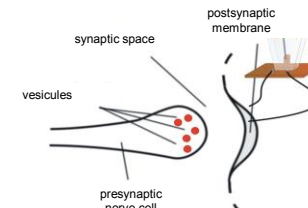
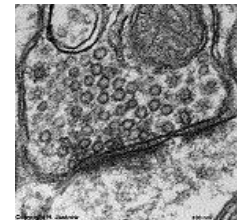


rods in the eye:

photochemical effect results the hyperpolarization of the membrane.

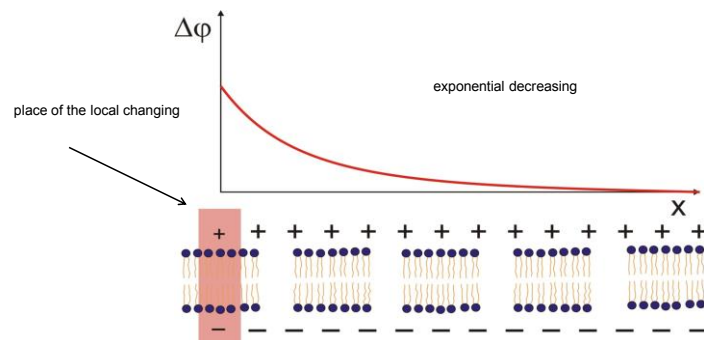


## Synapse (example)

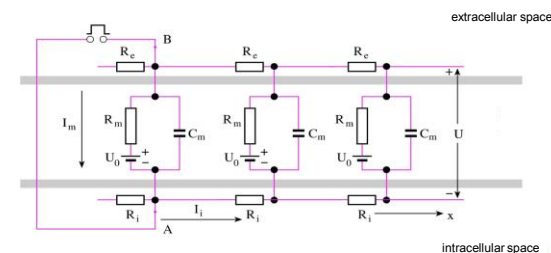


A possible mechanism: the released acetyl choline bonding to the receptor opens an ion-channel.

## Propagation of the changing along the membrane



## Extension of the electric model: cable model



$R_e$  - longitudinal resistance of the extracellular space.  
 $R_i$  - longitudinal resistance of the intracellular space.  
 These elements connect to each other the different parts of the membrane.

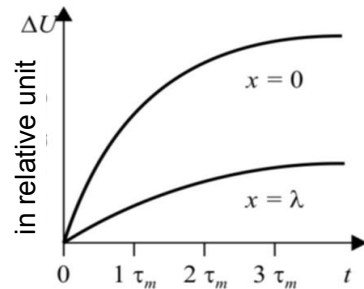
## Electric properties: time constant

on the basis of the exponential answer of the membrane:

(responses according to the distance of the place of the stimulus)

$$\tau_m = R_m \cdot C_m$$

the time, while the changing decreases or increases by factor e.



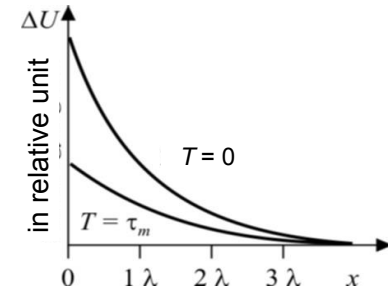
## Electric properties: space constant

on the basis of the propagation of the changing along the membrane:

(responses according to the time)

$$\lambda \approx \sqrt{\frac{R_m}{R_i + R_e}} \approx \sqrt{\frac{R_m}{R_i}}$$

the distance, where the changing decreases by factor e.



$$R_i \gg R_e$$

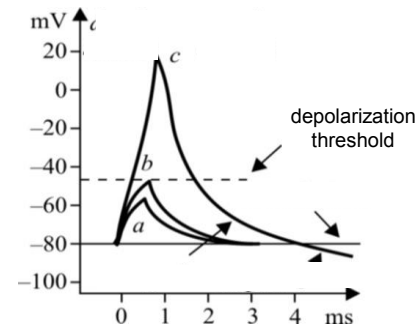
## Propagation of the depolarization

	$\rho_m$ ( $\Omega \text{ cm}^2$ )	$\rho_i$ ( $\Omega \text{ cm}^2$ )	$\tau$ (ms)	diameter ( $\mu\text{m}$ )	$\lambda$ (cm)
Squid nerve	700	30	0,7	500	0,5
Crawfish nerve	2000	22	5	30	0,25
Frog muscle	4000	87	24	75	0,2

Both the time constant and the space constant depend on the diameter.

The value of the space constant shows that these are **local phenomena** they are not able to propagate too far.

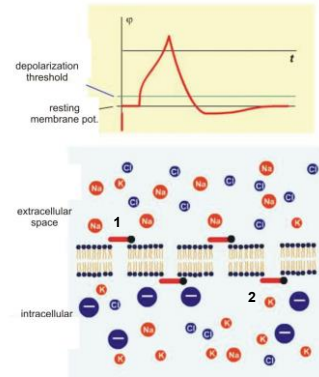
## Processes in nerves and muscles



- a – depolarization below the threshold (local response)
- b – depolarization below the threshold (local response)
- c – depolarization above the threshold - action potential

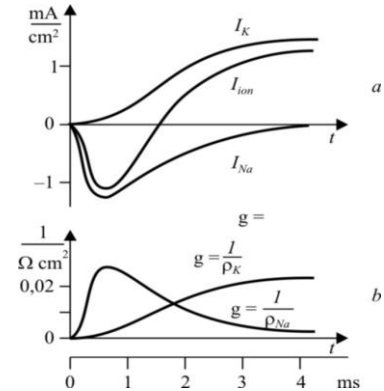
## Action potential

- 1 – voltage sensitive Na<sup>+</sup>-channels
- 2 - voltage sensitive K<sup>+</sup>-channels



## Ion flow during action potential

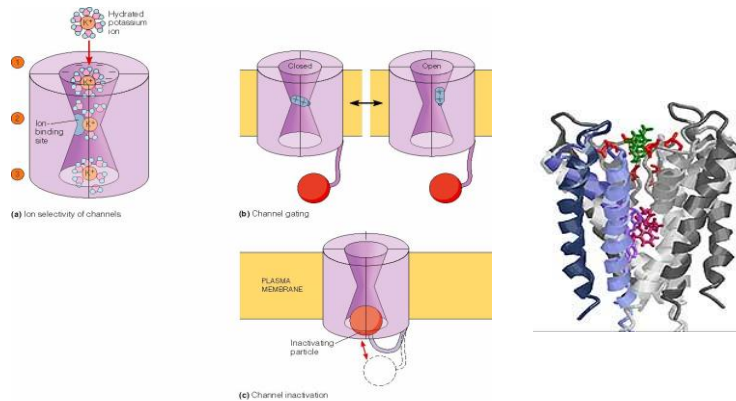
the inflow of the Na<sup>+</sup> is fast at the beginning according to the non-equilibrium state.



$$g = (1/\rho)$$

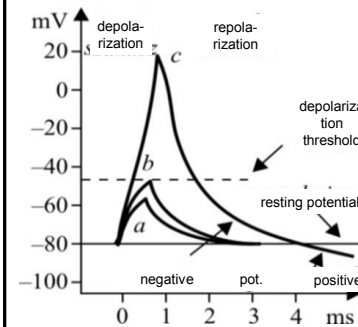
conductivity

## K<sup>+</sup> channel



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## Properties of the action potential



The first step is fast!  
(slow, long process is not suitable for fast response.)

## Why is it fast?

ratio of ion concentration  
(extra/intracellular space)

ion	Na <sup>+</sup>	K <sup>+</sup>	$\Delta U$ (mV)
Squid	6.3	0.029	-62
Frog	6.0	0,018	-92
rat	12.5	0.025	-92

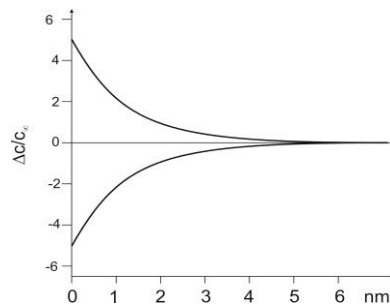
## Simple calculation

- Let the radius of a cell 20  $\mu\text{m}$ !
- The volume is:  $\sim 3 \cdot 10^{-11} \text{ l}$ .
- amount of the K<sup>+</sup> :  $\sim 6 \cdot 10^{-12} \text{ mol}$ .
- surface of the cell:  $\sim 5 \cdot 10^{-5} \text{ cm}^2$ .
- capacity of the membrane:  $\sim 5 \cdot 10^{-5} \mu\text{F}$ .  
(specific capacity:  $\sim 1 \mu\text{F/cm}^2$ )
- on the basis of resting potential:  
 $\sim 5 \cdot 10^{-12} \text{ C} \Rightarrow \sim 5 \cdot 10^{-17} \text{ mol ion}$ .

The changing affects only the small environment of the membrane and transports a small amount of ions.

## Debye-length and diffusion

the ion concentration close to  
the membrane



Speed of the  
diffusion

$$d = \sqrt{3Dt}$$

example:

$$D \sim 10^{-9} \text{ m}^2/\text{s}, t = 0,1 \text{ ms}$$

$$d \sim 100\text{-}200 \text{ nm}$$

(Compare d, the average  
distance, to the Debye  
length!)

The diffusion transports  
the ions far from the  
membrane.

## Electrochemical potential (rat muscle)

$$\Delta\mu^e = -RT \ln \frac{c_2}{c_1} + zF\Delta\phi$$

$$\text{Na}^+ \quad \Delta\mu_{\text{Na}}^e = -8.31 \times 310 \times \ln 12.5 + 96500 \cdot (-0.092) \quad \sim -15.4 \text{ kJ/mol}$$

$$\text{K}^+ \quad \Delta\mu_{\text{K}}^e = -8.31 \times 310 \times \ln 0.025 + 96500 \cdot (-0.092) \quad \sim -0.625 \text{ kJ/mol}$$

In rest there is a large thermodynamic force for  
Na<sup>+</sup>!

$$\text{K}^+ \quad \Delta\mu_{\text{K}}^e = -8.31 \cdot 310 \cdot \ln 0.025 + 96500 \cdot (+0.02) \quad \sim -11.4 \text{ kJ/mol}$$

After reversing the polarity this force is high for K<sup>+</sup>!

## Comparison

### membrane

Large force acts on  $\text{Na}^+$  ions. Fast passive inflow.

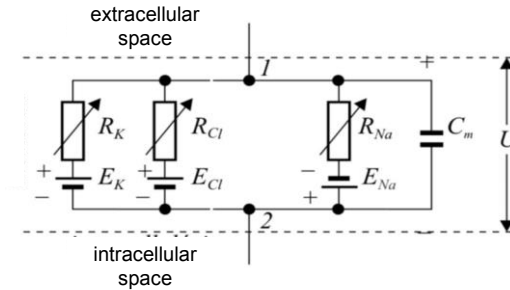
No energy consumption.

Changing of the membrane potential result the outflow of the  $\text{K}^+$ .

If were equilibrium.  
(Donnan-equilibrium)

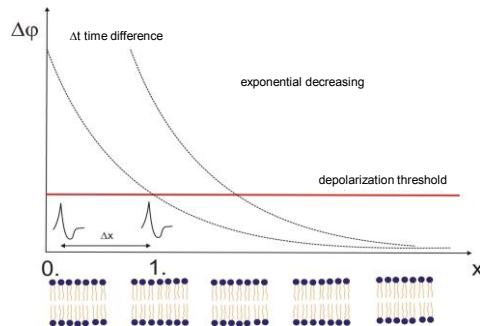
Changing of the membrane potential: requires energy and was slower!

## Modified electric model



The transmembrane resistance is represented by variable resistors, that makes possible changing the speed of the ion flow.

## Propagation of the action potential (AP)



at  $\Delta x$  the local changing is enough large to produce a new ap.

speed  $\sim \Delta x / \Delta t$

## Advantage

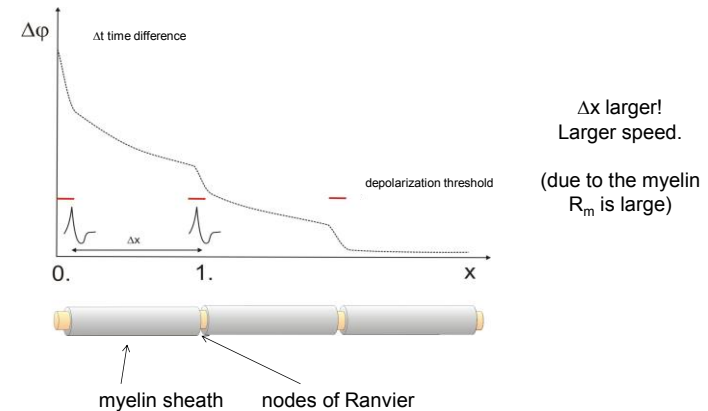
- Shape is independent from the stimulus: not sensitive to the external effects, noises.
- It propagates far without any attenuation.
- Such fast process makes possible fast responses.

## Speed of the propagation

space constant depends on:  
diameter,  $R_m$ ,  $R_i$

	$\rho_m$ ( $\Omega \text{ cm}^2$ )	$\tau$ (ms)	diameter ( $\mu\text{m}$ )	$\lambda$ (cm)
Squid	700	0.7	500	0.5
Crawfish	2000	5	30	0.25
frog	4000	24	75	0.2

## Saltatory propagation



## Role of the myelin sheath

$R_m$  very large, space constant is large too

At the nodes of Ranvier:

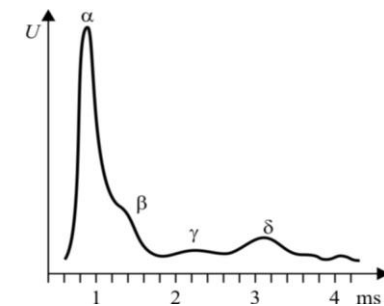
$R_m \sim 50 \Omega \text{ cm}^2$   
about  $10^4 \text{ Na}^+$ -channel/ $\mu\text{m}$

## Speed

large space constant: about 10-20 m/s

cat  
n. saphaneus

the time that is  
necessary to cover  
6 cm



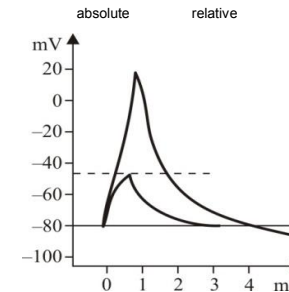
## Speed of the propagation

fiber	diameter (μm)	Speed (m/s)
α	15	70-120
β	8	30-70
γ	5	15-30
δ	<3	12-30
No sheath	<1	0.5-2

$$\lambda \approx \sqrt{\frac{R_m}{R_i + R_e}} \approx \sqrt{\frac{R_m}{R_i}}$$

increasing diameter  
– increasing  $R_m$  and  
decreasing  $R_i$ .

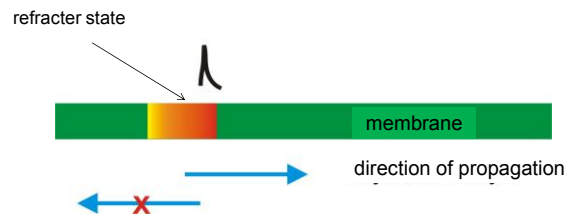
## Refractor state



absolute: Na-channels are opened, there is no new AP.

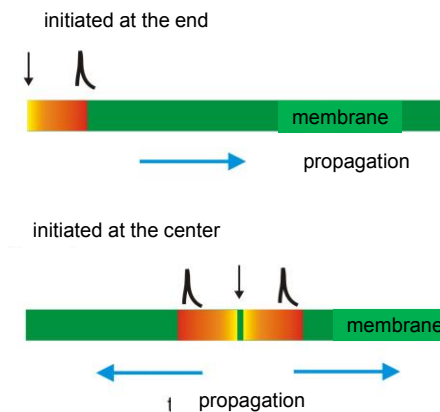
relative: only larger stimulus is able to produce new AP.

## Role of the refractor state

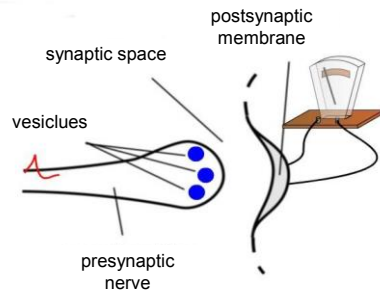


the refractor state prevents the back propagation of the ap.

## When is it not true



## Rectification: synapse



neuro-transmitters emitted by the vesicles depolarize the postsynaptic membrane and result action potential after the synapse. The structure makes impossible the back propagation.

Unidirectional step!

## Not a withdrawal?

remember: speed of the diffusion

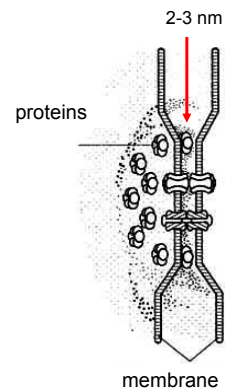
$$d = \sqrt{3Dt}$$

the size of the synaptic space is about a few 10 nm!

the diffusion is very fast if the distance is small!

the delay is not more than a few hundred  $\mu$ s!

## Electric synapse



bidirectional, no rectification.

More characteristics for the invertebrates.

man: e.g. heart muscle.

## Conclusion

Developed a fast system based on electric phenomena of the membrane.

The charges are ions, so this system is slower than equipment s used by us.

The stimulus (signal) is able to propagate far without any attenuation.



## Electric signals on the body surface

Diagnostics

Source

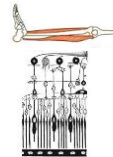
Electrocardiography (ECG)



Electroencephalography (EEG)



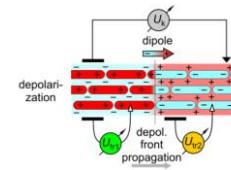
Electromyography (EMG)



Electroretinography(ERG)



## Genesis



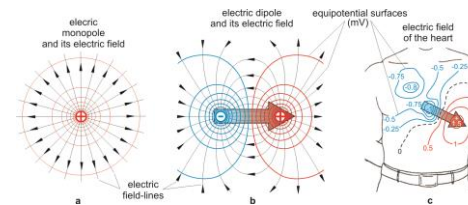
dipole moment:

$$\mathbf{d} = q\mathbf{l}$$

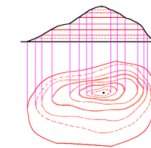
(vector quantity)

$q$  – charge  
 $l$  – distance between charges  
 $\mathbf{d}$  – dipole moment

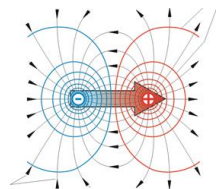
Elementary dipole moments are summed.



analogy:  
geographic map



## Measurement and its problems



electrodes

potential difference  
= voltage

### Problems:

- Source is an extended, 3D object.
- Measured on the body surface.
  - Noise.