

**WATER,  
MACROMOLECULES**

**MIKLÓS KELLERMAYER**

# Water

- Source of *inspiration* (music, paintings).
- Thales (580, B.C.): “...water is source of all things...”
- Henry Cavendish (1783): water is  $H_2O$ .
- Only chemical that naturally exists in *all three states* (solid, liquid, gas).
- 71% of the Earth’s surface is covered with water (“blue planet”).
- Water is of utmost importance for *life*:
  - 98% of jellyfish
  - 94% of three-month human fetus
  - 72% of newborn
  - 60% of adult
- Average daily water intake: 2.4 liters.



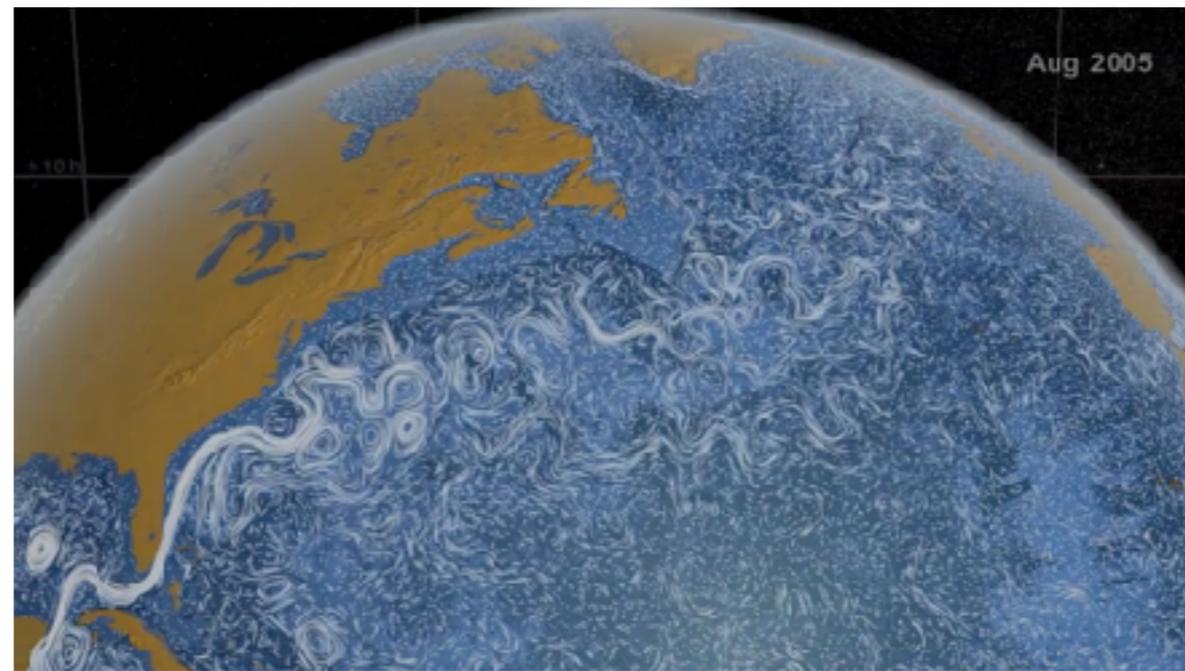
Georg Friedrich **Händel** (1685-1759): “**Water music**”.



Georg Friedrich Händel (center) and King George I (right) on the Thames River, 17 July 1717.



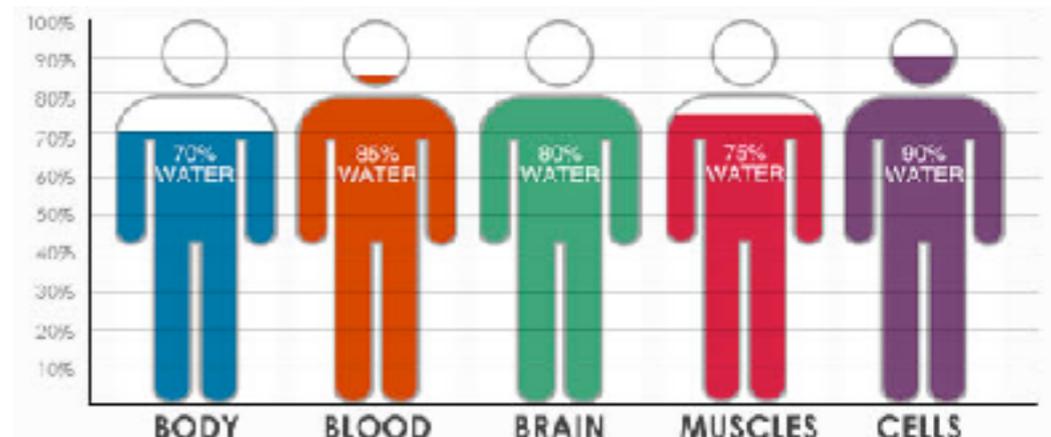
Hokusai (1760-1849): Great wave off Kanagawa



Perpetual motion of oceans on Earth’s surface.



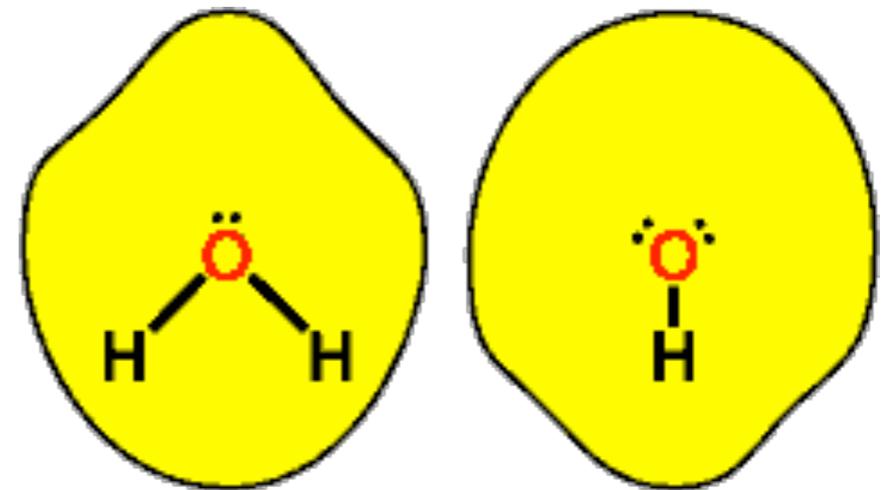
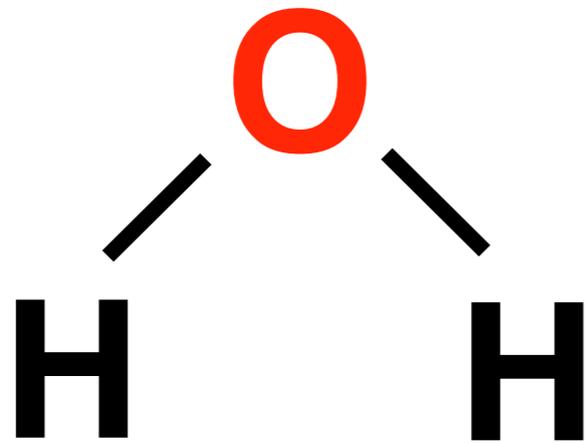
Jellyfish



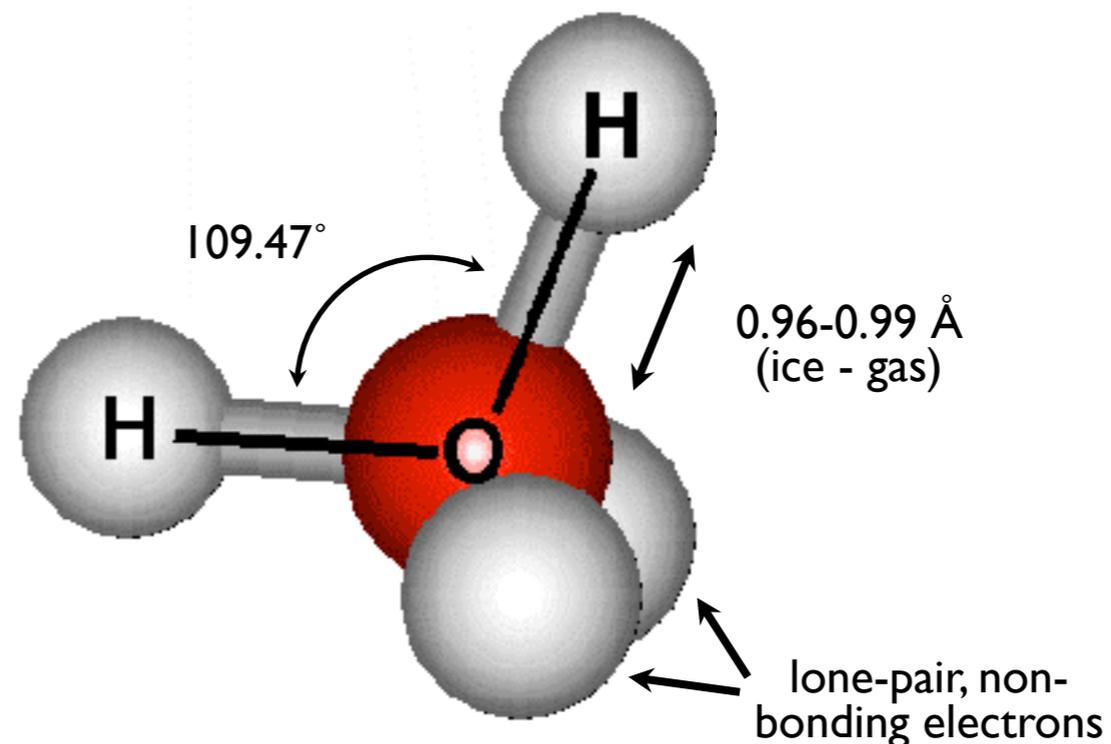
# Structure of the water molecule

One of the smallest molecules  
Barely larger than an atom

van der Waals radius:  $\sim 3.2 \text{ \AA}$   
Its shape is not spherical

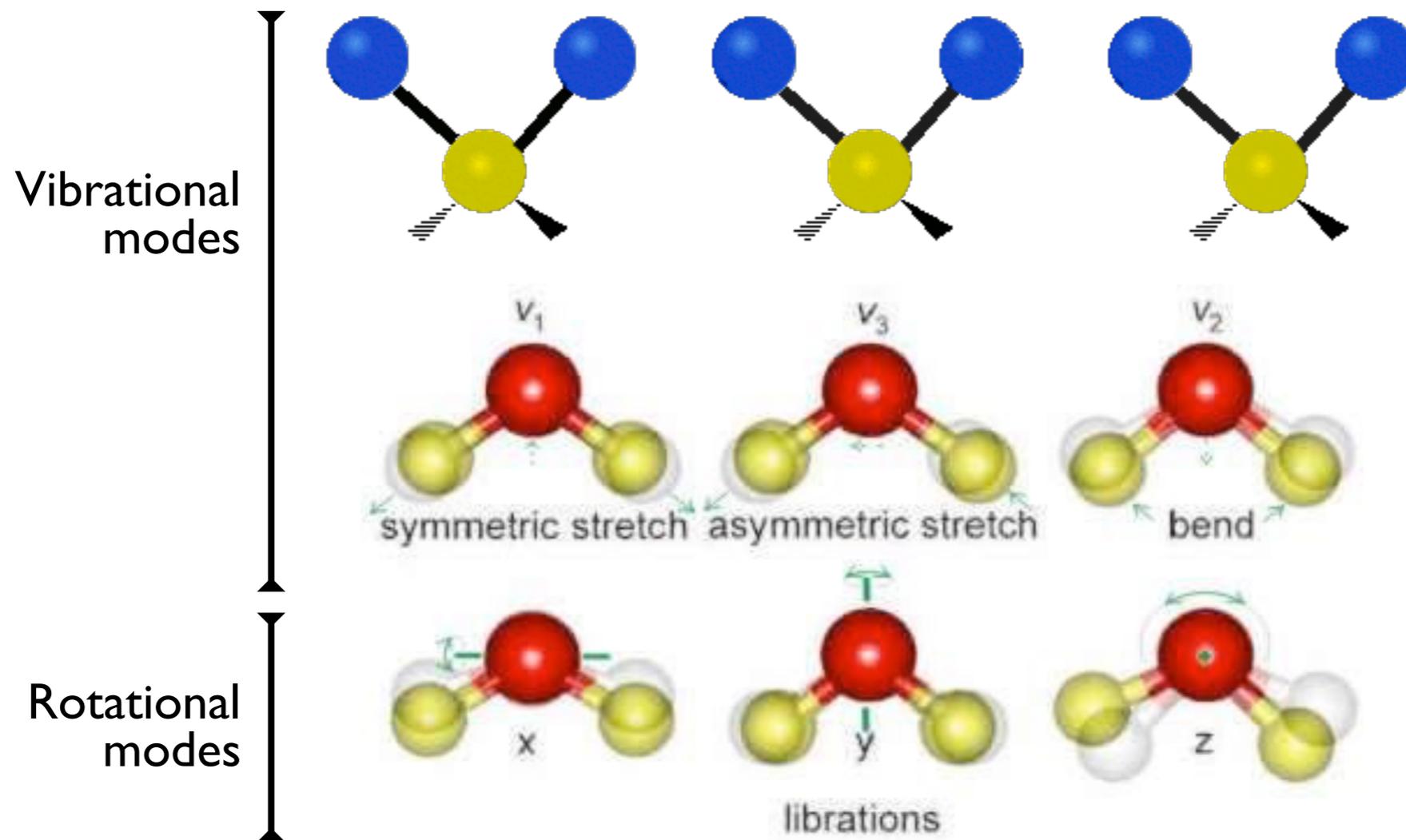


Tetrahedral structure:



# Dynamics of the water molecule

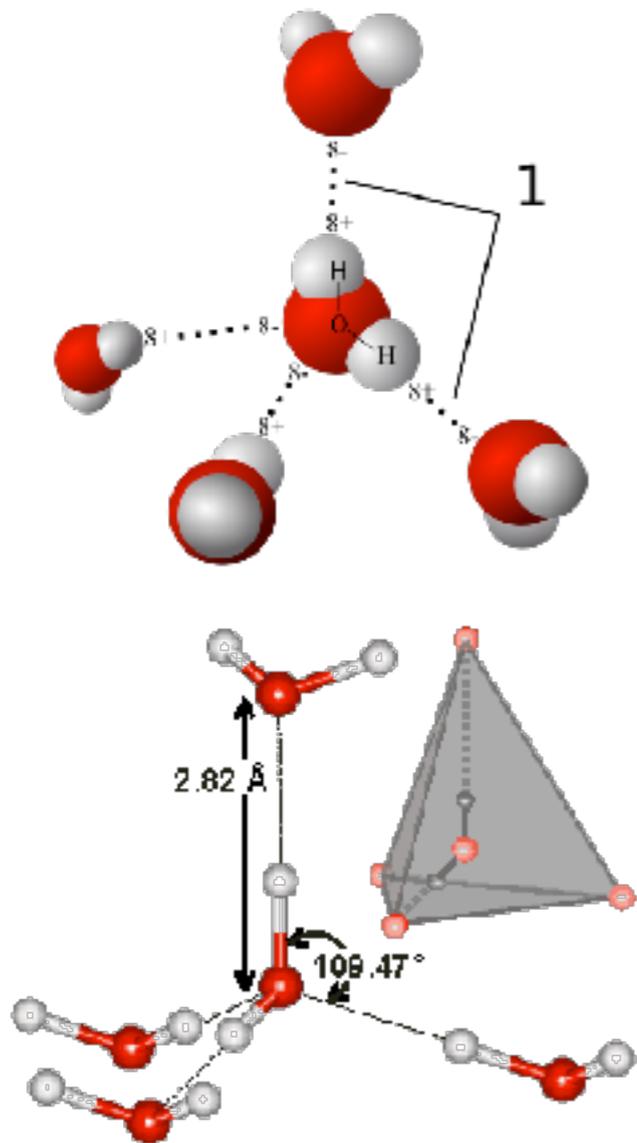
## Rotational and vibrational motion



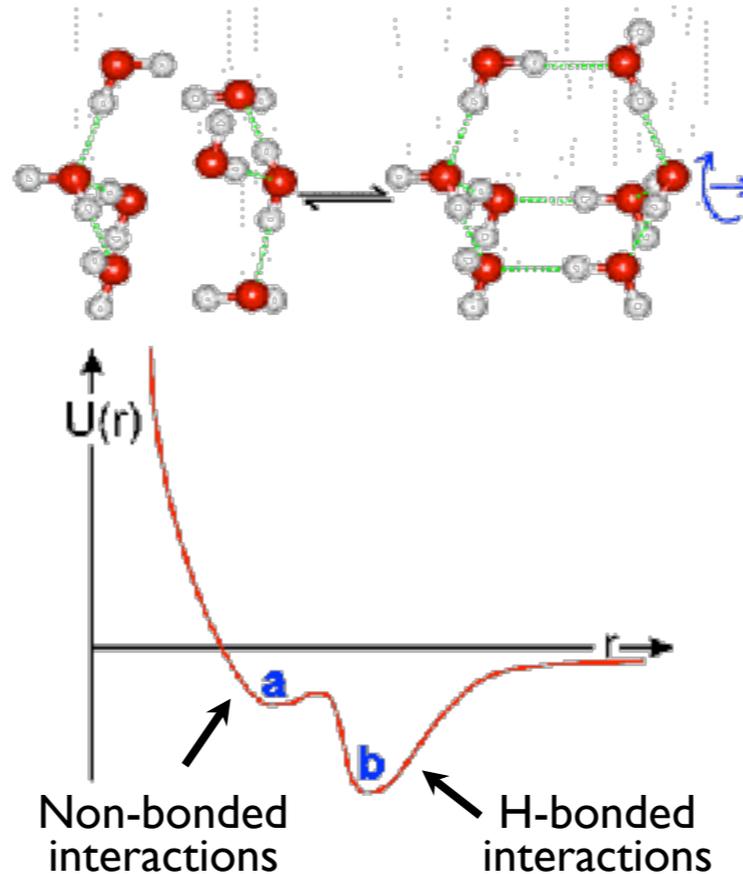
Absorption in the infrared and red spectral region →  
“blue” color of natural waters: *blue planet*

# Structure of liquid water

Hydrogen bonds in the vicinity of a water molecule: formation of the water pentamer

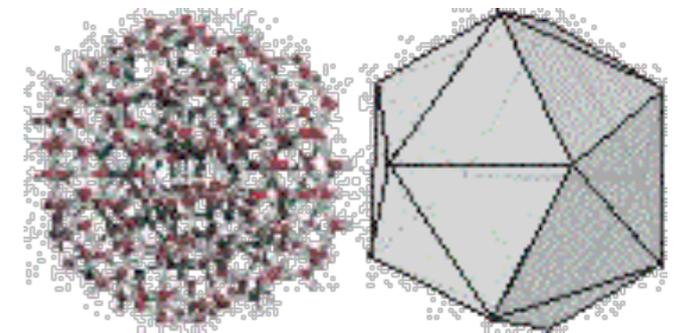


H-bridge: cohesion + repulsion  
Cluster formation: bicyclo-octamer



From clusters to networks:  
280 molecules form  
icosahedral structure

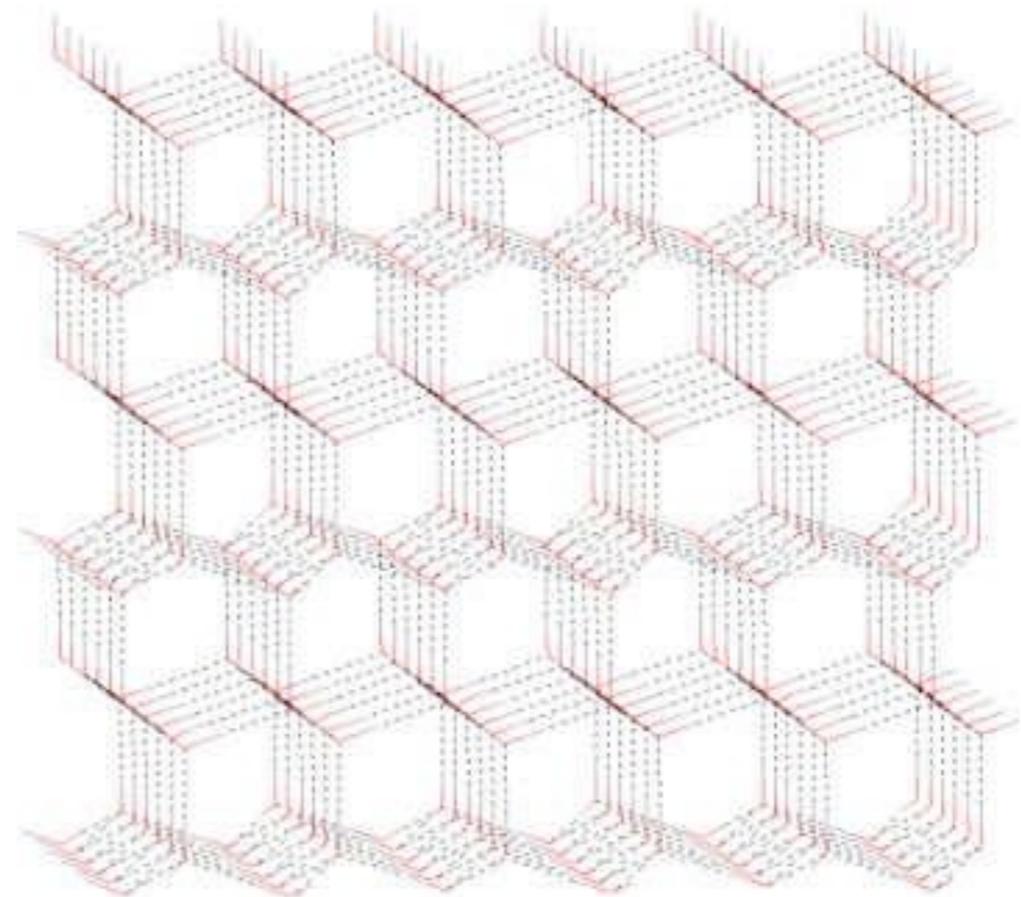
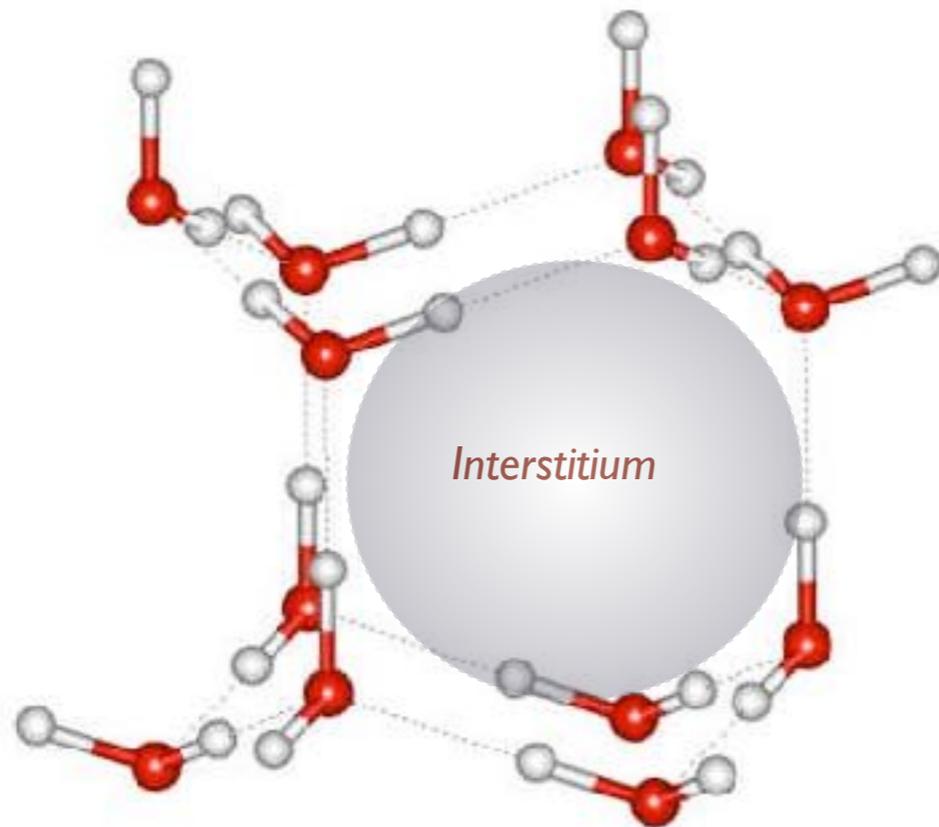
(icosahedron: regular polyhedron with 20 identical equilateral triangular faces)



Spatial networks:  
May explain anomalous  
properties of water

# Structure of ice

- 9 different forms
- Conventional ice: hexagonal structure
- Coordination number: 4 (each molecule coordinates another four) Interstitium: could incorporate a water molecule - important in the diffusion of gases



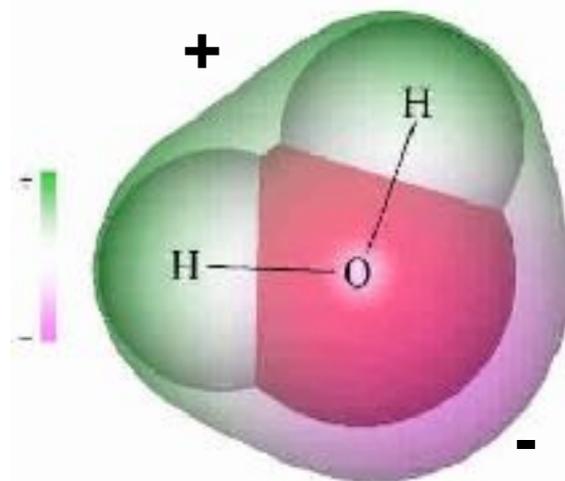
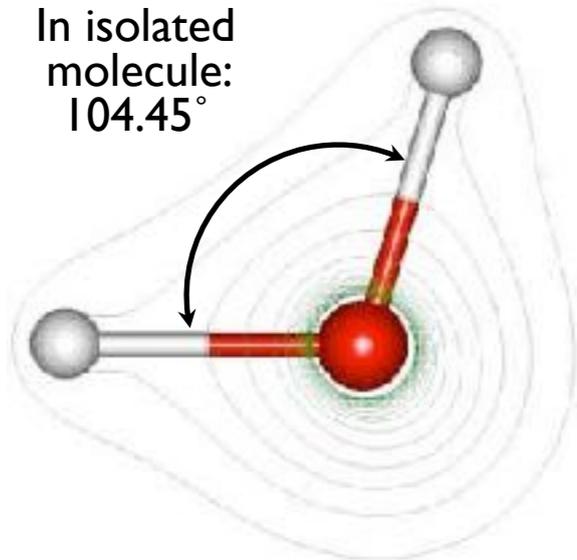
# Physical properties of water I.

Large permanent dipole moment



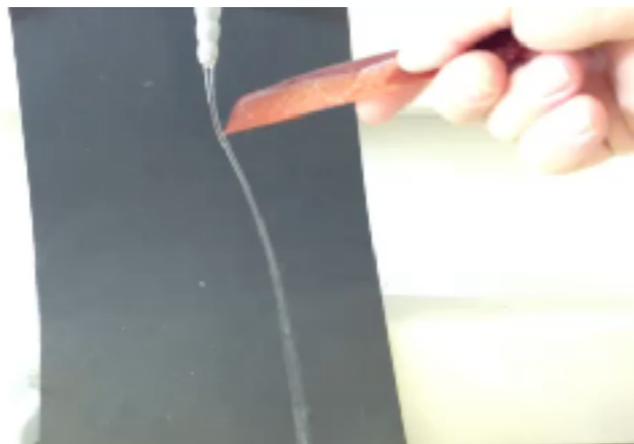
Good solvent

In isolated molecule:  
104.45°



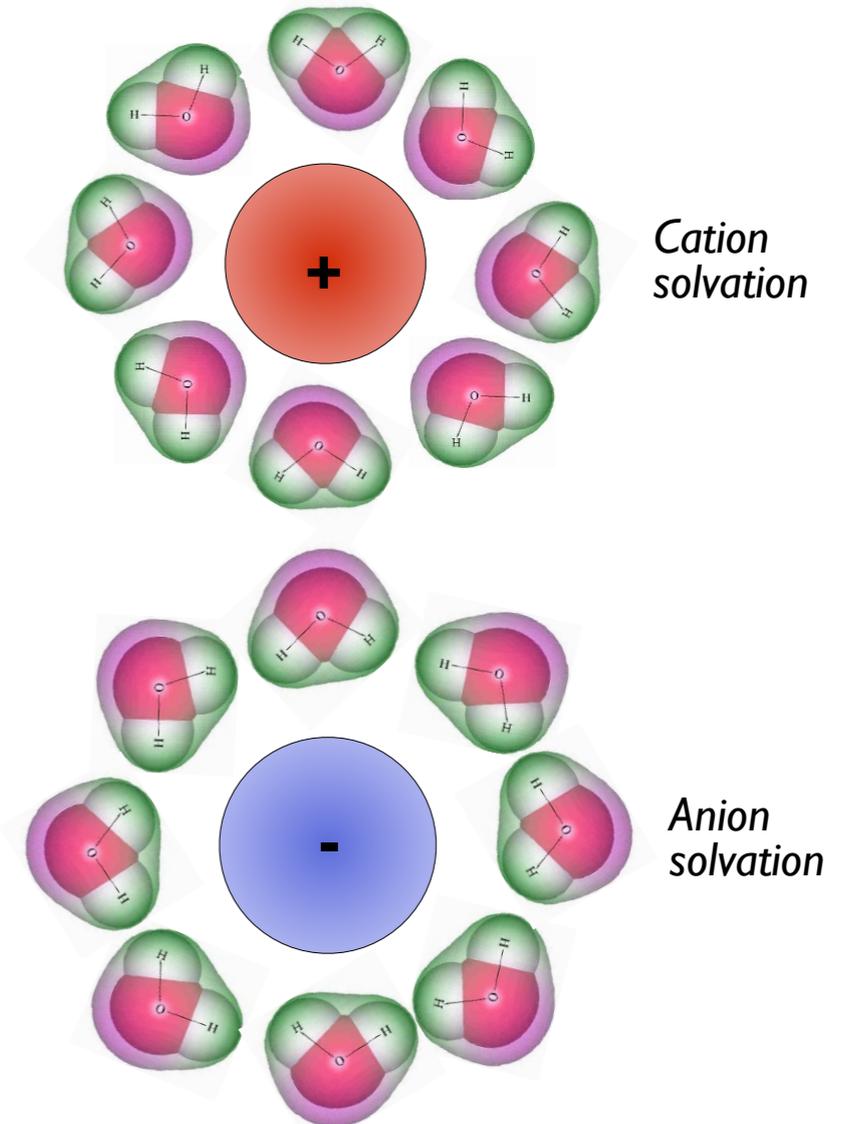
Chemical	Dipole moment
Polyethylene	2.25
Methanol	30
Ethylene glycol	37
Glycerol	47
<b>Water</b>	<b>80</b>
Titanium dioxide	86-173

Water stream bends in response to Coulombic forces



Courtesy of Prof. Miklós Zrínyi

*Dipole moment:* amount of electrical energy stored in the material by an applied voltage, relative to vacuum. It shows how good an electrical insulator the material is. Consequence: water is good solvent.



In the *microwave oven*: dipoles rotate according to the oscillating electromagnetic field. Water molecules acquire kinetic energy, which dissipates into the surroundings.

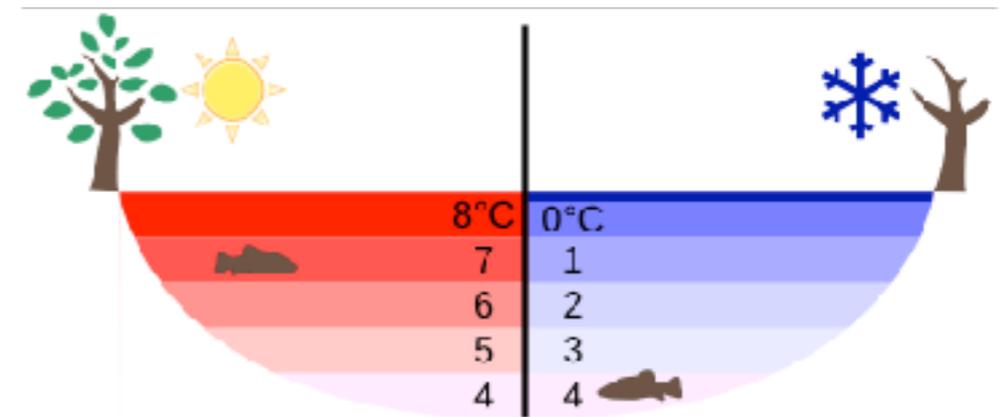
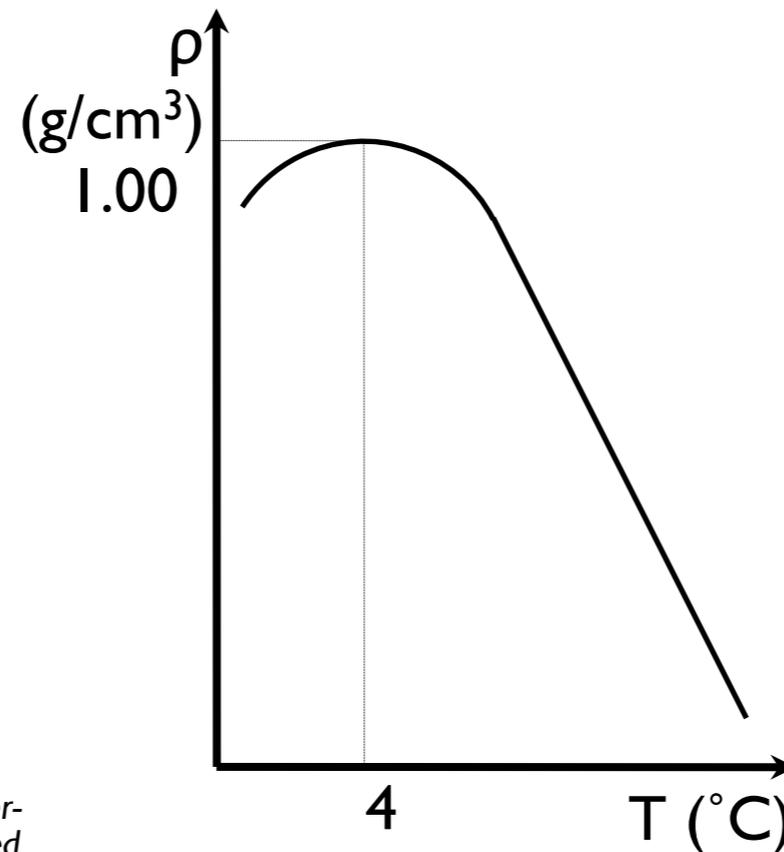
# Physical properties of water II.

## Anomalous density-temperature function

Temperature (°C)      Density (kg/m<sup>3</sup>)

+100	958.4
+80	971.8
+60	983.2
+40	992.2
+30	995.6502
+25	997.0479
+22	997.7735
+20	998.2071
+15	999.1026
+10	999.7026
<b>+4</b>	<b>999.9720</b>
0	999.8395
-10	998.117
-20	993.547
-30	983.854

Super-cooled water



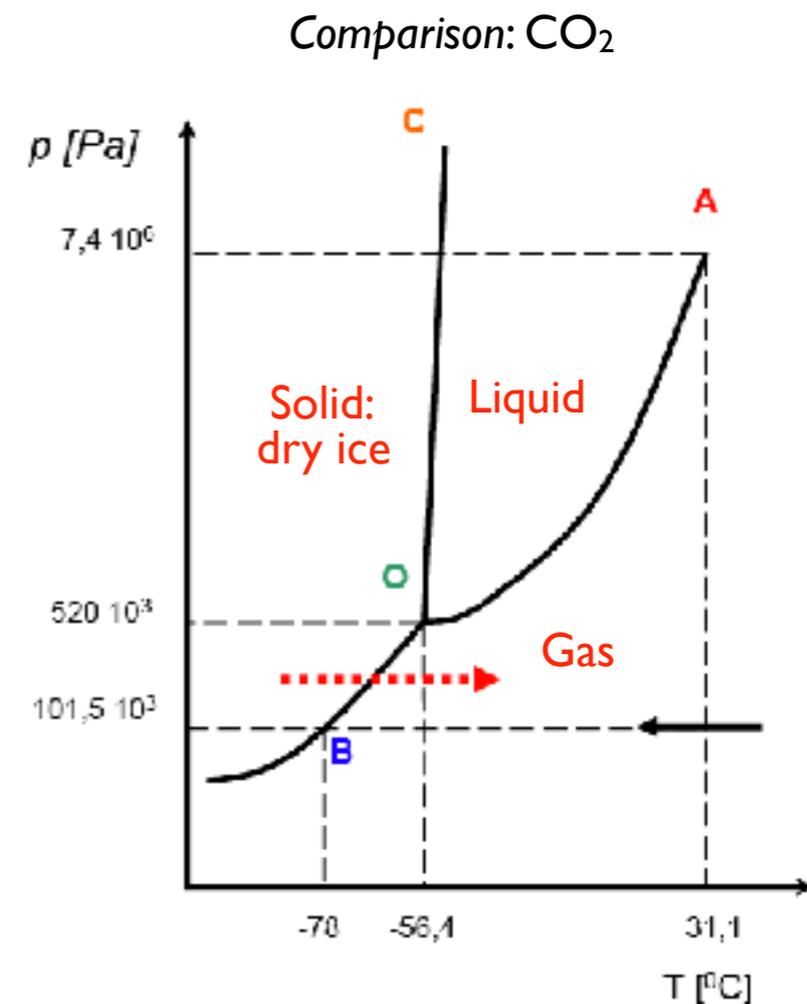
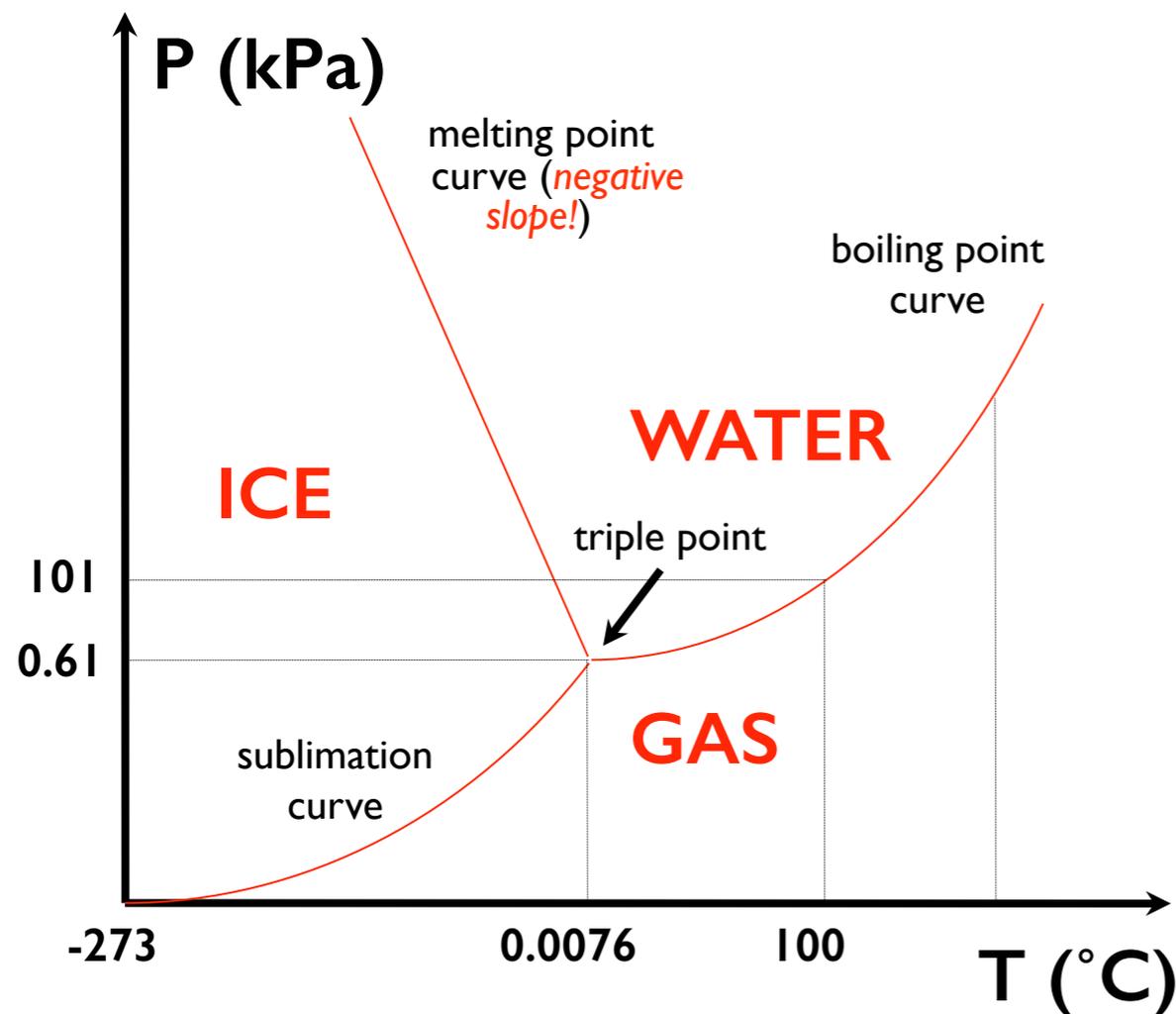
### Consequences:

- 4 °C water is always at the bottom of the lake.
- Life persists under frozen lake.
- Creek runs under ice.

# Physical properties of water III.

## Anomalous phase diagram

- Phase curve: two phases are in equilibrium
- Area between phase curves: a single phase is present
- Intersection of phase curves: triple point

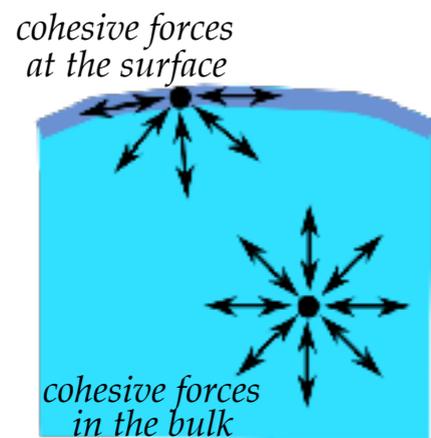


# Physical properties of water IV.

## Large surface tension

**Surface tension:** contractive tendency of the liquid that resists external force.

Imbalance of cohesive forces in the **bulk** versus the **surface** of the liquid.



Chemical	Surface tension (mN/m)
Ethanol	24.4
Methanol	22.7
Acetone	23.7
Chloroform	27.1
Benzene	28.5
<b>Water</b>	72.9

### Consequences on **hydrophobic** surface



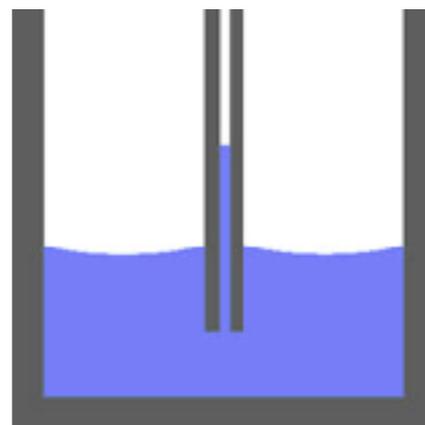
Persisting droplet on a superhydrophobic surface

### Consequences in macroscopic living systems

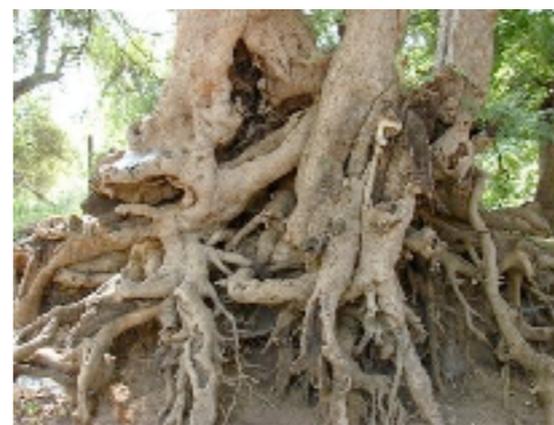


Water striders

### Consequences on **hydrophilic** surface



Capillary action (model)



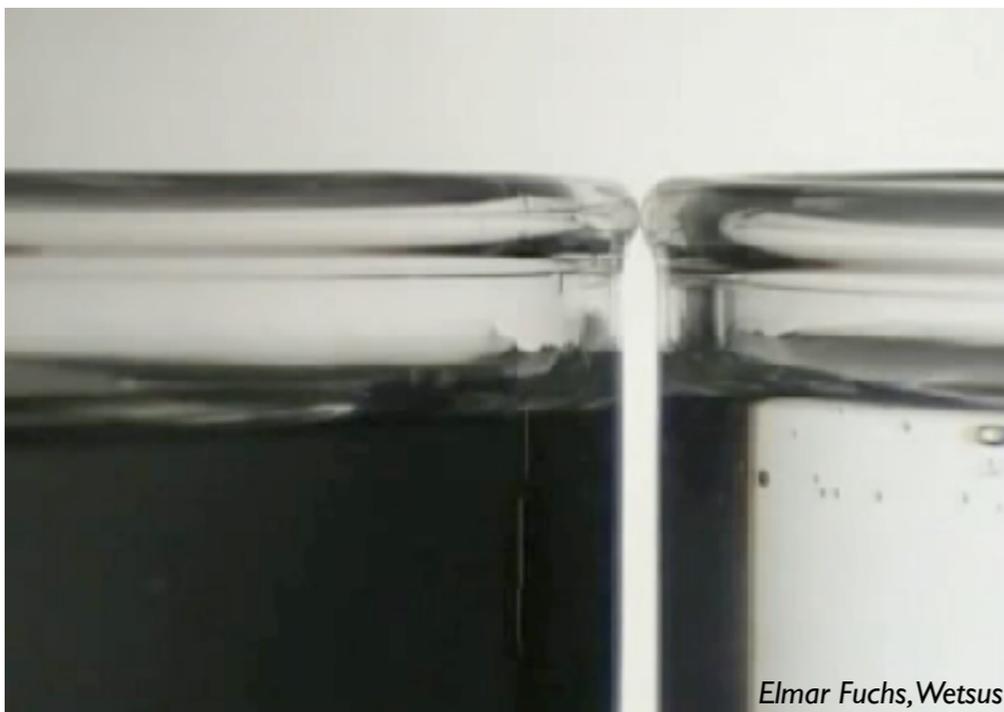
Capillary action aiding plant root function



"Jesus Christ lizard" (basilisk)

# Further interesting features of water

Floatig water bridge

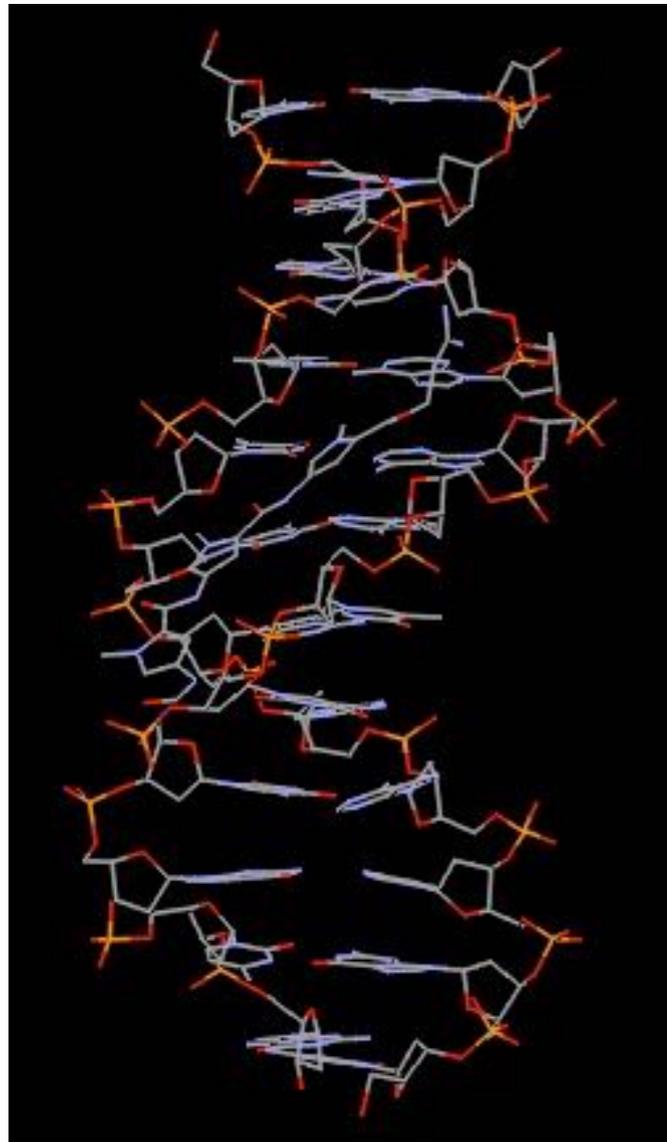


Persisting water droplets on vibrating water surface

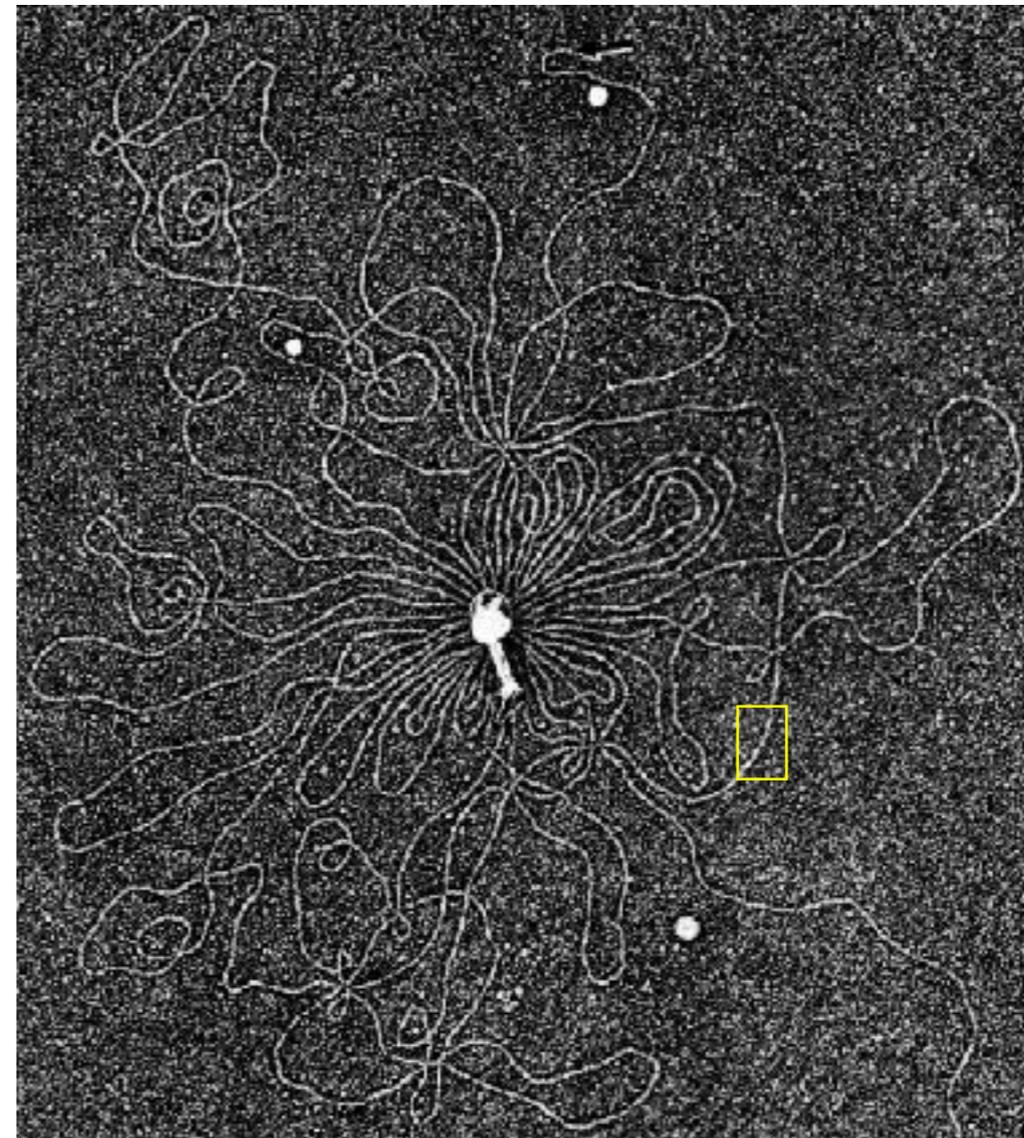


Number of water molecules in the cell	$\sim 1.6 \times 10^{14}$
Distance between water molecules	$\sim 0.4$ nm

# Biological macromolecules are **GIANT** molecules

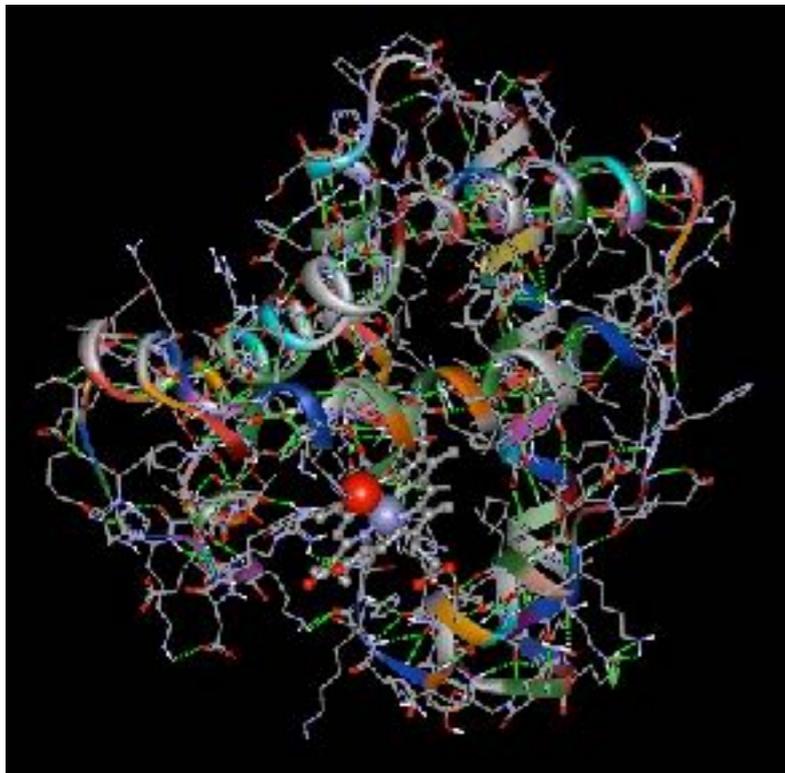


DNS double helix

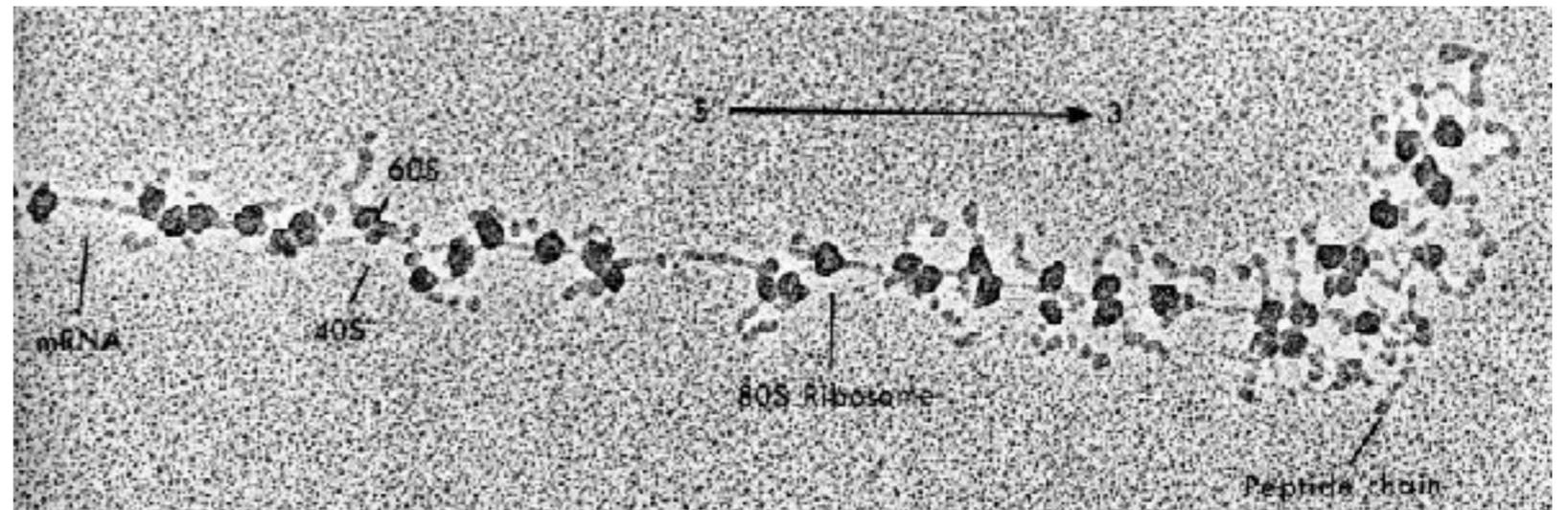


DNA released from bacteriophage head

# Biological macromolecules are **EXCITING** molecules

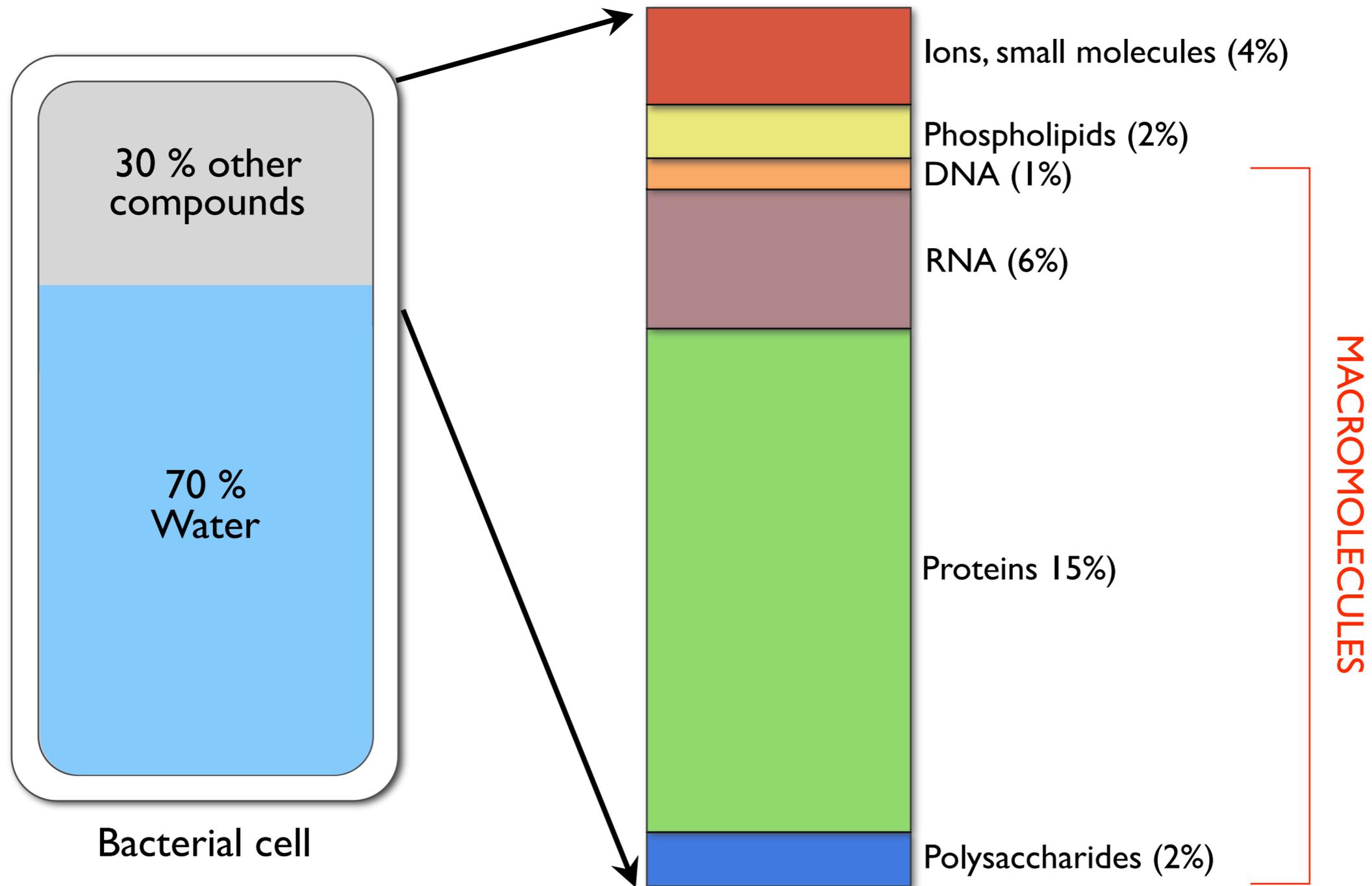


Structure of hemoglobin  
subunit



Newly synthesized protein (silk fibroin)

# Proportion of macromolecules in the cell by mass is **LARGE**



# Biological macromolecules: biopolymers

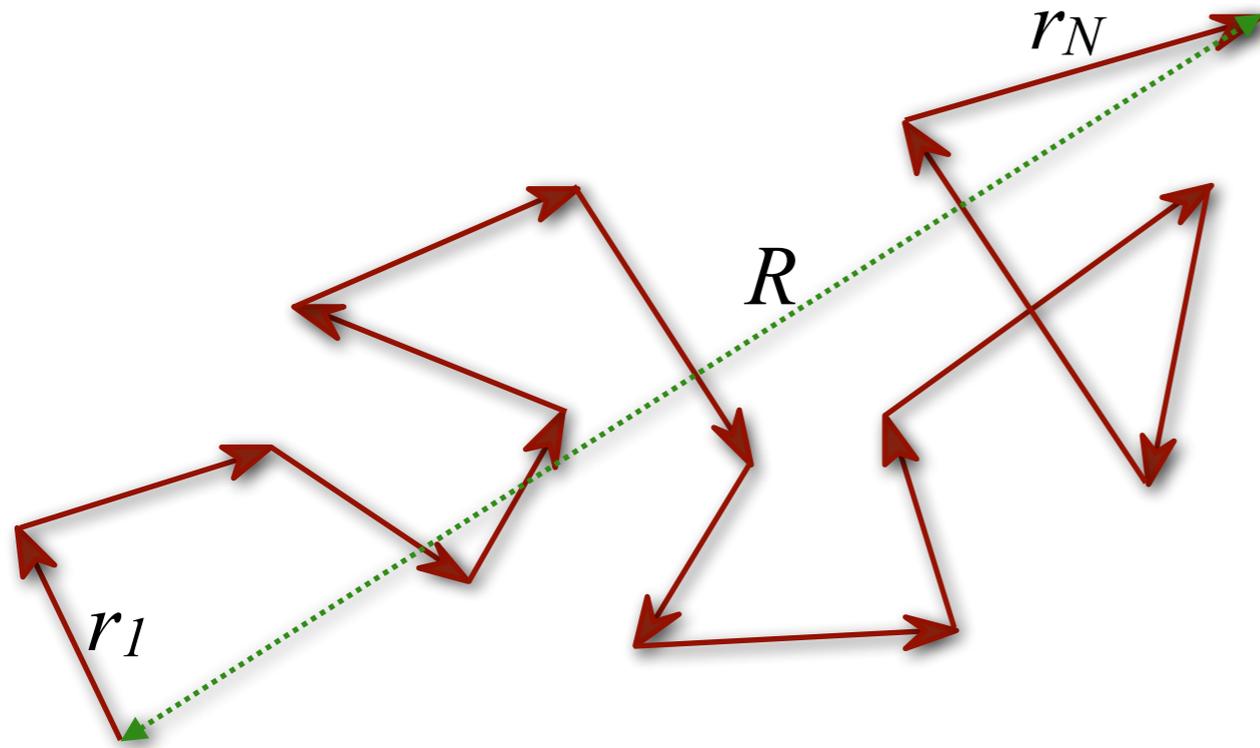
Polymers:  
chains built up from monomers

Number of monomers:  $N \gg 1$ ;  
Typically,  $N \sim 10^2 - 10^4$ ,  
but, in DNA, e.g.:  $N \sim 10^9 - 10^{10}$

<b>Biopolymer</b>	<b>Monomer</b>	<b>Bond</b>
Protein	Amino acid	Covalent (peptide bond)
Nucleic acid (RNA, DNA)	Nucleotide (CTUGA)	Covalent (phosphodiester)
Polysaccharide (e.g., glycogen)	Sugar (e.g., glucose)	Covalent (e.g., $\alpha$ -glycosidic)
Protein polymer (e.g., microtubule)	Protein (e.g., tubulin)	Secondary

# Shape of the polymer chain resembles random walk

Brownian-movement -  
“random walk”



“Square-root law”:

$$\langle R^2 \rangle = Nl^2 = Ll$$

$R$  = end-to-end distance

$N$  = number of elementary vectors

$l = |\vec{r}_i|$  = correlation length

$r_i$  = elementary vector

$Nl = L$  = contour length

$l$  is related to **bending rigidity**.

In case of Brownian-movement  $R$  = displacement,  $N$  = number of elementary steps,  $L$  = total path length, and  $l$  = mean free path length.

# Biopolymer elasticity

## Entropic (thermal) elasticity

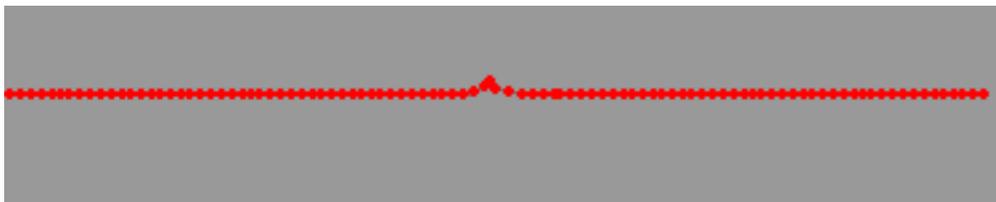
Polymer chain goes through thermal fluctuations of shape.



Configurational entropy (orientational disorder of elementary vectors) increases.



Due to the entropy maximization of the system the chain shortens (end-to-end distance falls below contour length).

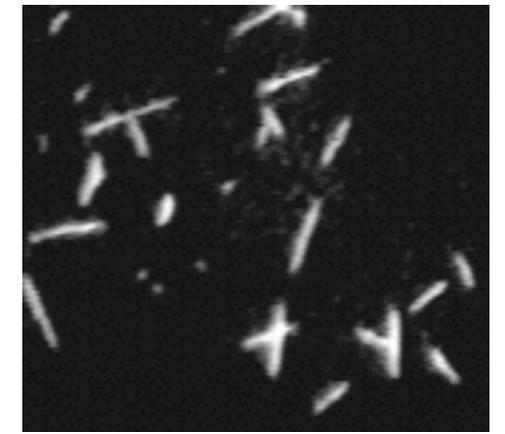


## Relationship between persistence length ( $l$ ) and contour length ( $L$ ) in biopolymers

Rigid chain:  $l \gg L$



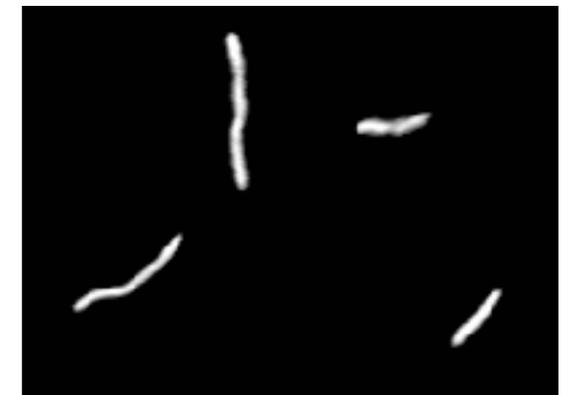
Microtubule



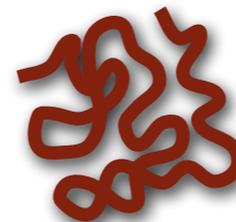
Semiflexible chain:  $l \sim L$



Actin filament



Flexible chain:  $l \ll L$



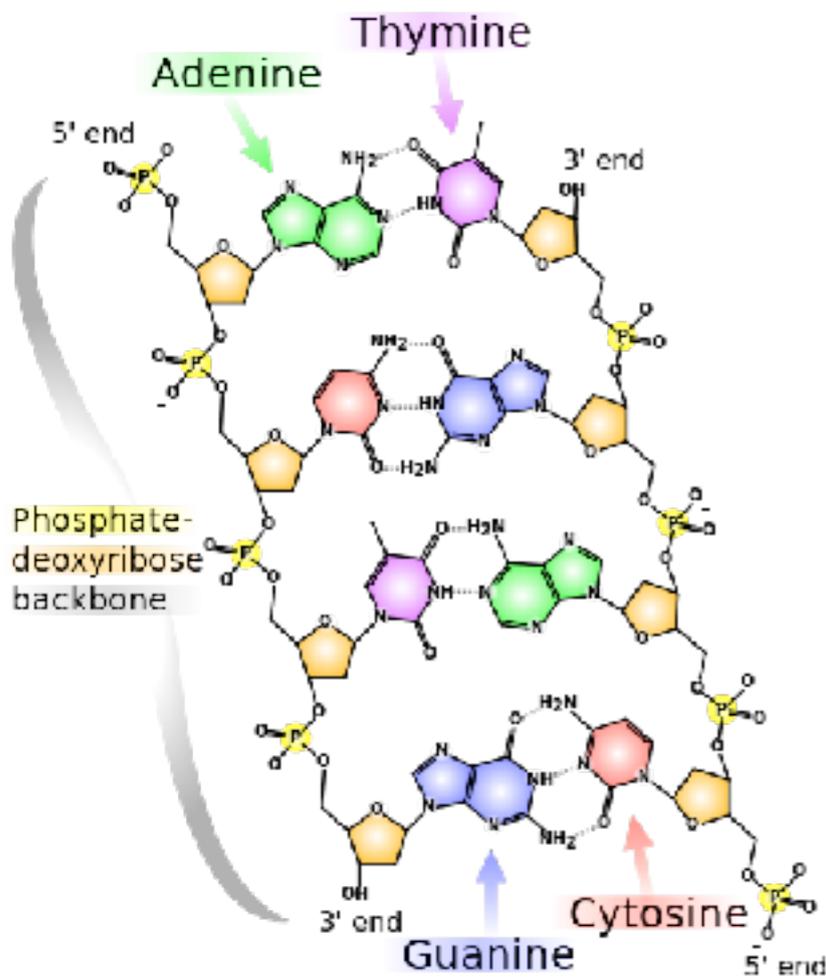
DNA molecule



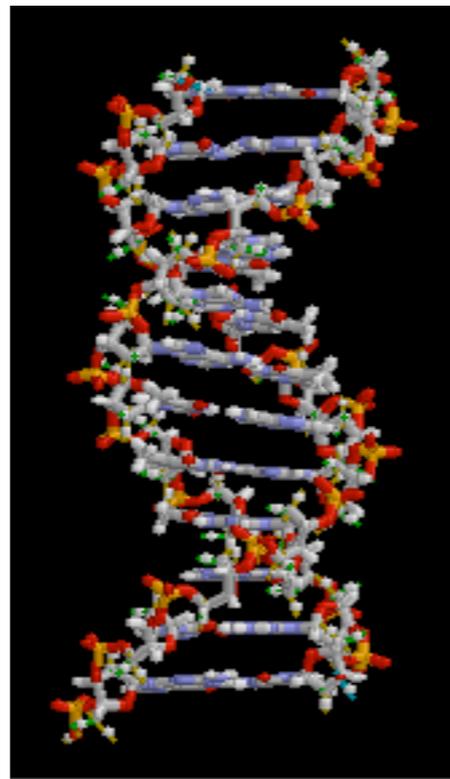
# I. DNA: deoxyribonucleic acid

**Function:** molecule of biological information storage

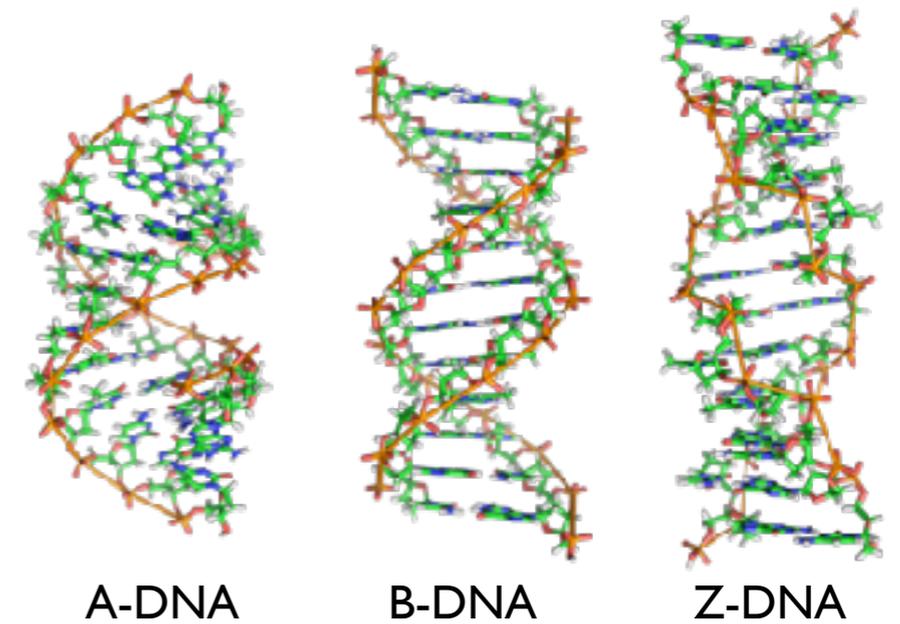
Chemical structure



3D structure: double helix

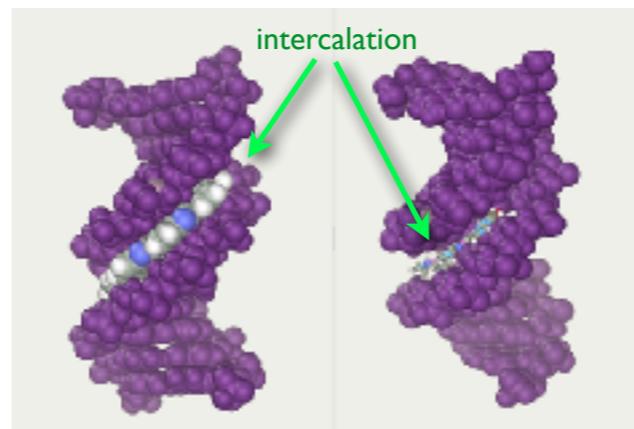


Various DNA structures

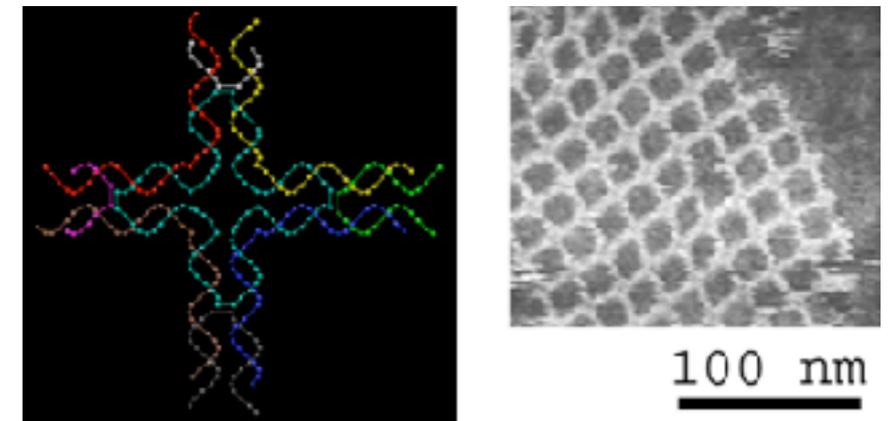


Depends on hydration, ionic environment, chemical modification (e.g., methylation), direction of superhelix

“Watson-Crick” base pairing: via H-bonds  
Gene sequence is of central significance in molecular genetics



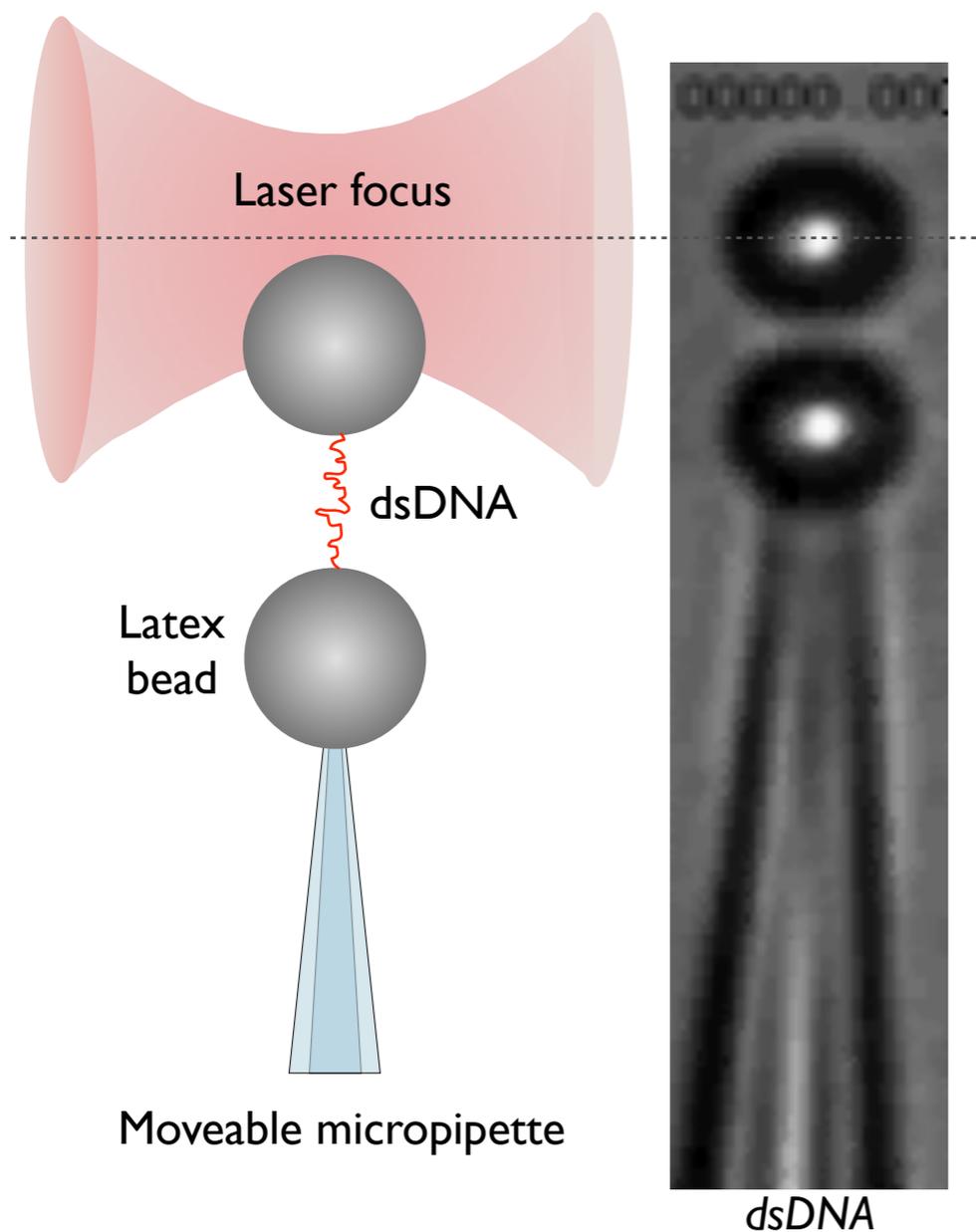
Large groove      Small groove



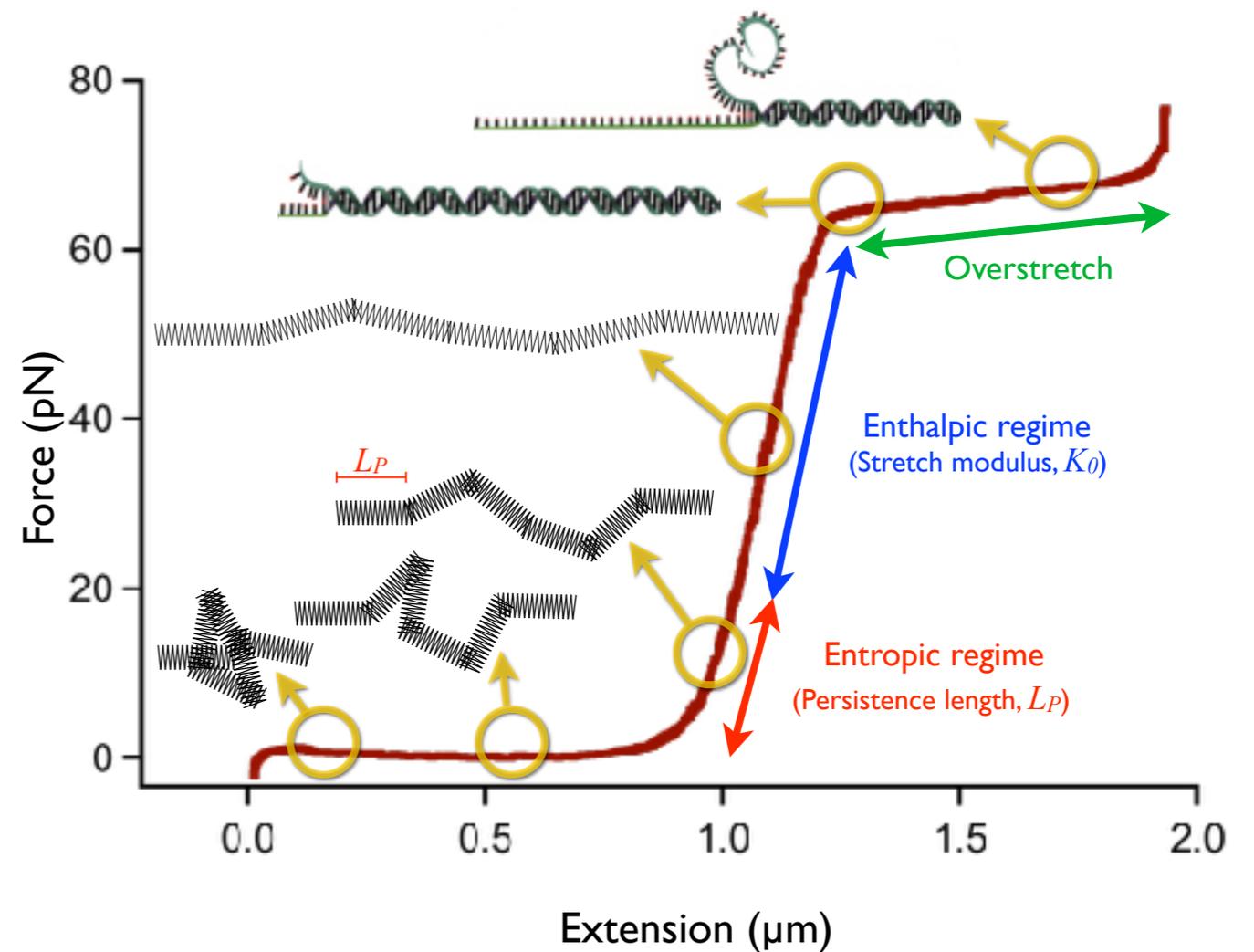
DNA nanostructures (origami)  
Depends on base-pairing order and hierarchy

# The DNA molecule is elastic!

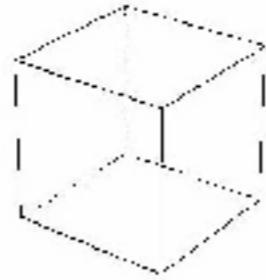
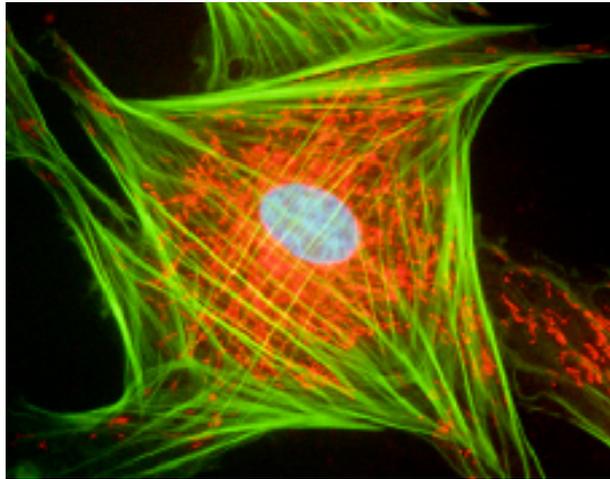
Force measurement: with optical tweezers



Force versus extension curve of a single dsDNA molecule



# How much DNA is in a cell?

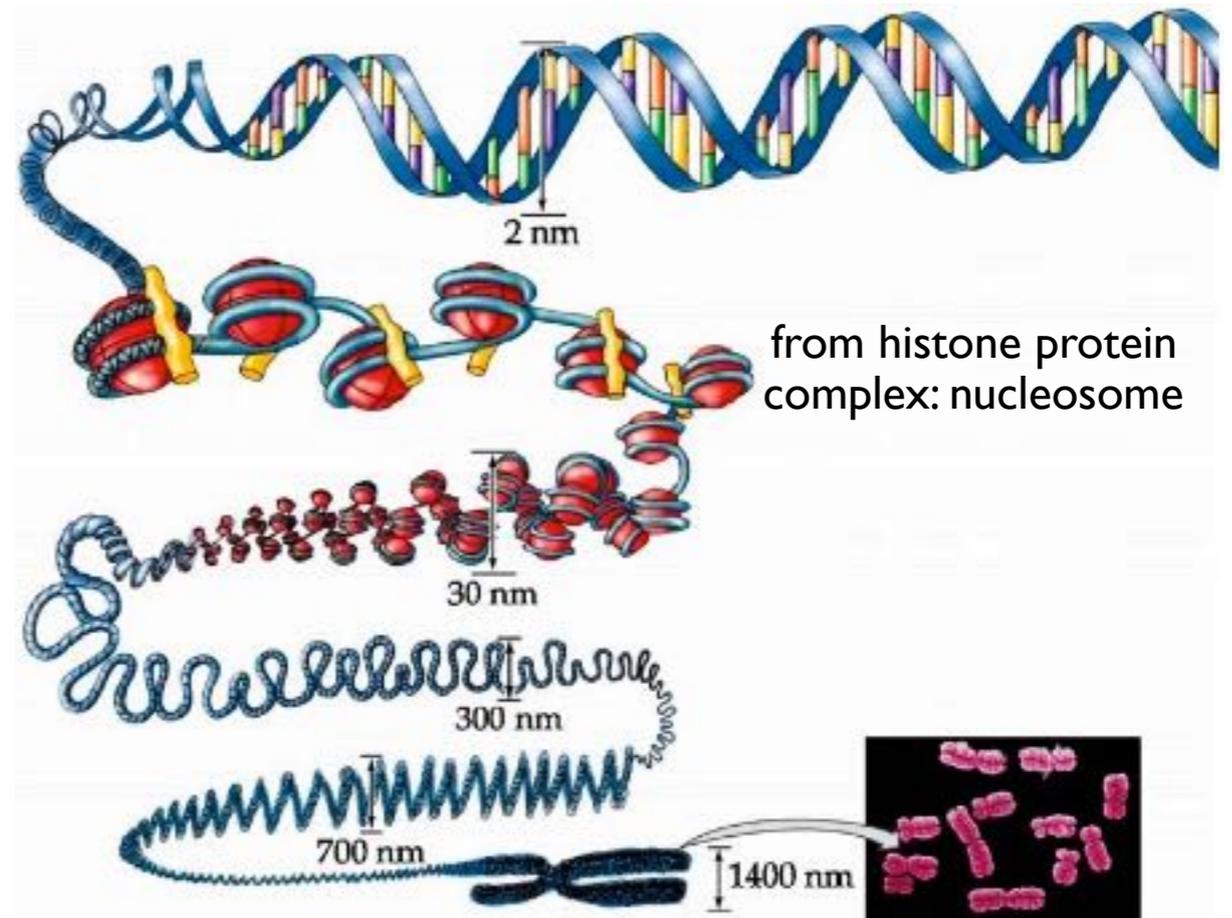


Simplified cell model: cube

**Solution:** DNA needs to be packed

Chromosome condensation

	<b>Cell:</b> 20 $\mu\text{m}$ edge cube	Analog - <b>Lecture hall:</b> 20 m edge cube
DNA thickness	2 nm	2 mm
Full length of human DNA	$\sim 2$ m	$\sim 2000$ km (!!!) (Perimeter of Hungary: $\sim 2200$ km)
Persistence length of dsDNA	$\sim 50$ nm	$\sim 50$ cm
End-to-end distance (R)	$\sim 350$ $\mu\text{m}$ (!)	$\sim 350$ m (!)
Volume of fully compacted DNA	$\sim 2 \times 2 \times 2$ $\mu\text{m}^3$	$\sim 2 \times 2 \times 2$ $\text{m}^3$ (= 8 $\text{m}^3$ )

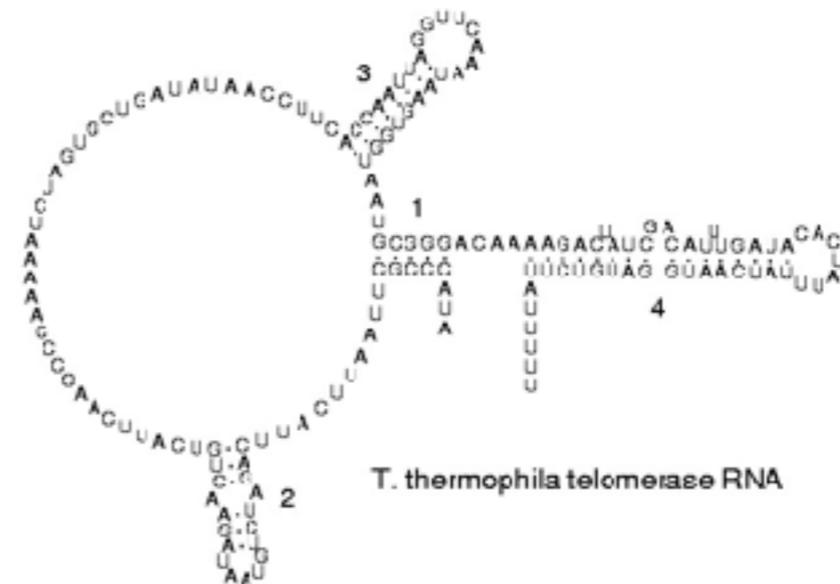
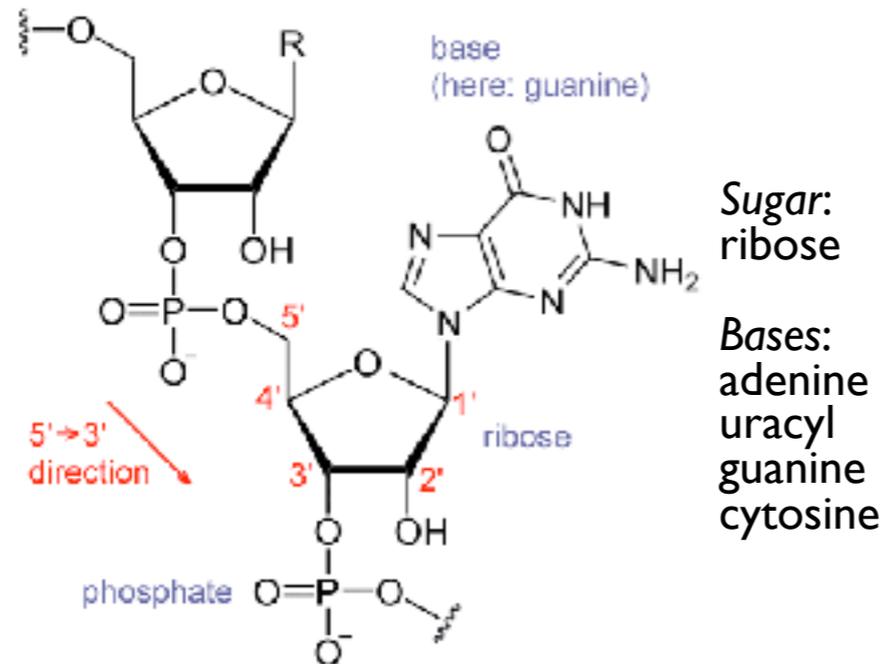


- **Condensins** play a role in high-order DNA packaging
- DNA chain: complex linear path with roadblocks!

# 2. RNA: Ribonucleic acid

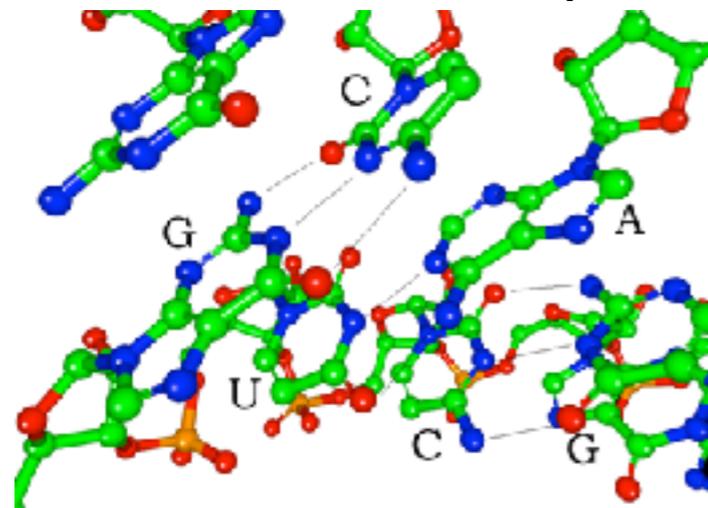
**Function:** information transfer (transcription), structural element (e.g., ribosome), regulation (turning gene expression on and off)

Chemical structure

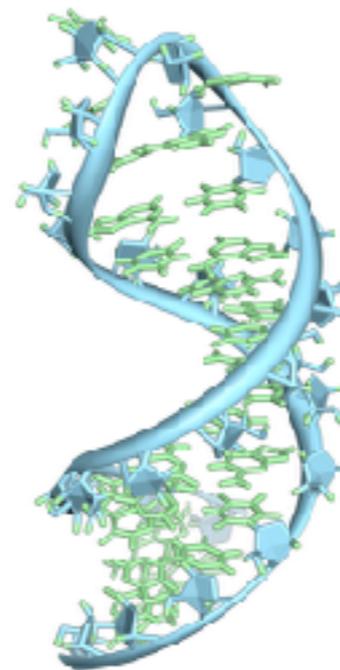


Secondary and tertiary structural elements

“Watson-Crick” base pairing



RNA hairpin

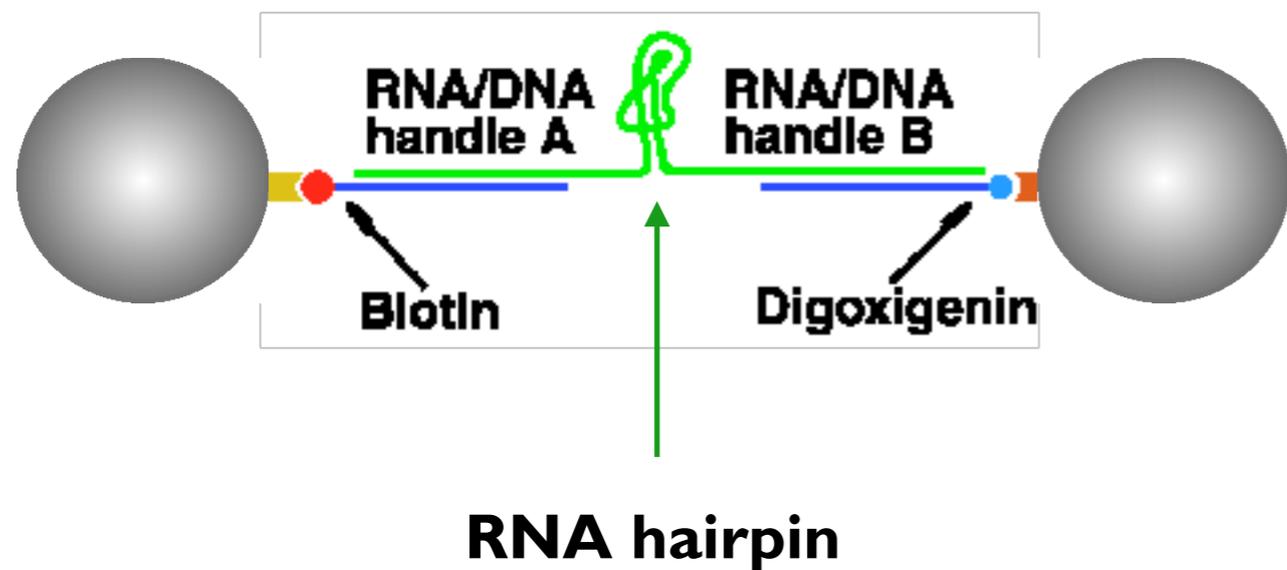


Complex structure (ribozyme)

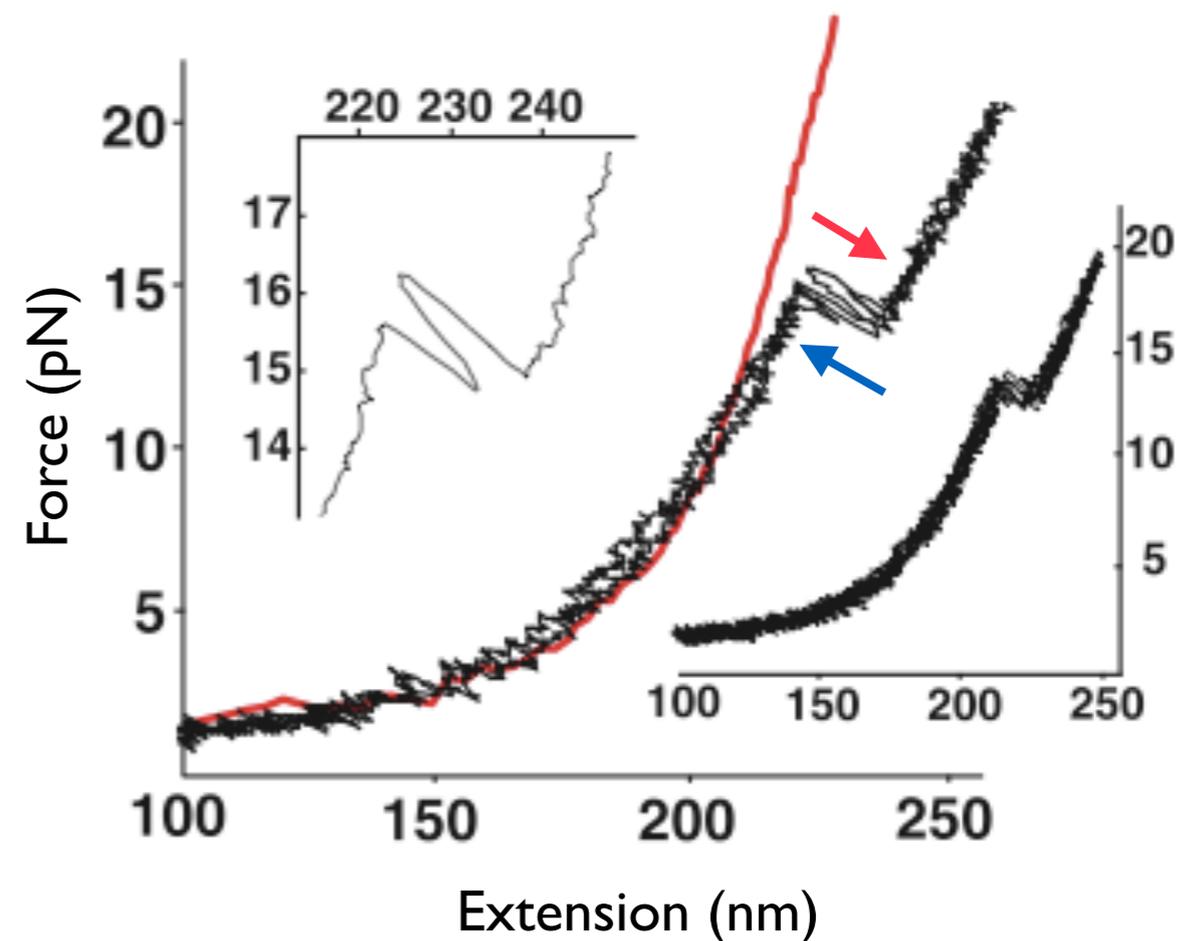


# RNA structure can be perturbed with mechanical force

Mechanical stretching with optical tweezers

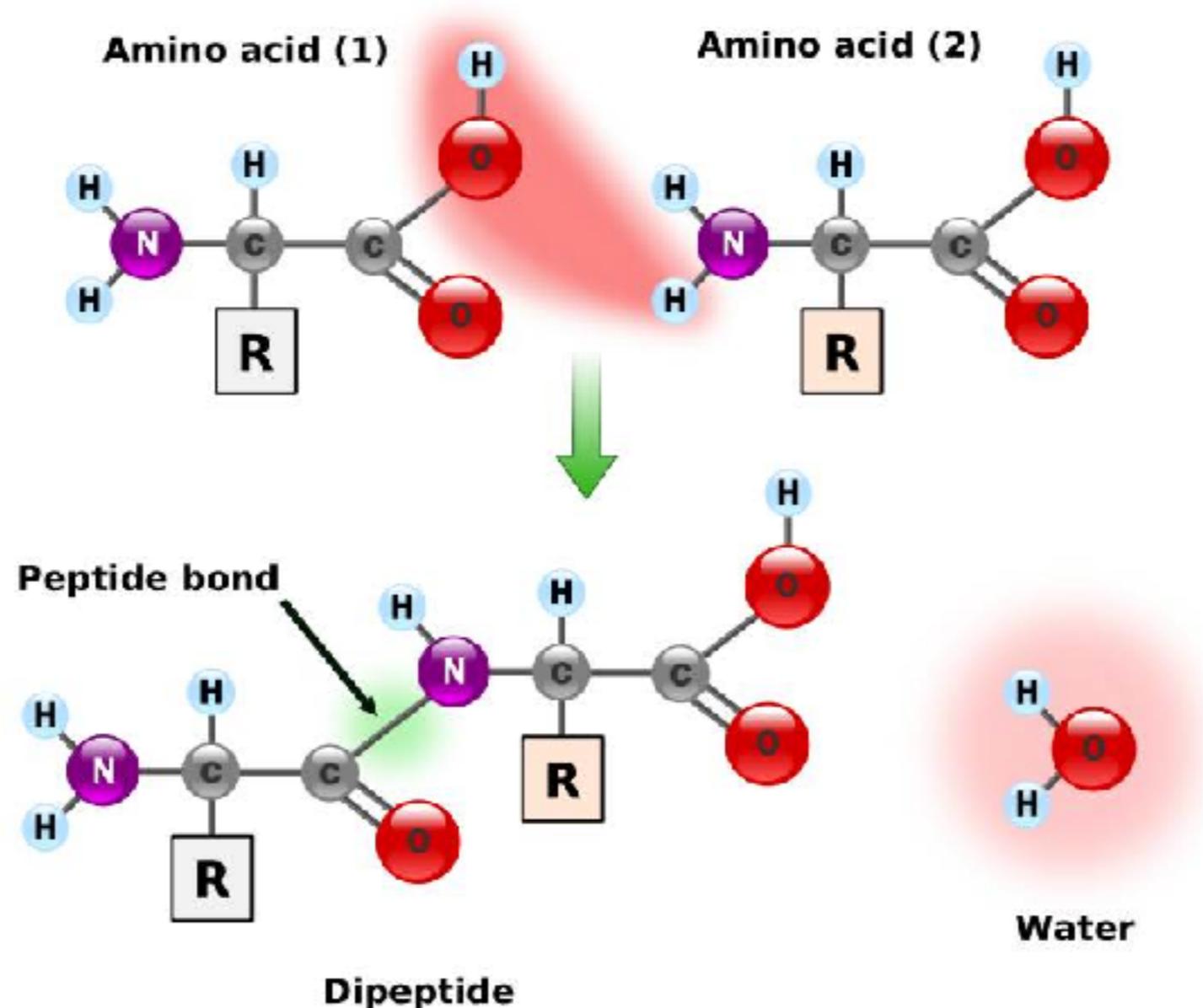


Mechanical **unfolding** of an RNA hairpin: nearly reversible process - the RNA rapidly **folds** when relaxed



# 3. Proteins: polymers connected with peptide bonds

**Function:** most important molecules of the cell. Highly diverse functions - structure, chemical catalysis energy transduction, motoric functions, etc.



Formation of the peptide bond: condensation reaction followed by the release of water

# Protein structure

## Primary

Amino acid sequence

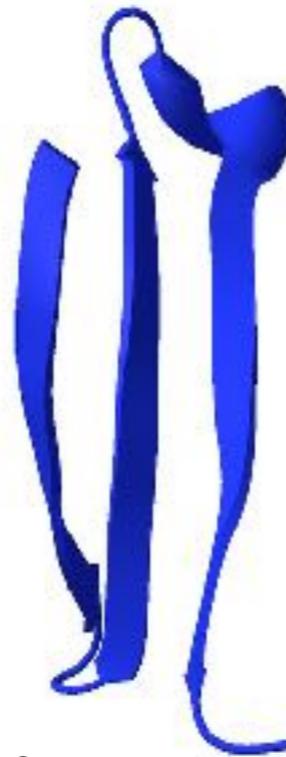
Determines spatial structure as well.

## Secondary

$\alpha$ -helix  
 $\beta$ -sheet  
 $\beta$ -turn ( $\beta$ -hairpin)



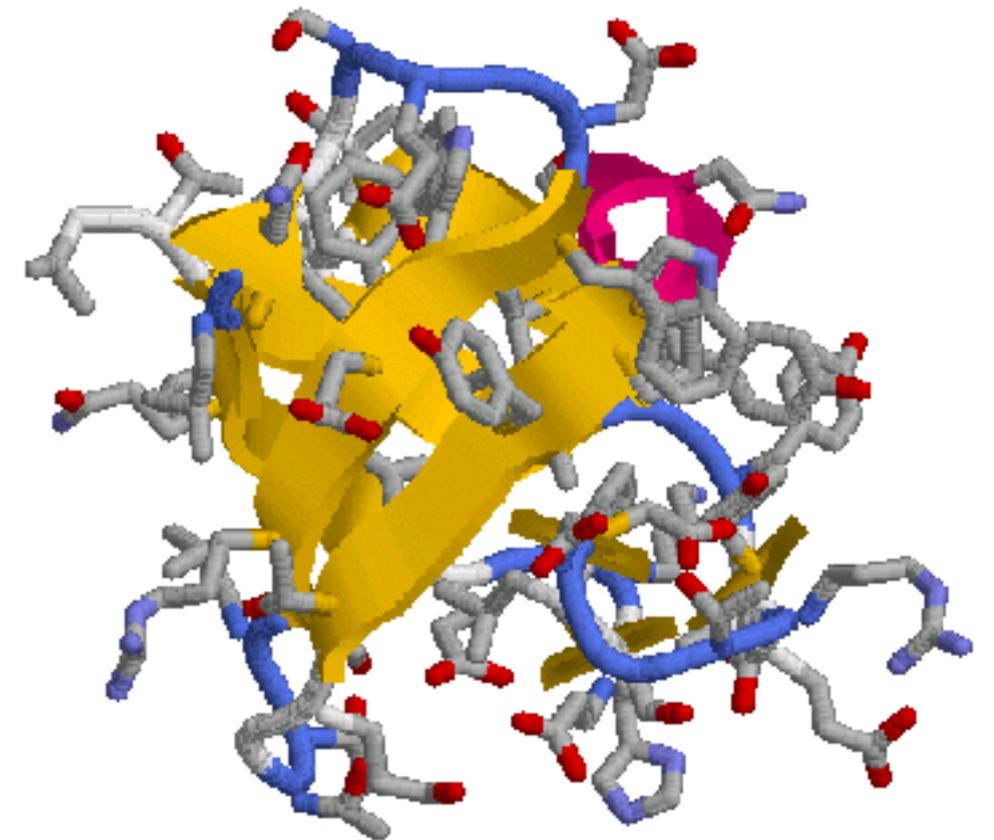
$\alpha$ -helix:  
•right handed  
•3.4 residue/turn  
•H-bridges



$\beta$ -sheet:  
•parallel or  
•antiparallel  
•H-bridges between distant residues

## Tertiary

3D structure of single-chain protein



\*Quaternary structure: binding of independent subunits into a complex

# Bonds holding protein structure together

- 
- Weak (secondary) bonds
1. **Hydrogen bond**: proton sharing between proton-donor side chains.
  2. **Electrostatic interaction** (salt bridge): between oppositely charged residues.
  3. **van der Waals bond**: weak interaction between atoms (molecules) with closed electron shells.
  4. **Hydrophobe-hydrophobe interaction**: between hydrophobic residues (in the interior of the molecule).
  5. **Disulfide bridge**: between cysteine side chains; connects distant parts of the protein chain.
- Covalent bond

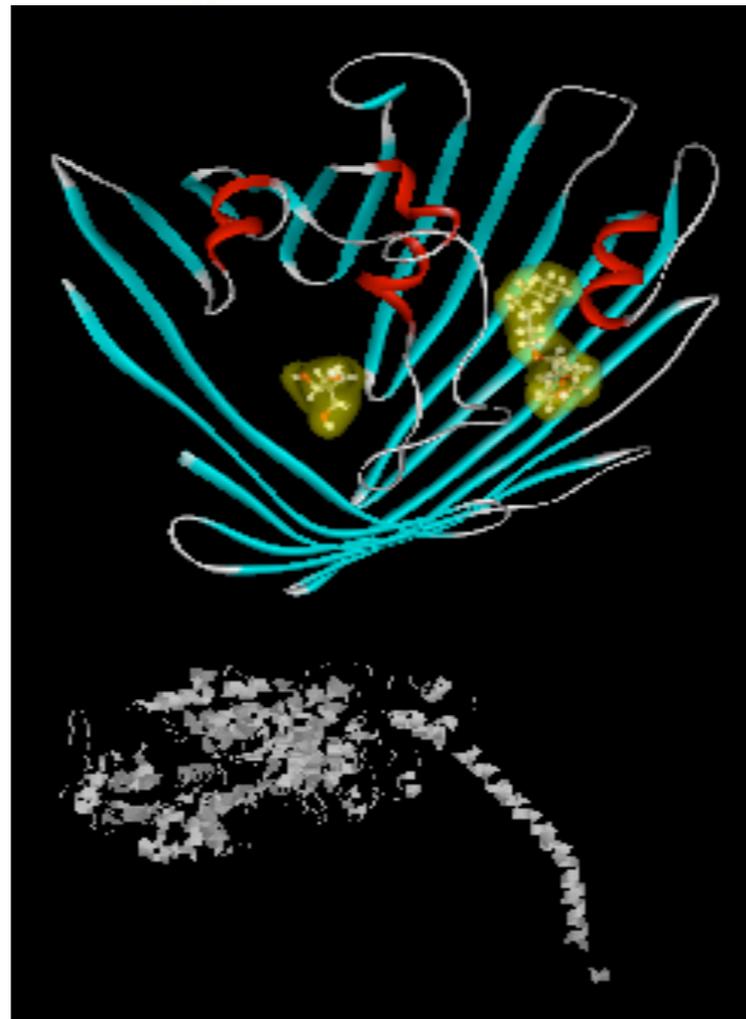
# Protein structure classes

1. All alpha



calmodulin

2. All beta



porin

(3. Alpha-beta)

4. Multidomain

Domain:  
folding subunit

myosin

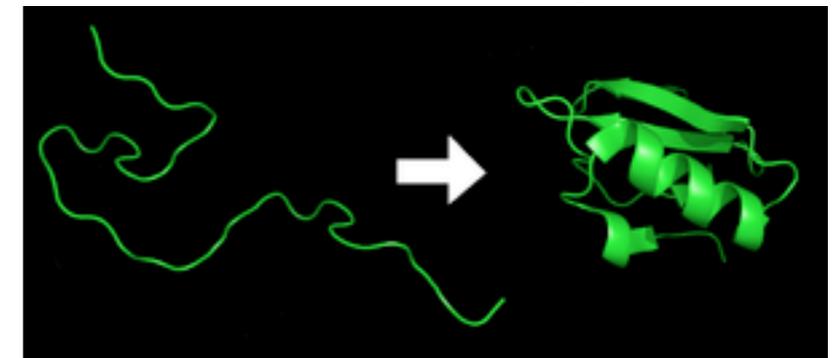
Although there are as many sequences as proteins, the spatial structures are classified into a surprisingly small number of classes!

# How is the three-dimensional structure acquired?



Christian Anfinsen  
(1916-1995)

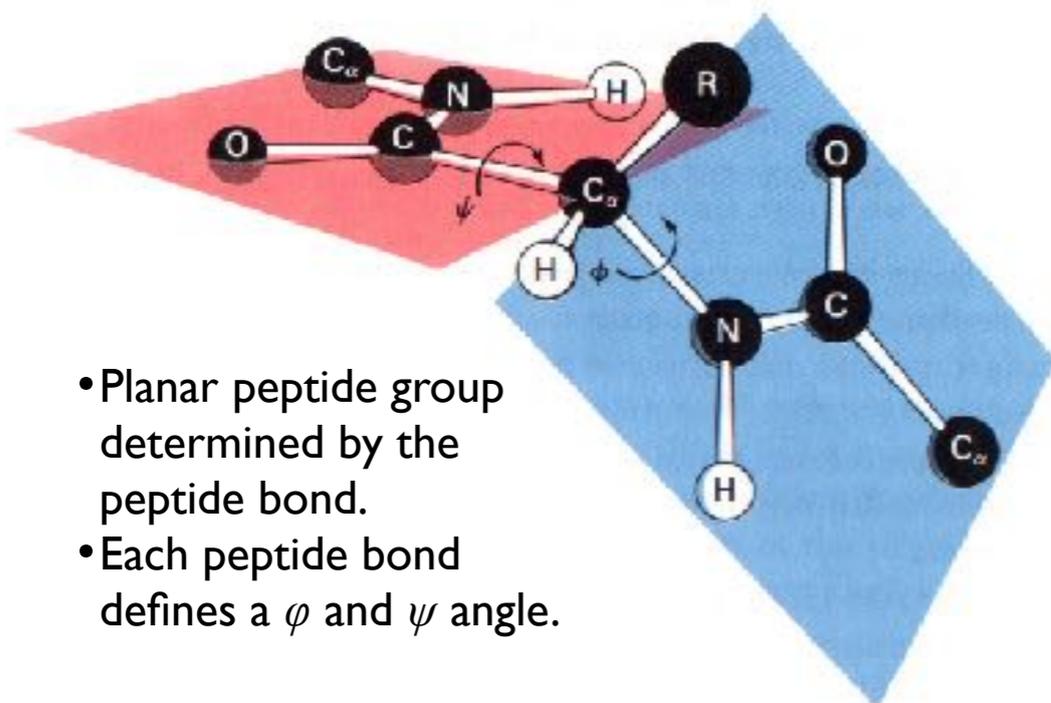
**Anfinsen:** proteins fold spontaneously (sequence determines structure)



Unfolded state

Native state (N)  
Lowest energy

**Levinthal's paradox** (Cyrus Levinthal, 1969):  
Are all available conformations explored?

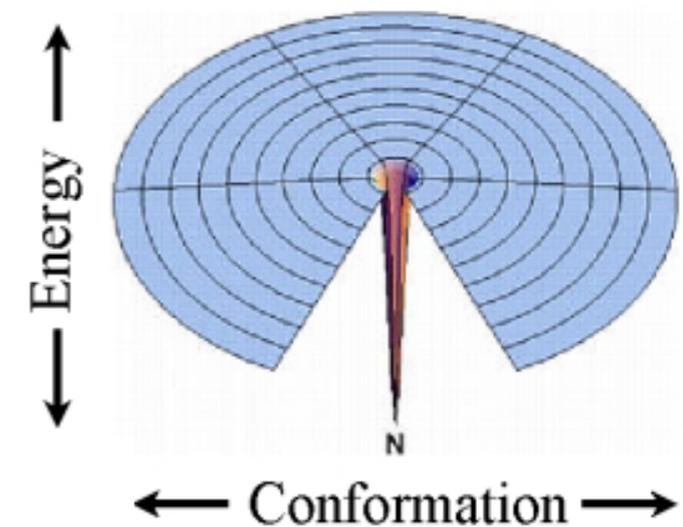


Number of possible conformations (degrees of freedom):

$$i^n$$

$i$  = number of possible angular positions of a given  $\phi$  or  $\psi$  angle  
 $n$  = total number of  $\phi$  and  $\psi$  angles

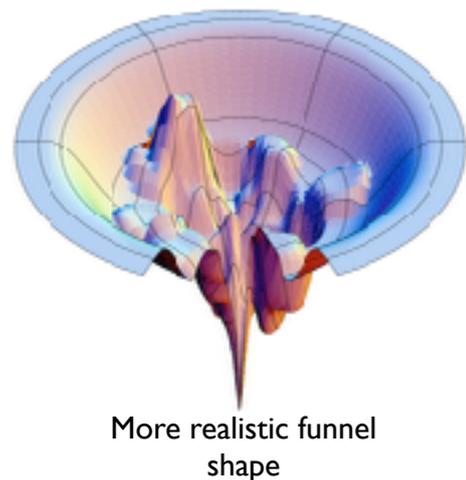
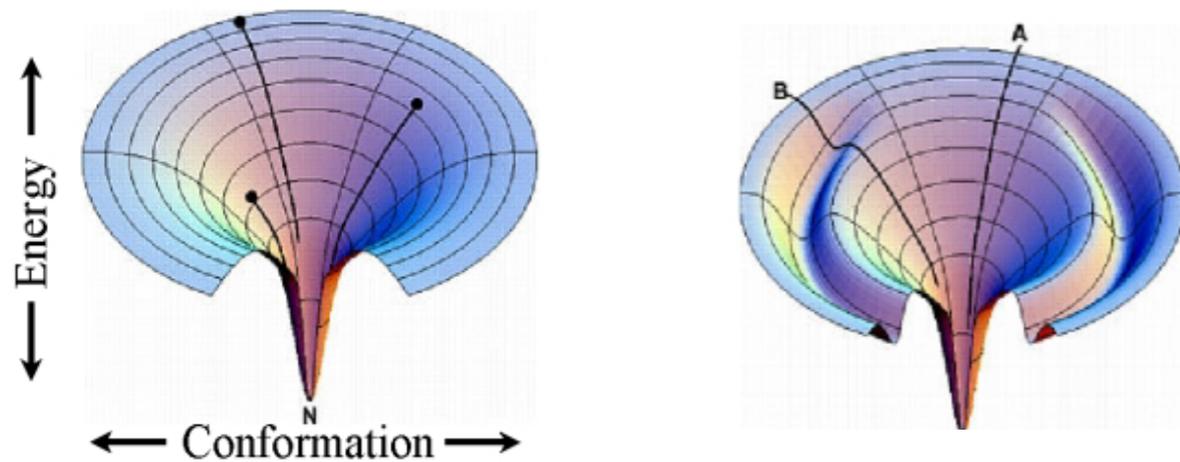
Example: in a peptide composed of 100 residues the number of possible  $\phi$  or  $\psi$  angles is 2.  $n=198$ . Number of possible conformations:  $2^{198}$ (!!!)



What is the probability that a billiards ball will find the hole merely via random motion?

# Protein folding is guided by the shape of its conformational space

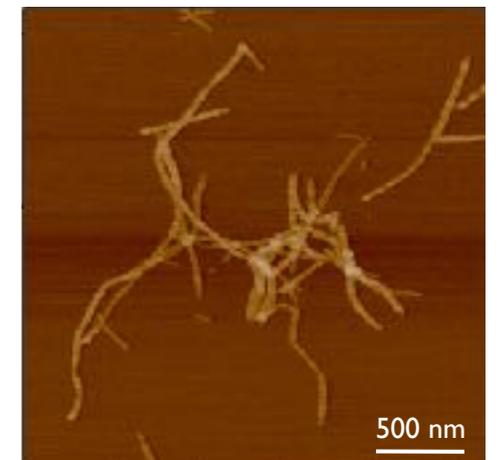
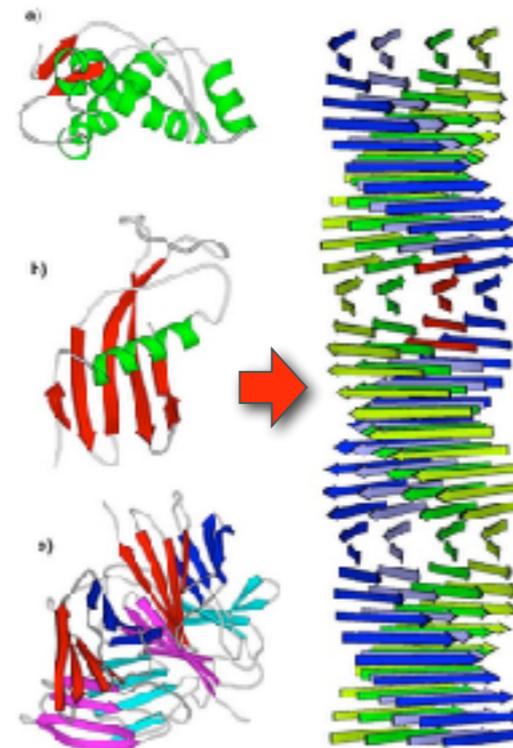
## Shape of conformational space: “Folding funnel”



- Proteins “slide down” the wall of the funnel.
- Folding funnel shape can be complex (determination of the shape is usually very difficult).
- A protein may get stuck at intermediate states (pathology).
- In the living cell chaperones assist folding.

## Pathology

- Protein “folding diseases”
- Alzheimer’s disease
- Parkinson’s disease
- II-type diabetes
- Familial amyloidotic neuropathy

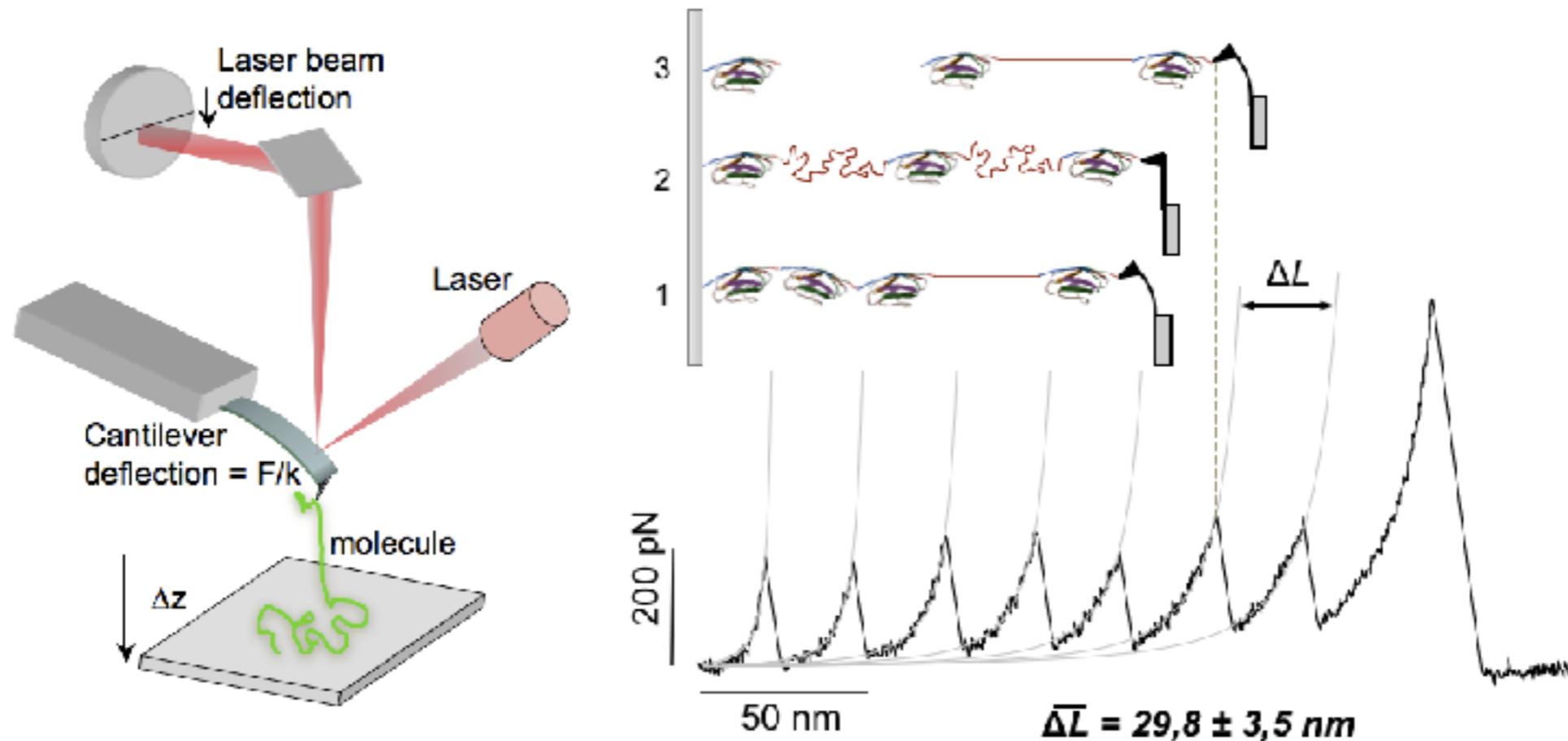


$\beta$ -fibrils:  
undissolved precipitate  
cross- $\beta$  structure

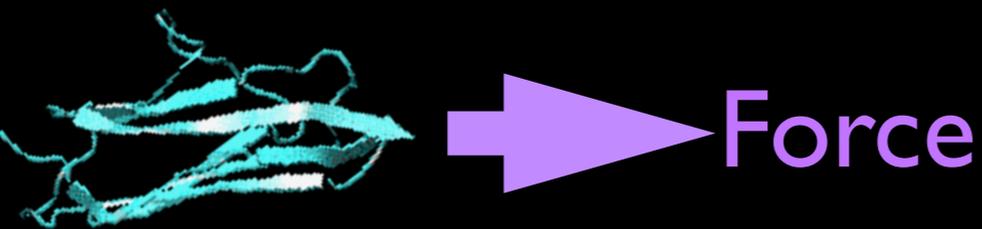
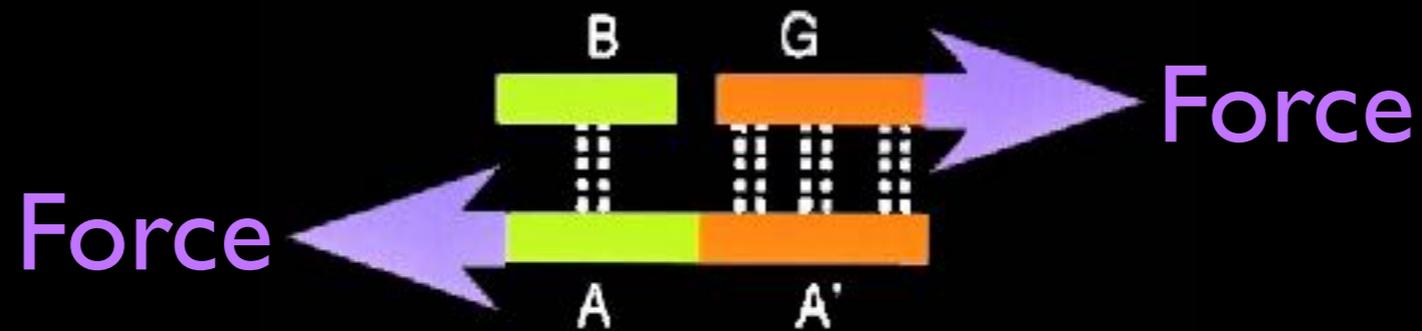
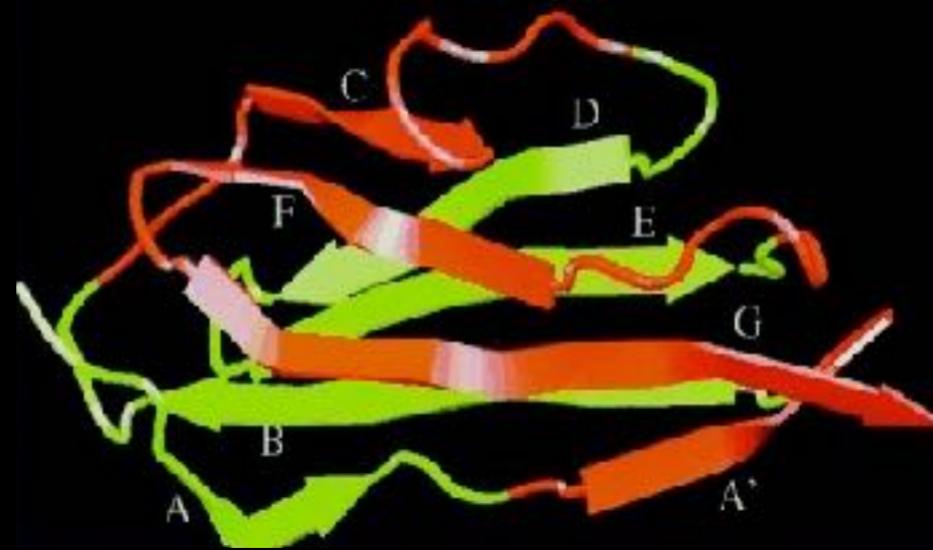
# Methods of protein unfolding (denaturation)

- Heat Break secondary chemical bonds
- Chemical agent Disrupt secondary and tertiary structure
- Mechanical force

Mechanical unfolding of a single protein with atomic force microscope

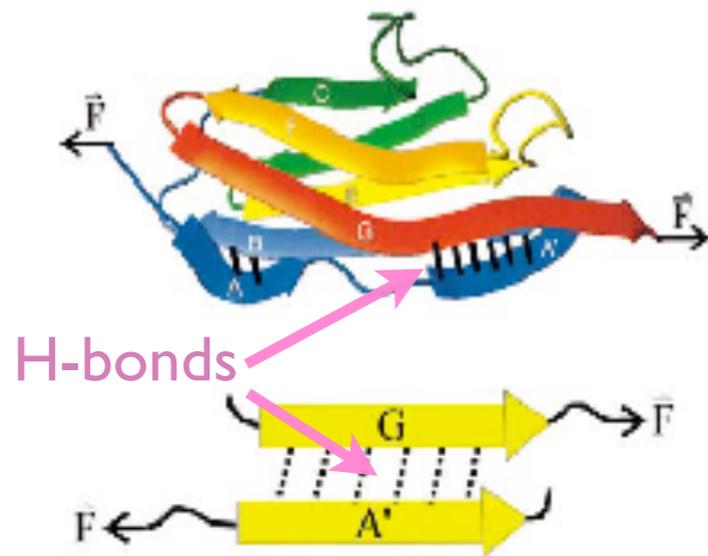


# Structural basis of mechanical stability

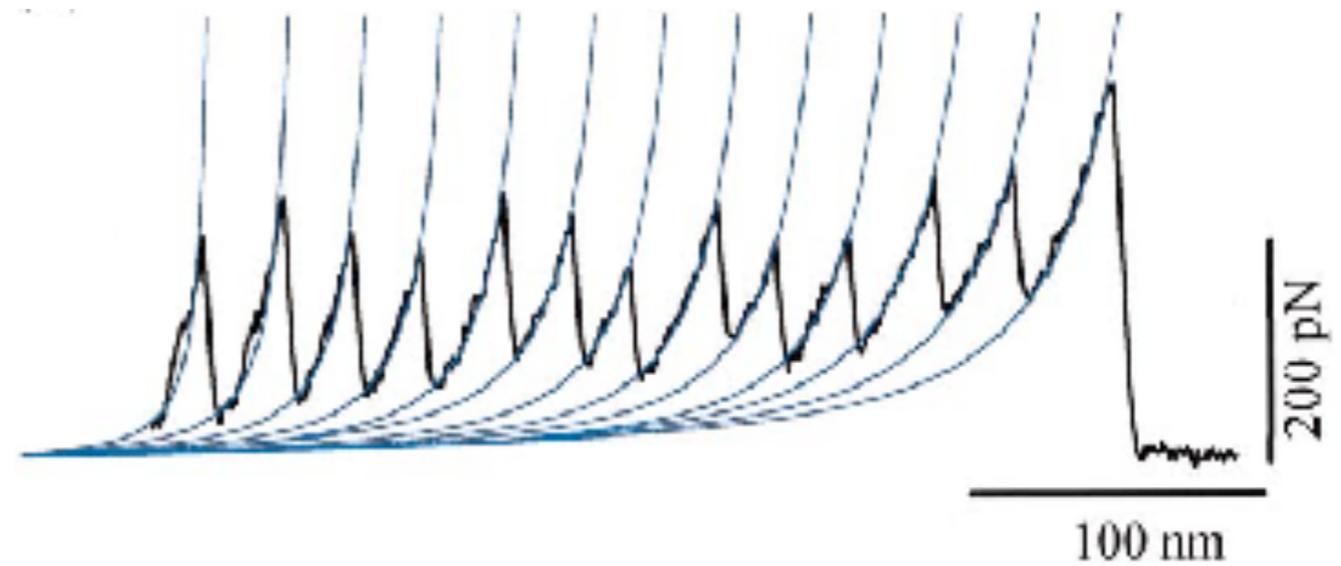


# Biological logic of mechanical stability

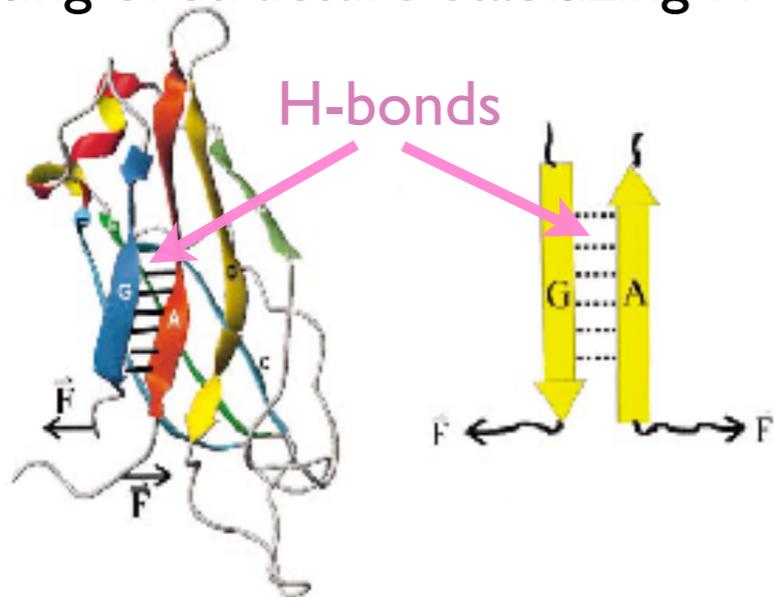
Parallel coupling of structure-stabilizing H-bonds



High unfolding forces



Serial coupling of structure-stabilizing H-bonds



Low unfolding forces

