

Principles of Biostatistics and Informatics

2nd Lecture: Descriptive Statistics

18th September 2017

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Tastitsticsss? What's that?

Statistics describes **random mass** phenomenon.



- **Data Collecting (Sampling)**
- **Data Organization**

Descriptive Statistics

- **Data Analysis**
- **Conclusion**

**Inferential Statistics
(Inductive)**

Tastitsticsss? What's that?

Statistics describes **random mass** phenomenon.



- Data Collecting (Sampling)
- Data Organization

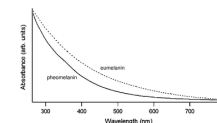
Descriptive Statistics

- Data Analysis
- Conclusion

**Inferential Statistics
(Inductive)**

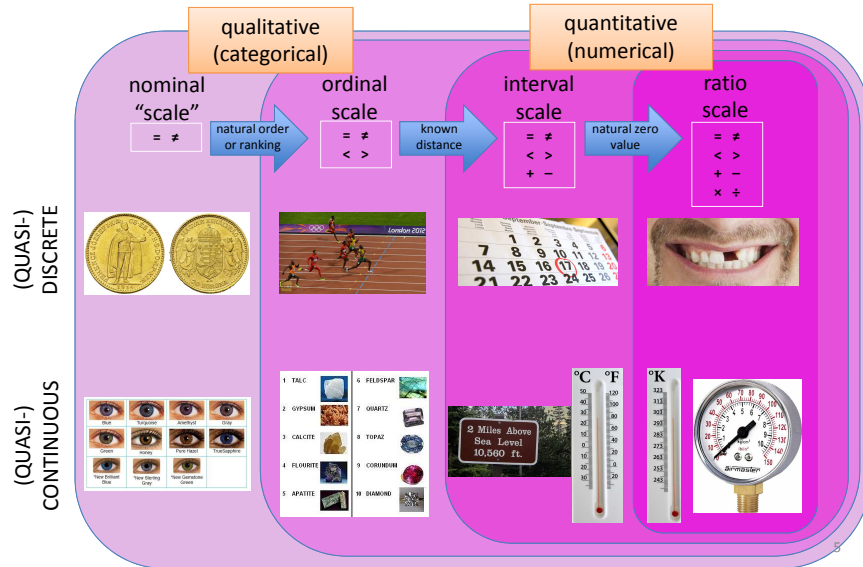
Variables, outcomes

Could be measured or observed



4

Variable Types: Levels of Measurement



Description of Nominal Variables I.

Numerical (analytical)

List

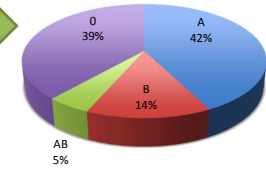
| patient No | blood group (ABO) | cholesterol level (mg/dL) |
|------------|-------------------|---------------------------|
| 1 | B | 148 |
| 2 | AB | 147 |
| 3 | B | 169 |
| 4 | B | 159 |
| 5 | B | 150 |
| 6 | B | 167 |
| 7 | A | 144 |
| 8 | B | 158 |
| 9 | A | 177 |

Frequency table

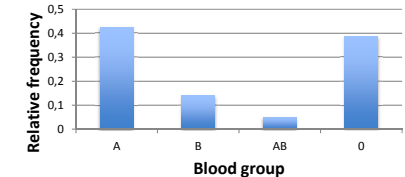
| blood group | (absolute) frequency | relative frequency |
|-------------|----------------------|--------------------|
| A | 85 | 0.425 |
| B | 28 | 0.14 |
| AB | 10 | 0.05 |
| 0 | 77 | 0.385 |
| Σ | 200 | 1 |

Graphical

Relative frequency



Relative frequency „distribution”



Univariate organization – without losing information

Description of Nominal Variables II.

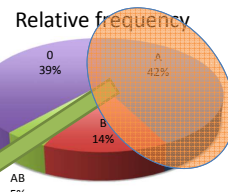
Numerical

Frequency table

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Graphical

The brain and the common sense



Organization, but loss of information

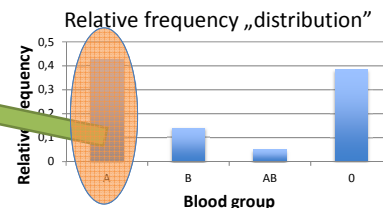
„Typical value” (*indicator*): **Mean?!**

Mode: most frequent element(s)

Notation: *Mod*, x_{mod}

Other parameters:

data count (*n*), **count of categories**



Description of Ordinal Variables I.

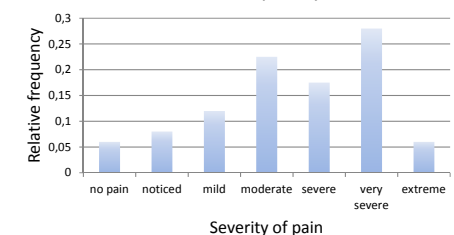
Numerical

Frequency table

| Severity of pain | Relative frequency | Cumulative relative frequency |
|------------------|--------------------|-------------------------------|
| no pain | 0,06 | 0,06 |
| noticed | 0,08 | 0,14 |
| mild | 0,12 | 0,26 |
| moderate | 0,225 | 0,485 |
| severe | 0,175 | 0,66 |
| very severe | 0,28 | 0,94 |
| extreme | 0,06 | 1 |
| Σ | 1 | |

Graphical

Relative frequency



Indicator:

Mode

Other parameters:

data count (*n*), **count of categories**

Description of Ordinal Variables II.

Numerical

Frequency table

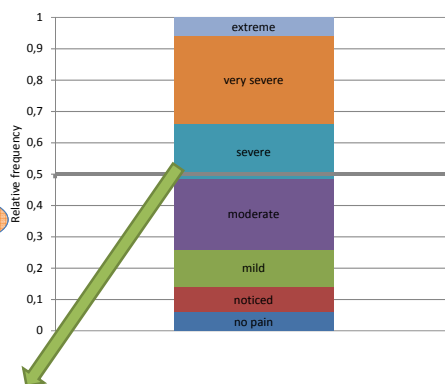
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| very severe | 0,94 |
| extreme | 1 |
| Σ | |

New indicator:

Median: „middle” element(s)

Notation: Me, Med, x_{med}

Graphical



Description of Quantitative Variables I.

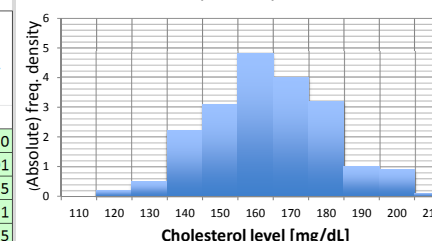
Numerical (analytical)

Graphical

Frequency tables

| frequency distributions (differential discrimination functions) | | | | |
|---|----------------------------------|--------------------|------------------------------|----------------------------|
| bins (classes, intervals) | (absolute) frequency (FREQUENCY) | relative frequency | (absolute) frequency density | relative frequency density |
| $x \leq 100$ | 0 | 0 | 0 | 0 |
| $100 < x \leq 110$ | 0 | 0 | 0 | 0 |
| $110 < x \leq 120$ | 2 | 0,01 | 0,2 | 0,001 |
| $120 < x \leq 130$ | 5 | 0,025 | 0,5 | 0,0025 |
| $130 < x \leq 140$ | 22 | 0,11 | 2,2 | 0,011 |
| $140 < x \leq 150$ | 31 | 0,155 | 3,1 | 0,0155 |
| $150 < x \leq 160$ | 48 | 0,24 | 4,8 | 0,024 |

(absolute)freq.density distribution



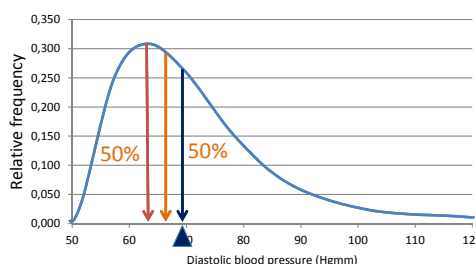
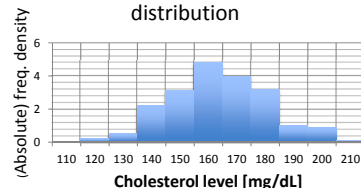
Organizing data – with **loss of information**

Determination of bin width:

- technical and aesthetic concerns
- statistical concerns

Description of Quantitative Variables II.

(absolute)freq.density distribution



„Typical values” – **central tendencies** (special **measures of location**):

- **Mode:** most frequent element(s) ?
- **Median:** „middle” element(s)?
- **Mean** (arithmetic mean): „gravity center” , sensitive to „outliers”?

Notation: x_{mean} , \bar{x}

Advantage: compact, **could be determined from few data**

Formulas: in the formula collection...

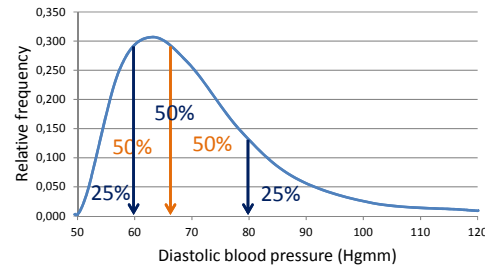
Digress I.

Average \neq Mean

In statistics the average could means:

mode,
median,
means – arithmetic, geometric, harmonic... mean

Quantiles I.



Other measures of location:

- **Median:** 50-50% (Q_2)
- **Quartile:** lower quartile (Q_1): 25-75%; upper quartile (Q_3): 75-25%

General

p-quantile(s): is the number to which the count of data are smaller is maximum $n \cdot p$ and to which the count of data are larger is maximum $n \cdot (1 - p)$,

where p is between 0 and 1, and n is the count of data

Digress II.

| Day | Waiting time (min) | | Day | Waiting time (min) | |
|-----|--------------------|----------------|------|--------------------|----------------|
| 1 | 1,27 | median | 8,48 | 1,27 | median |
| 2 | 3,3 | lower quartile | 3,59 | 3,3 | lower quartile |
| 3 | 3,44 | mean | 7,72 | 3,44 | mean |
| 4 | 3,64 | | | 3,64 | |
| 5 | 6,33 | | | 6,33 | |
| 6 | 7,72 | | | 7,72 | |
| 7 | 9,23 | | | 9,23 | |
| 8 | 9,87 | | | 9,87 | |
| 9 | 10,31 | | | 10,31 | |
| 10 | 12,29 | | | 12,29 | |
| 11 | 12,3 | | | 12,3 | |
| 12 | 12,98 | | | 20 | |

Median, quantiles could differ in theory and practice.

Mean is sensitive to the outliers, but quantiles not (...).

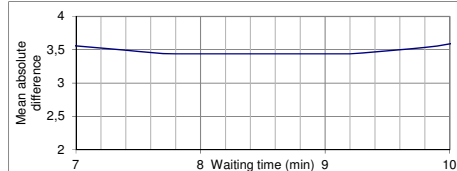
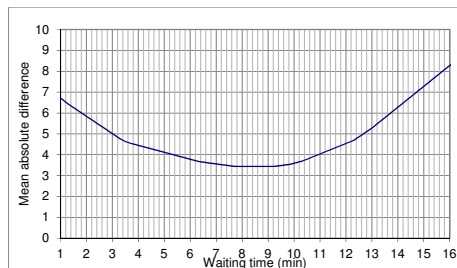
Mode?

Digress III.

$$\frac{1}{n} \sum |x_i - x^*|$$

Minimal if:

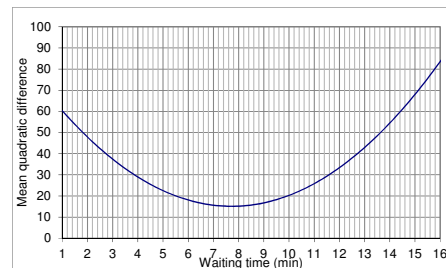
$$x^* = \text{Median}$$



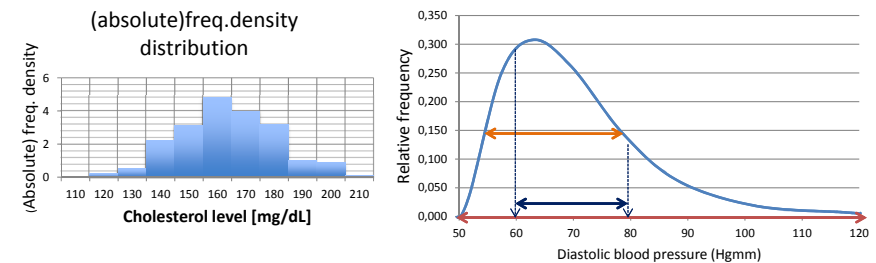
$$\frac{1}{n} \sum (x_i - x^*)^2$$

Minimal if:

$$x^* = \text{Mean}$$



Description of Quantitative Variables III.

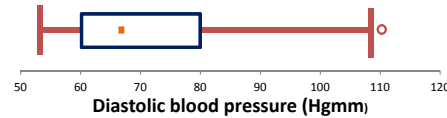


Measures of spread:

- **Range:** the difference between the maximum and the minimum
- **Variance (s^2):** the average of the squared distance from the mean (corrected - sample, uncorrected - population)
- **Standard deviation (s , sd , SD):** the square root of the variance the width of the curve
- **Interquartile range (IQR):** the difference between the upper and the lower quartile – not sensitive to the „outliers“

Description of Quantitative Variables IV.

Graphical: Box plot



Middle point: mean, or *median*

Box: 2*standard deviation, or *interquartile range*, p-quantile range

Whisker: $3 \times SD$, minimum and maximum, 0.05 and 0.95 quantiles, p-quantiles, $1.5 \times IQR$...

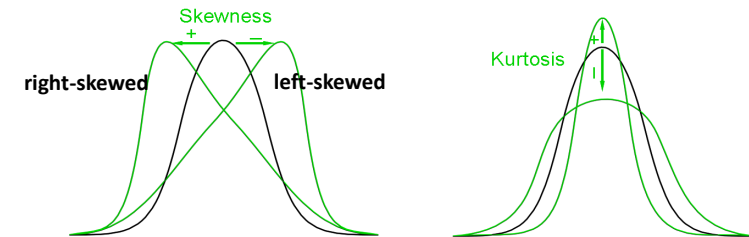
out of whiskers: **outliers**

Trimmed mean: mean calculated without outliers

Description of Quantitative Variables V.

Other parameters:

- **moment:**
the k-th moment: $\Sigma (x_i)^k / n$
 - **central moment:**
the k-th central moment: $\Sigma (x_i - \mu)^k / n$
 - **skewness,**
 - **kurtosis**
- } **measures of shape**

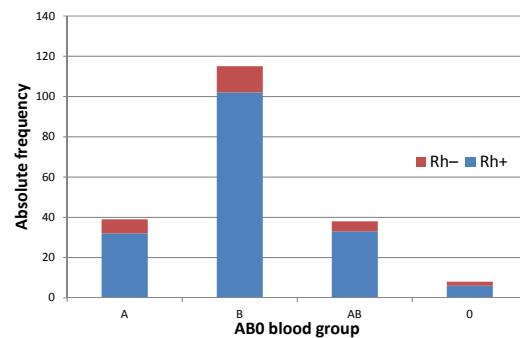


Qualitative Bivariate Description

Numerical: **contingency** table

| | A | B | AB | 0 | Σ |
|----------|----|-----|----|---|----------|
| Rh+ | 32 | 102 | 33 | 6 | 173 |
| Rh- | 7 | 13 | 5 | 2 | 27 |
| Σ | 39 | 115 | 38 | 8 | 200 |

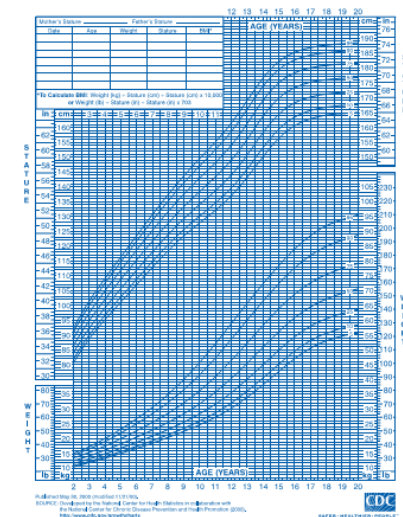
Graphical: ***stacked bar chart***

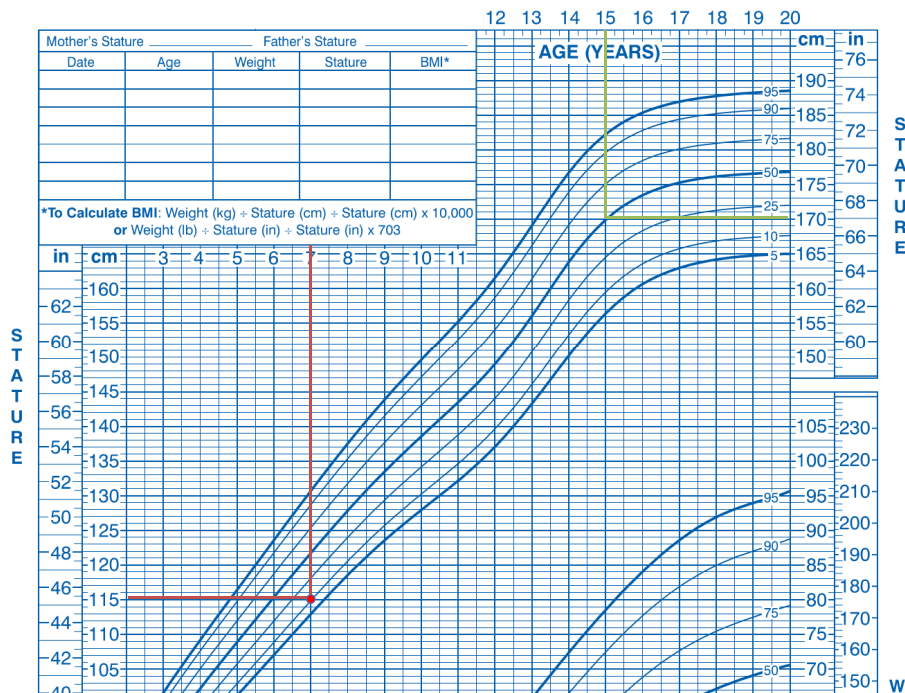


Quantitative Bivariate Description

Graphical: ***percentile curves***

Percentile: quantile expressed as percentage





Data Collection Thoughts

Data collection is motivated by a goal and not by a variable.
Use the highest measurement level as possible.

Record data

- use a form that is easy to organize and convert - excel
- *variables in separated cells*
- *Coding have to be clear* (type of variable, categories)

Test Questions #1

- Give the four actions of statistics.
- Give the two part of descriptive statistics.
- Give the two part of inferential statistics.
- Name some ordinal variables, scales.
- Name some discrete numerical variables, scales.
- Name some continuous numerical variables, scales.
- What is the substantial difference between a nominal and an ordinal scale?
- Give example for interval scale.
- What is the substantial difference between an ordinal and an interval scale?
- Give examples for ratio scale.
- What is the substantial difference between an interval and a ratio scale?
- Why is it important to define a statistical variable properly?
- What are the two way as we could describe a variable?
- What are the indicators that we can use to describe a nominal variable?
- What are the indicators that we can use to describe an ordinal variable?
- What are the indicators that we can use to describe a numerical variable?
- Define the mode(s) of a dataset.
- What is the notation of mode?
- Define the median(s) of a dataset.
- What is the notation of median?
- In which type of measurement scale do we loose information usually?
- How we can determine the bin width?
- What is the equation we have to use to determine the bin width?
- What are the central tendencies in case of a numerical variable?
- What is the „meaning“ of the mode in a diagram?
- What is the „meaning“ of the median in a diagram?
- What is the „meaning“ of the mean in a diagram?
- Define the mean of a dataset.
- What is the notation of mean?
- Which central tendency sensitive to outliers?
- What is the advantage of indicators versus distribution functions?
- What is the difference between average and mean?
- What are the measures of location?
- Define the p-quantile.
- Define the lower quartile.
- What is the difference between the second quartile and the median?
- Show how we could calculate the lower quartile of a dataset in theory and in practice.
- What is the value that for the sum of the absolute differences are minimal?
- What is the value that for the sum of the squared differences are minimal?

Test Questions #2

- What are the measures of spread?
- What are the measures of shape?
- Define the variance.
- Define the standard deviation.
- Define the skewness.
- Define the kurtosis.
- Define the interquartile range.
- What is the notation of interquartile range?
- What is a box plot?
- What are the parts of a box plot?
- What we could use as a middle point of a box plot?
- What we could use as a box of a box plot?
- What we could use as a whisker of a box plot?
- What is recommended middle point in a box plot if we have a non symmetrical distribution with outliers?
- What is recommended box boundary in a box plot if we have a non symmetrical distribution with outliers?
- What is recommended box boundary in a box plot if we used a median as a middle point?
- What is the trimmed mean?
- How we define the outlier range commonly?
- What are the moments?
- What are the central moments?
- What is the first central moment?
- What is the first moment?
- What is the second central moment?
- What are the percentiles?
- What we could read out from a percentile curve?