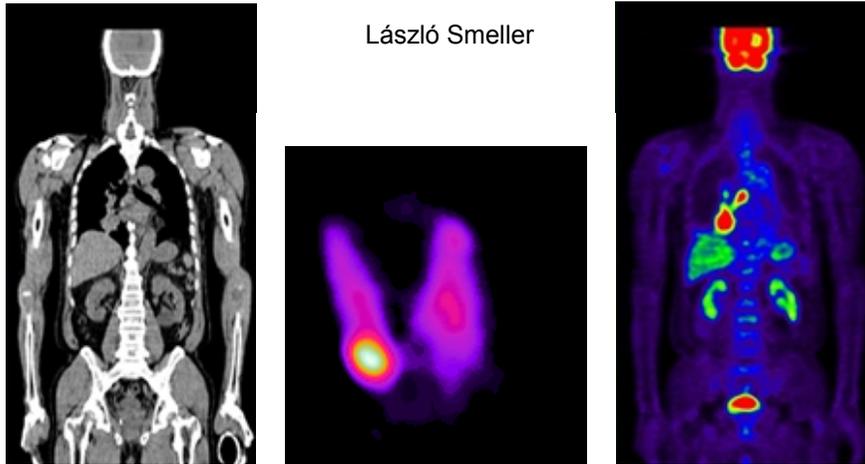
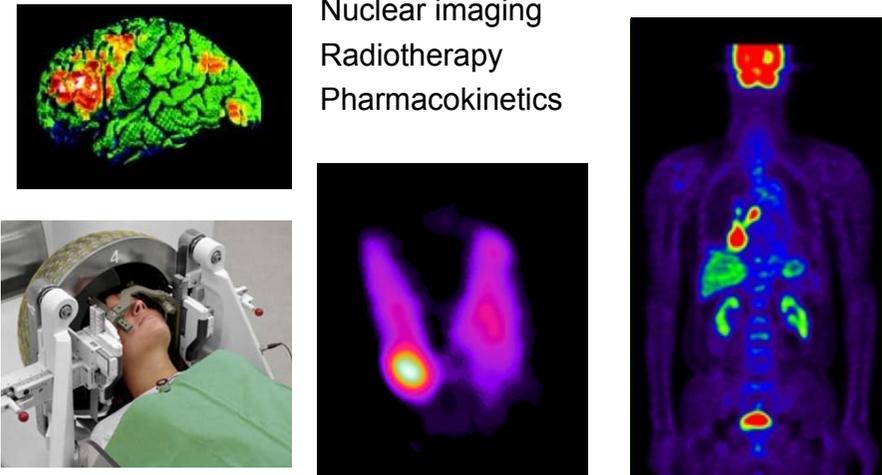


# The atomic nucleus. Radioactivity. Nuclear radiations



# Why?

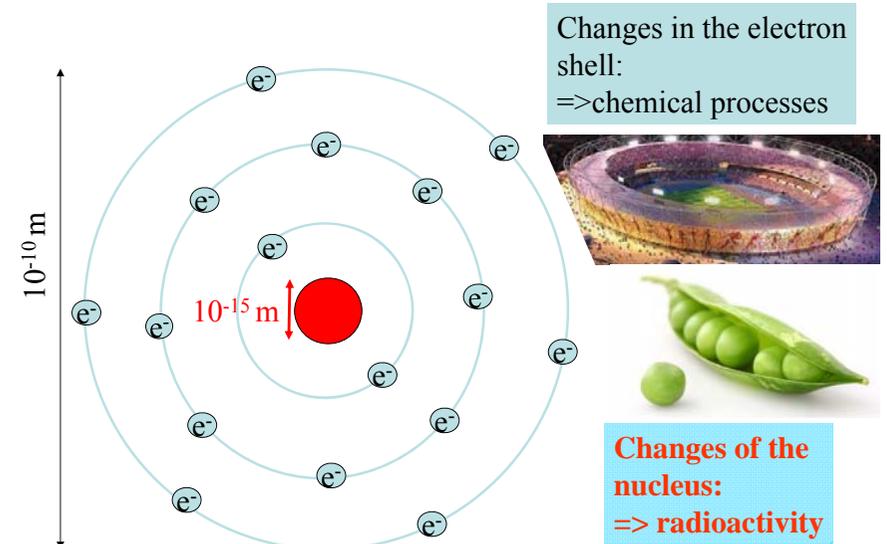
Medical/pharmaceutical applications of nuclear radiation:



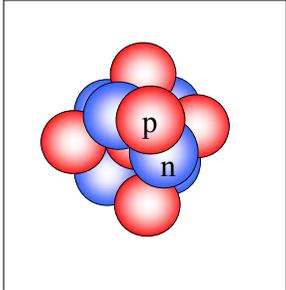
## Length scale of the nature

m		
$10^0$	meter	men
$10^{-3}$	millimeter	letters you can read
$10^{-6}$	micrometer	size of a cell (e.g. erythrocyte) $\varnothing 7\mu\text{m}$
$10^{-9}$	nanometer	protein
$10^{-10}$	- angstrom	diameter of an atom, bond length H atom $\varnothing \approx 1$ angstrom (Å)
$10^{-12}$	picometer	wavelength of the X-ray
$10^{-15}$	femtometer	size of the nucleus

## The electrons and the nucleus



# Structure of the nucleus



Elementary charge =  $1,6 \cdot 10^{-19} \text{ C}$

	charge	mass
proton	+1 e	1 atomic mass unit
neutron	0	1 atomic mass unit

A (mass number) = number of protons + number of neutrons } → 99  
 Z (atomic number) = number of protons } → 43 **Tc**  
 99 nucleon, 43 proton and 56 neutron

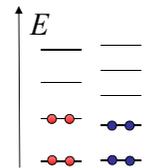
# Stability of the nucleus

- Coulomb force: destabilization (electrostatic repulsion between the protons)

- Nuclear force: very strong attractive force acts only on short range (~fm) independent on the charge



- Quantized energy levels for the nucleus.
- Typical binding energy is in the MeV range  $eV = 1,6 \cdot 10^{-19} \text{ J}$

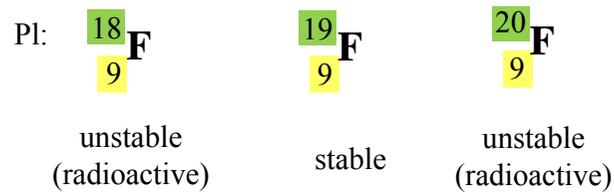


# Isotopes

Number of protons is the same  
 Number of neutrons is different  
 Variants of the same element

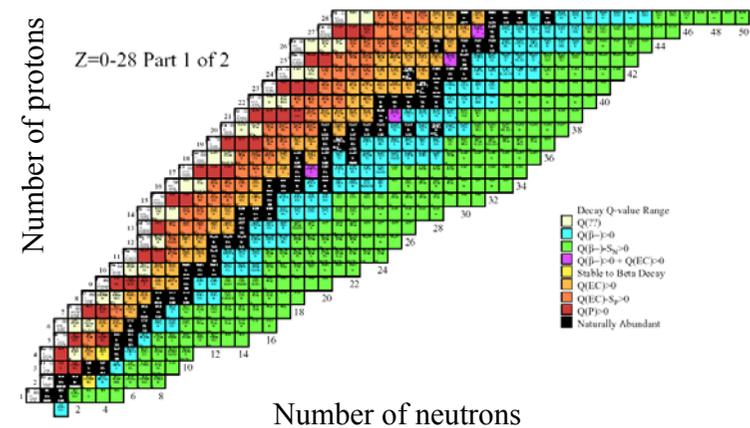


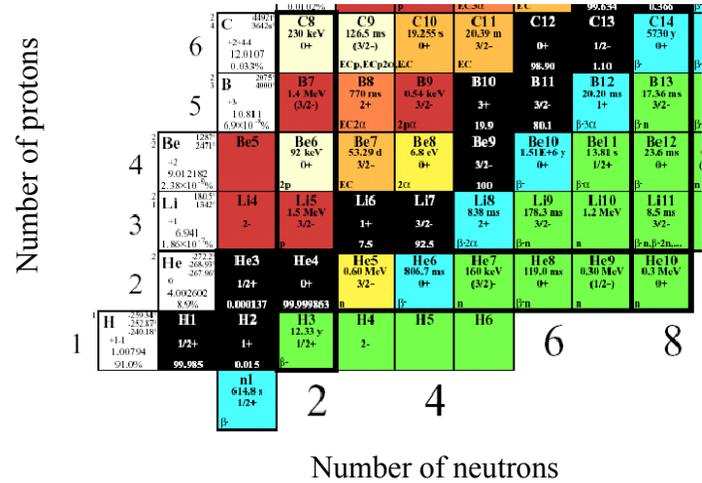
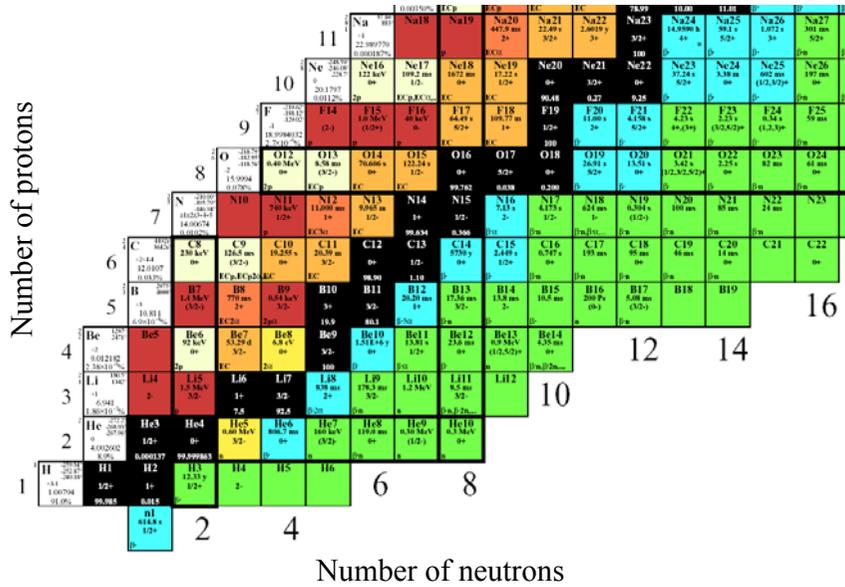
⇒ the chemical properties are identical.



isotope  $\leftrightarrow$  radioactive isotope

# Table of isotopes





## Radioactive decays and particles

$\alpha$  - decay       $\alpha$  - particle =  ${}^4_2\text{He}$  nucleus

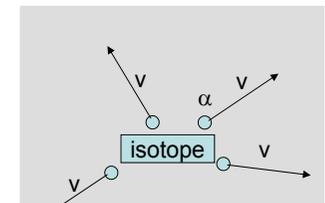
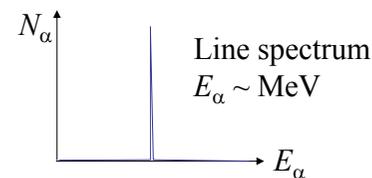
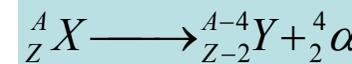
$\beta^-$  - decay :  $\beta^-$        $\beta^-$  particle = electron  
 $\beta^+$                        $\beta^+$  particle = positron

Isomeric transition       $\gamma$ -ray

K-electron capture      characteristic x-ray photon

## $\alpha$ - decay

$\alpha$  - decay: an  $\alpha$  particle ( ${}^4\text{He}$  nucleus) will be emitted  
 typical for the heavy atoms



neutron surplus

## $\beta^-$ - decay

e.g.:  ${}^{20}_9F$   
 ${}^{32}_{15}P$   
 ${}^{59}_{26}Fe$   
 ${}^{131}_{53}I$

$${}^A_Z X \longrightarrow {}^A_{Z+1} Y + {}^0_{-1}\beta + \bar{\nu}$$

$${}^1_0 n \longrightarrow {}^1_1 p + {}^0_{-1}\beta + \bar{\nu}$$

remains in the nucleus      leave the nucleus

e.g.:  ${}^{32}_{15}P \longrightarrow {}^{32}_{16}S + {}^0_{-1}\beta + \bar{\nu}$

$\beta^-$ -ray  $\rightarrow$  continuous energy spectrum

$\beta^- = {}^0_{-1}\beta = e^-$

proton surplus

## $\beta^+$ - decay

e.g.:  ${}^{11}_6C$   
 ${}^{15}_8O$   
 ${}^{18}_9F$   
 ${}^{52}_{26}Fe$

$${}^A_Z X \longrightarrow {}^A_{Z-1} Y + {}^0_{+1}\beta + \nu$$

$${}^1_1 p \longrightarrow {}^1_0 n + {}^0_{+1}\beta + \nu$$

remains in the nucleus      leave the nucleus

e.g.:  ${}^{30}_{15}P \longrightarrow {}^{30}_{14}Si + {}^0_{+1}\beta + \nu$

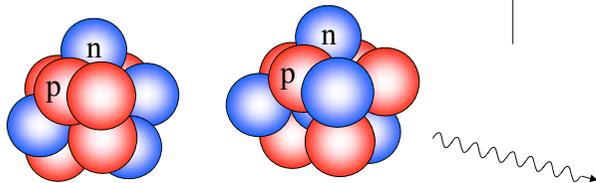
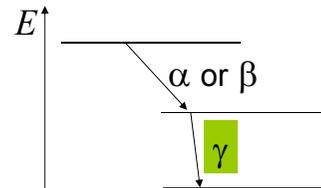
$\beta^+$ -ray  $\rightarrow$  continuous energy spectrum

These isotopes must be produced artificially (e.g. in cyclotron)

## Prompt $\gamma$ -radiation

The daughter nucleus has an **energetically unfavoured** arrangement of nucleons.

The surplus energy will be immediately (ns) emitted in form of the  $\gamma$  radiation



Atomic number, mass number are unchanged.

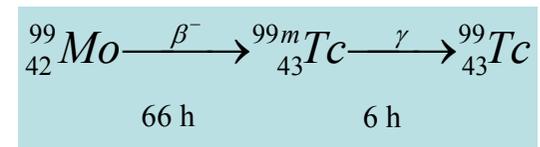
## Isomeric transition

If the excited state of the daughter nucleus is metastable, the  $\gamma$ -radiation will be emitted later.

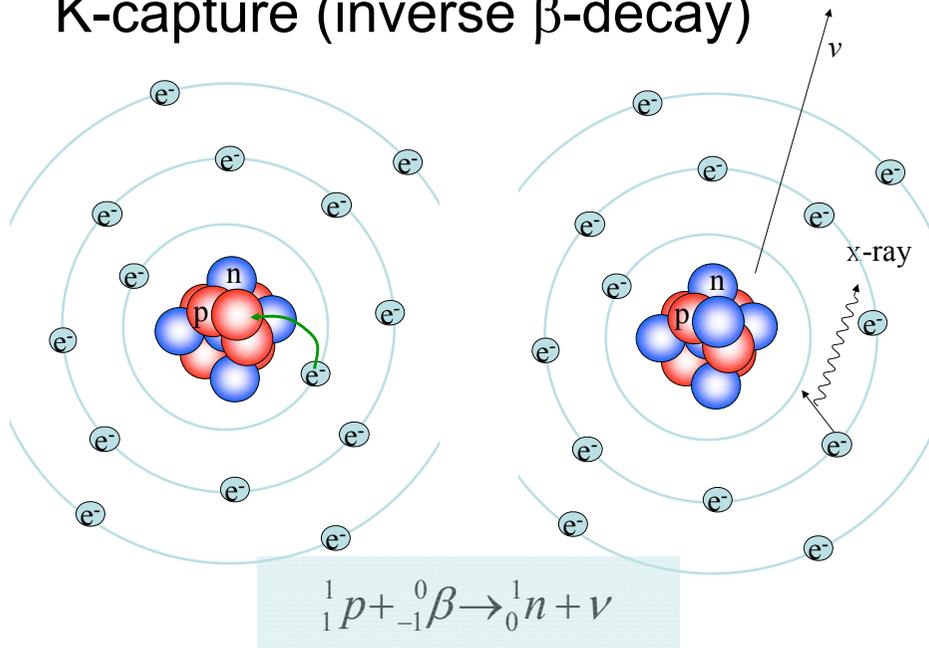
The parent and daughter atoms can be separated: the daughter atom emits **only  $\gamma$ -radiation!**

=> **Isotope diagnostics (nuclear imaging)**

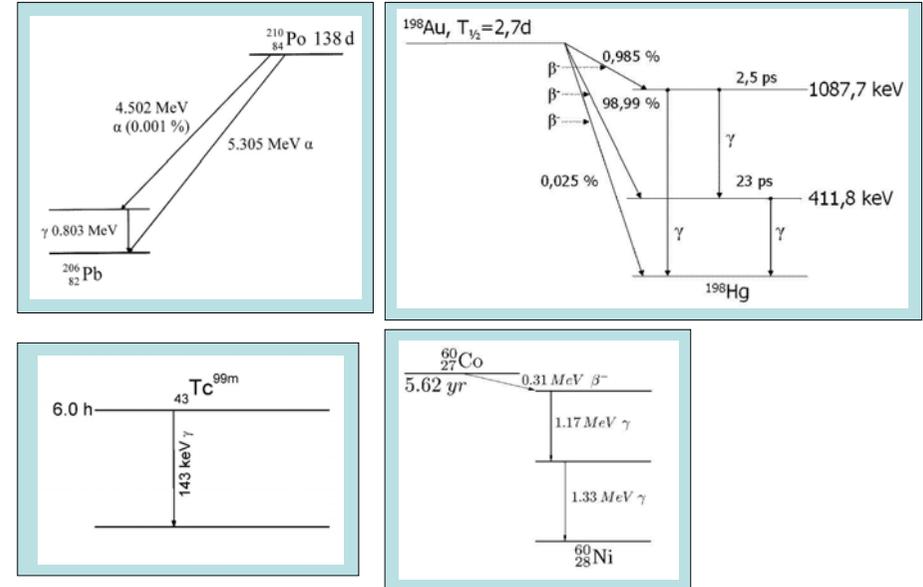
E.g.:  ${}^{99m}_{42}Tc$



# K-capture (inverse $\beta$ -decay)



# Some examples of the decay paths



## Characteristics of radioactive decays in general

- activity characterizes the source
- half life time characterizes the speed of the decay (depends on the type of the isotope)
- particle energy characterizes the radiation (depends on the type of the isotope)

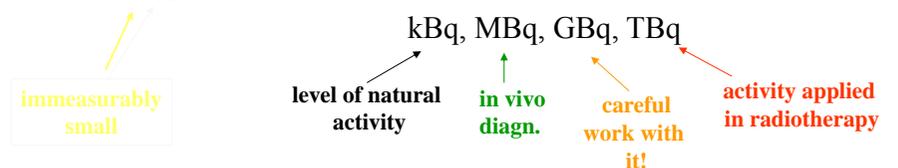
## Activity ( $\Lambda$ )

$$\Lambda = \left| \frac{dN}{dt} \right| \quad \left( = \left| \frac{\Delta N}{\Delta t} \right| \right)$$

$N$  = Number of undecayed atoms  
 $t$  = time  
 $\Delta N$  = Number of decays during  $\Delta t$  time

Activity = number of decays in a unit time

unit: becquerel Bq  
 1 Bq = 1 decay/sec



## Law of radioactive decay

$$\Delta N = -\lambda N \Delta t \quad N: \text{Number of undecayed nuclei}$$

$$\frac{dN}{dt} = -\lambda N \quad \begin{array}{l} \lambda: \text{decay constant (probability of the decay [1/s])} \\ 1/\lambda = \tau \text{ average lifetime} \end{array}$$

Differential equation

solution:

$$N(t) = N_0 e^{-\lambda t} \quad \text{Exponential decrease}$$

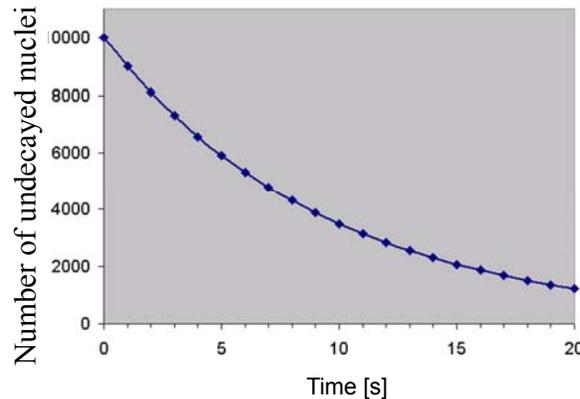
↑  
number of undecayed atoms at  $t=0$

## An example

- $N_0=10000 \quad \lambda=0.1 \text{ 1/s}$
- After 1 sec : 9000 (10000x0.1=1000 decayed)
- After 2 sec : 8100 (9000x0.1=900 decayed)
- After 3 sec : 7290 (8100x0.1=810 decayed)
- After 4 sec : 6561 (7290x0.1=729 decayed)
- ....

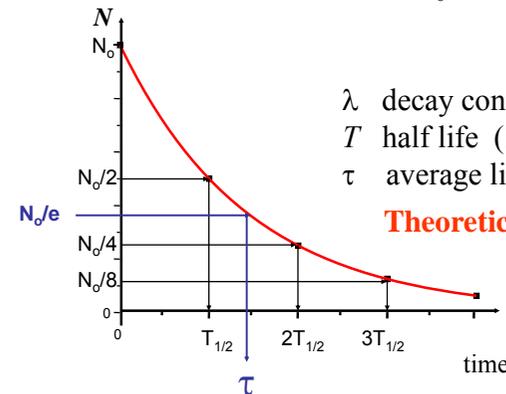
## An example

- $N_0=10000 \quad \lambda=0,1 \text{ 1/s}$
- 1 sec 9000
- 2 sec 8100
- 3 sec 7290
- 4 sec 6561
- ....



## Law of radioactive decay

$$N(t) = N_0 e^{-\lambda t} = N_0 2^{-\frac{t}{T}}$$

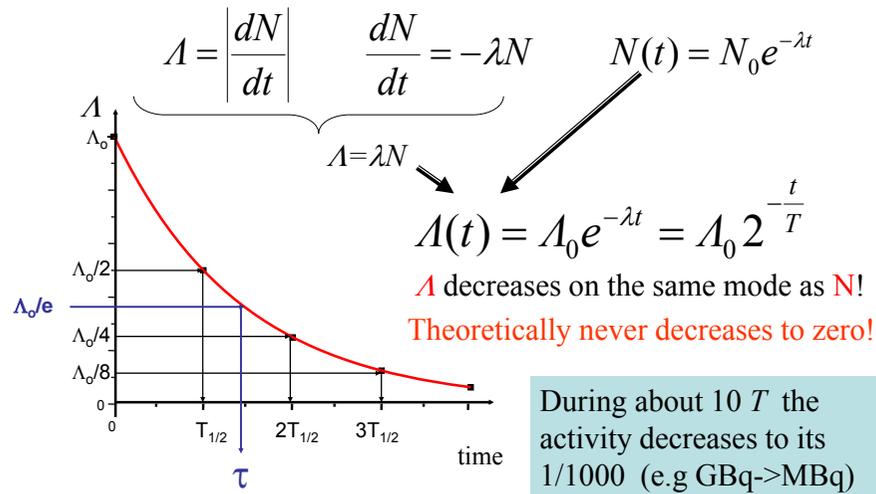


$\lambda$  decay constant (probability of the decay)  
 $T$  half life ( $T_{1/2}$ )  
 $\tau$  average lifetime

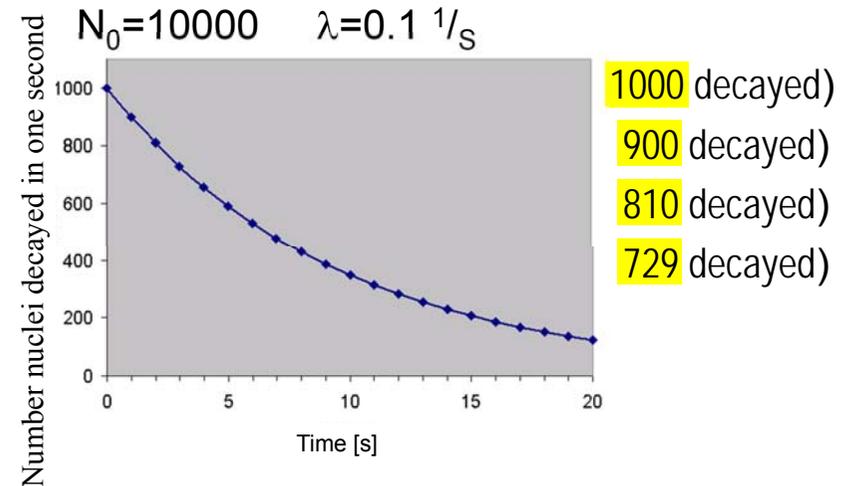
**Theoretically never decreases to zero !**

$$\lambda = \frac{\ln 2}{T} = \frac{0,693}{T}$$

## Decrease of the activity as a function of time



## Example



## Few examples for half life

$^{232}\text{Th}$	$1,4 \cdot 10^{10} \text{ y}$	$^{60}\text{Co}$	5,3 y
$^{238}\text{U}$	$4,5 \cdot 10^9 \text{ y}$	$^{59}\text{Fe}$	1,5 m
$^{40}\text{K}$	$1,3 \cdot 10^9 \text{ y}$	$^{56}\text{Cr}$	1 m (28 d)
$^{14}\text{C}$	5736 y	$^{131}\text{I}$	8 d
$^{137}\text{Cs}$	30 y	$^{99\text{m}}\text{Tc}$	6 h
$^3\text{H}$	12,3 y	$^{18}\text{F}$	110 min
		$^{11}\text{C}$	20 min
		$^{15}\text{O}$	2 min
		$^{222}\text{Th}$	2,8 ms

**Don't learn these numbers!**

## Typical energy levels in the microworld

Excitation of the outer electrons

eV (aJ)

light



Electron transition between inner electrons

keV (fJ)

X-ray



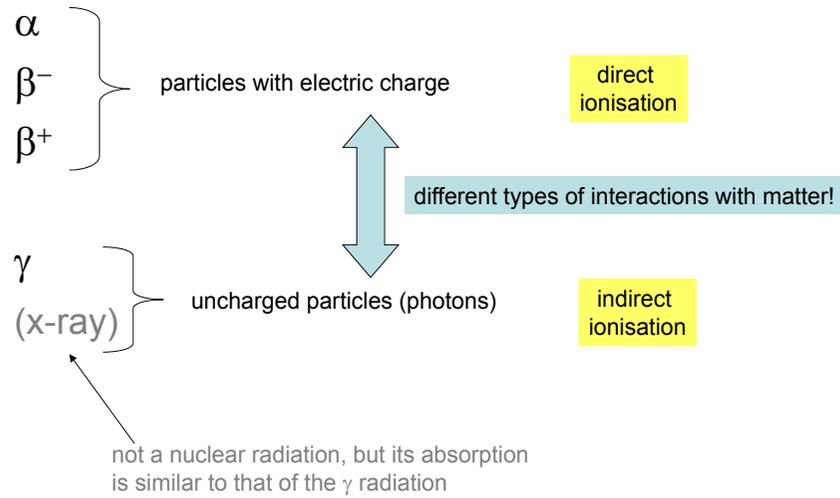
Transformation of the nucleus (decay)

MeV (pJ)

Nuclear radiation  
 $\alpha$ ,  $\beta$ ,  $\gamma$



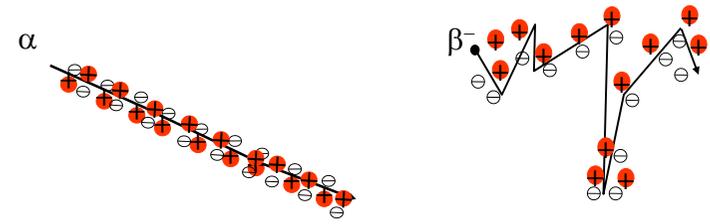
# Absorption of the nuclear radiation



# Absorption of the charged particles

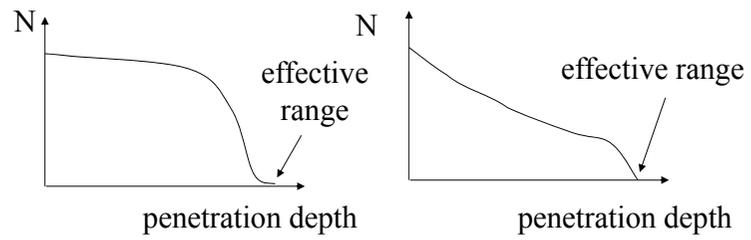
Ionizing during the path => continuous decrease of the particle energy  
 The energy after a given path length decreases to the thermal value

effective range

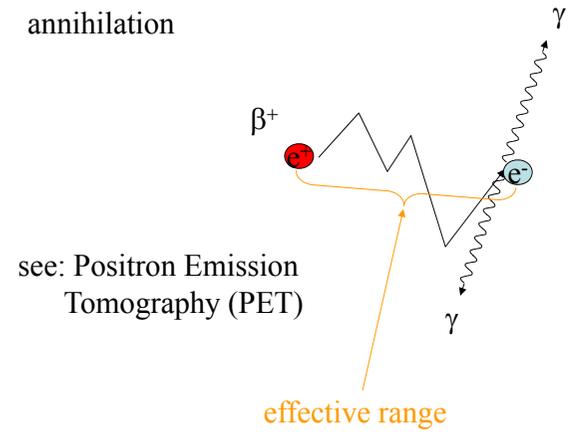


# Effective range

	$\alpha$ -particle	$\beta^-$ -particle
in air	few cm	~ m
in tissue	0,01-0,1 mm	~ cm

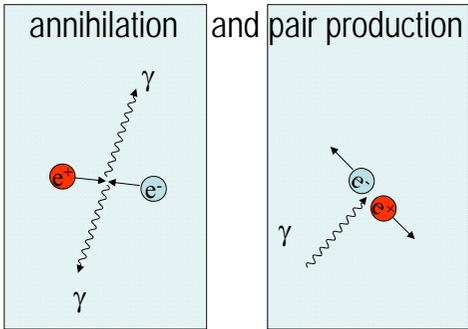


# $\beta^+$ -radiation



# Electron and positron

- particle - antiparticle
- same mass,
- charge: same value, but different

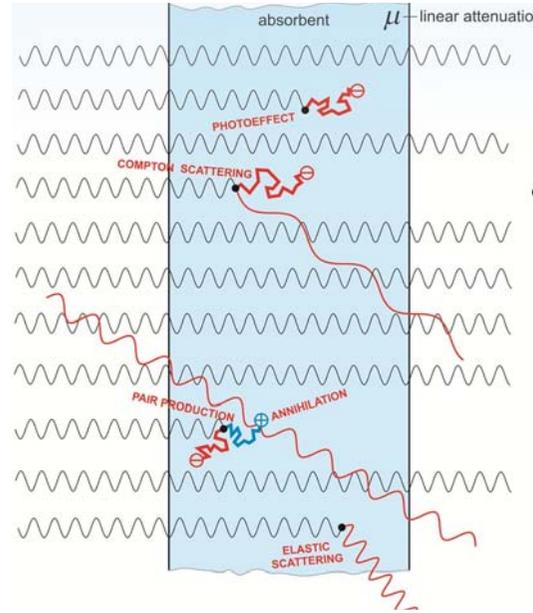


Einstein:  
mass-energy  
equivalence

$$E=mc^2$$

$m_e c^2 = 511 \text{ keV} \approx 0,5 \text{ MeV}$

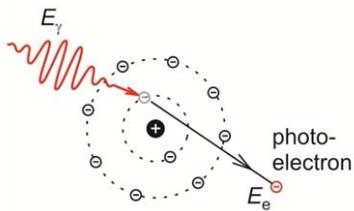
# Absorption of the $\gamma$ -radiation (and x-ray)



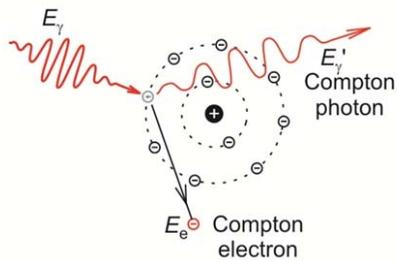
Absorption processes happen accidentally :

Photoeffect,  
Compton-effect,  
Pair production,  
(elastic scattering)

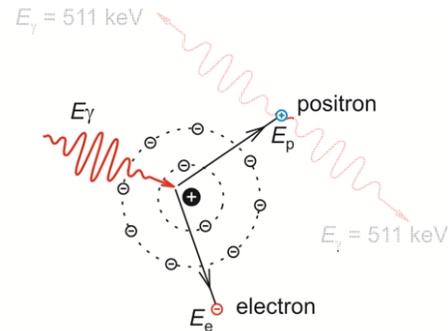
Photoeffect



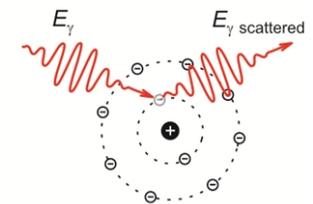
Compton effect  
Compton-scattering



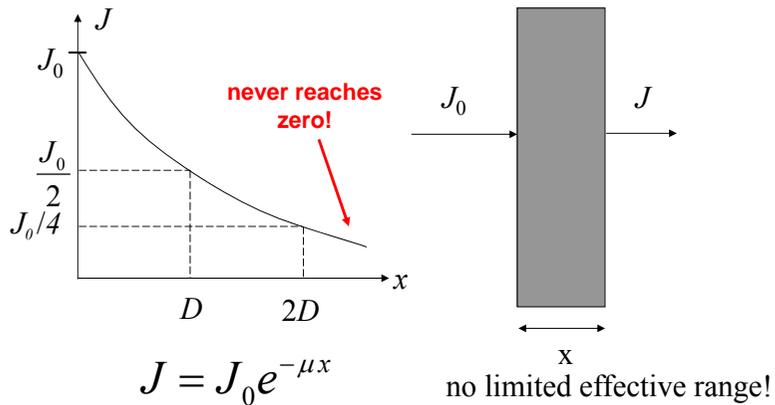
Pair production



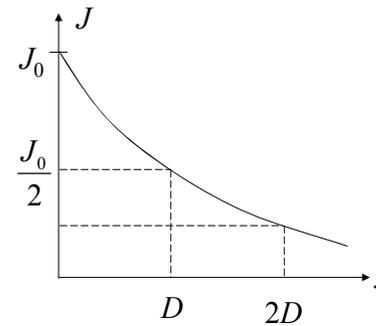
elastic scattering



# Attenuation of the $\gamma$ -radiation and x-ray



few rules of thumb:  $x_{1/10} = 3,33 D$      $x_{1/1000} = 10 D$



$$J = J_0 e^{-\mu x}$$

$\mu$ : (linear) attenuation coefficient  
its units are: 1/m, 1/cm

$\delta = \frac{1}{\mu}$  „penetration depth”  
Intensity decreases to the e-th part (c.a. 37%)

$\mu$ (material, number of absorbing centers, energy of the radiation)  
 $= \mu(\text{material}, \rho, E_{\text{photon}}) \sim \rho$

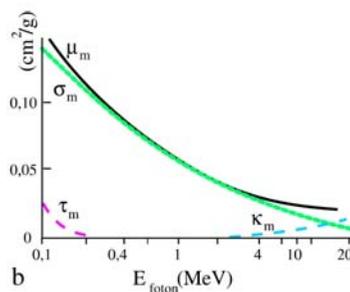
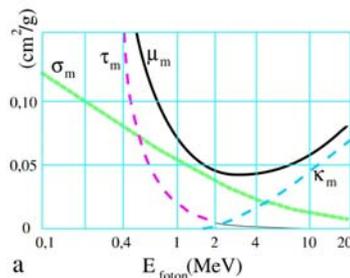
$$\mu_m = \frac{\mu}{\rho} \quad \text{mass attenuation coefficient}$$

mass attenuation coeff.

$$\mu_m = \frac{\mu}{\rho}$$

$$\mu_m = \tau_m + \sigma_m + \kappa_m$$

$$\tau_m = c \lambda^3 Z^3$$



## Applications (attenuation)



← lead glass

→ protective apron

