





**Tipping:**

force	couple	$\sum F$	$\sum \tau$	
-	✓	<b>0</b>	$\tau_C$	→ rotation ↻
✓	-	<b>F</b>	$\tau_F$	→ <b>tipping:</b> translation + rotation ↻
✓	✓	<b>F</b>	$\tau_F - \tau_C$	→ <b>controlled tipping:</b> translation + rotation ↻

$0 < \tau_F - \tau_C \quad (\tau_F - \tau_C < 1)$  ↻  
 $\tau_F - \tau_C < 0 \quad (1 < \tau_F - \tau_C)$  ↻

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Example:

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**Dental brace**

Dental braces are elastic bodies, that will recover the elastic energy after deformation by exerting forces on the teeth („**mechanical battery**“).

activation:  
deformation  
(energy input)

dental application:  
**recovery**  
(stored energy utilized)

loading  
force recovery  
activation  
application

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**Mechanical properties of brackets**

- properties: stiffness, elastic strain recovery, resilience

elastic region!

work done = work recovered, assuming no friction!!

plastic region!

work done  
work recovered

Example:

- polymers
- steel
- Co-Cr alloys
- Ti alloys

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- geometry: shape, dimensions (i.e. thickness, length, ...)

- stretch/compression
- bending
- torsion

$$F = E \frac{A}{l} \Delta l \quad W = \frac{1}{2} E \cdot \frac{A}{l} \Delta l^2$$

$$F = 3E \cdot \frac{\Theta}{l^3} \cdot s \quad W = \frac{1}{2} 3E \cdot \frac{\Theta}{l^3} \cdot s^2$$

$$M = G \frac{r^4 \pi}{2l} \phi$$

body stiffness

**Problems:**

- friction

Frictional force ( $F_f$ ):

$$F_f = \mu \cdot F$$

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## Restoring force

- magnitude?
- time course?

↔ utilized strain (time of application)

↔ utilized strain (time of application)

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## Superelastic materials

Ni+Ti    Cu+Al+Zn    Cu+Al+Ni

**Nitinol** (Nickel-Titanium Naval Ordnance Laboratory)

- Superelastic (pseudoplastic)
- shape memory
- biomechanical compatibility
- biocompatible

Constancy of Stress

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elastic (reversible) response to an applied stress, caused by a phase transformation between the austenitic and martensitic phases of a crystal.

Martensite

a, b, & c are not equal,  
γ about 96°

expansion

Austenite

FCC

temperature

↑  $A_s$      $A_f$  →

←

↓  $M_f$      $M_s$

rapid cooling

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