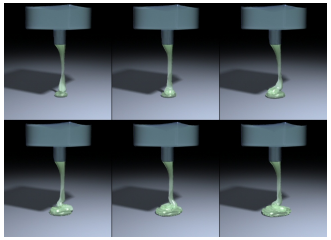
stiffness flexible ↔ stiff	Young-modulus, E (Pa)
elasticity rigid ↔ elastic	elastic strain recovery, ε_r resilience, w_r (J/m^3)
ductility not ductile↔ ductile	$\varepsilon_y - \varepsilon_s$
strength weak ↔ strong	σ_s (Pa)
toughness not tough (brittle) ↔ tough	toughness, w_s (J/m^3)
Hardness soft ↔ hard	hardness scales, HB, HV, HK („Pa")

1



Physical bases of dental materials science

9.

Viscoelasticity

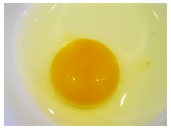
Keynotes:
- ❖ *Viscoelastic behavior*
- ❖ Viscoelastic models
- ❖ Viscoelastic phenomena

E-book chapter: 18

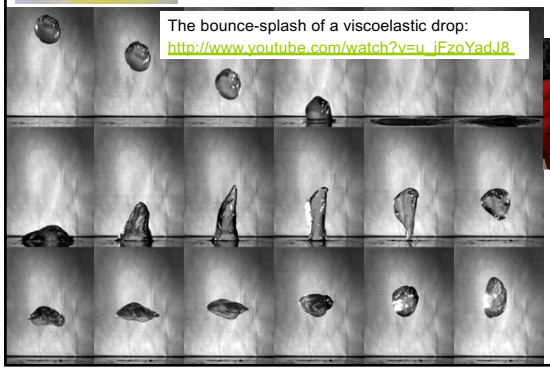
2

2

Viscoelasticity



The bounce-splash of a viscoelastic drop:
http://www.youtube.com/watch?v=u_jFzoYadJ8



3

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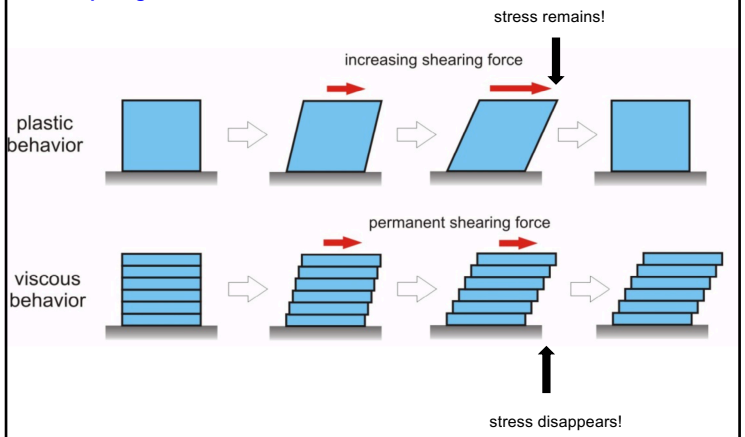
Comparing elastic and viscous behavior:



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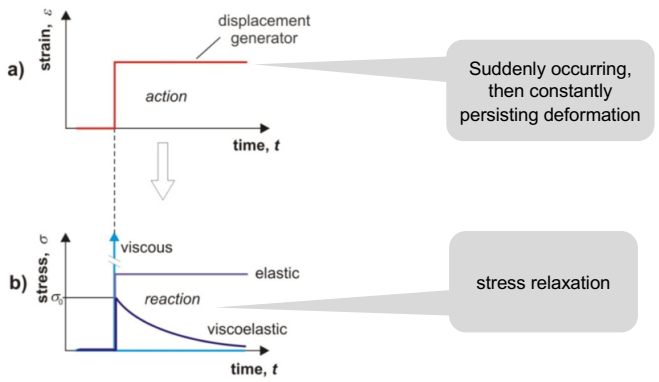
Viscoelasticity



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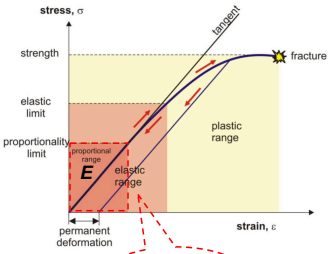
Reminder:

Elastic behavior:

- sudden
- force is required to maintain strain



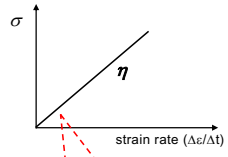
Hooke's law: $\sigma = E\varepsilon$

Hooke-body
E

Ideally elastic body

Viscous behavior

- time dependent
- force is required to maintain stress rate



Newton's law: $\sigma = \eta \frac{\Delta\varepsilon}{\Delta t}$

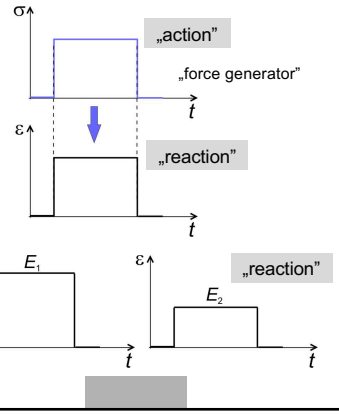
Newton-body
η

Ideally viscous body

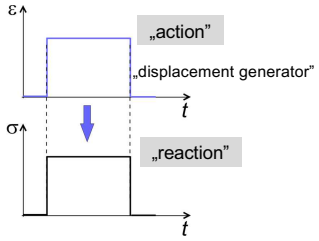
6

Ideal elastic behavior

How would strain change in case of constant stress?



How would stress change in case of constant strain?

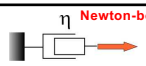


stress is constant
(no stress relaxation)

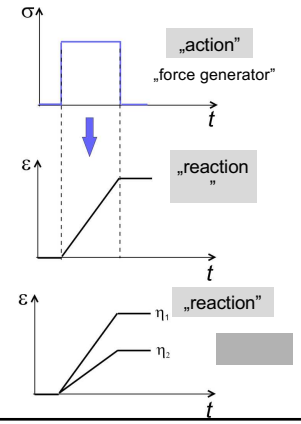
7

7

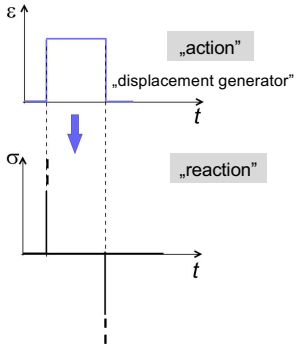
Behavior of an ideally viscous body



How would strain change in case of constant stress?



How would stress change in case of constant strain?



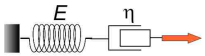
sudden stress relaxation

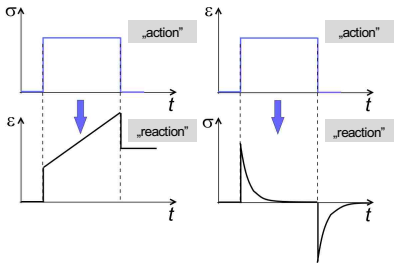
8

8

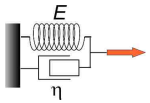
Viscoelastic models

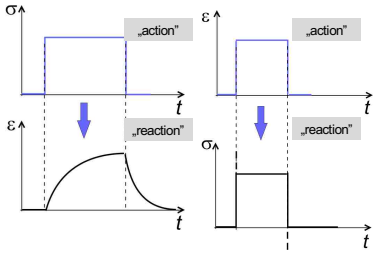
Maxwell-model





Kelvin-Voigt-model





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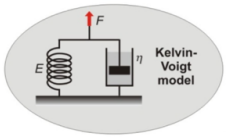
Viscoelasticity

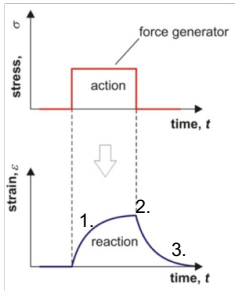
(mechanical model)



Viscoelasticity means the co-appearance of viscous and elastic behavior.

model: parallel connection of spring and dashpot (Kelvin-Voight model)

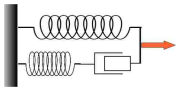
Spring: ideal elastic (Hooke) body
Dashpot: ideal viscous (Newton) body

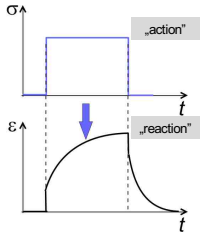


1. Upon stretch, the extension of the spring is slowed down by the dashpot.
2. Extension stops when the elastic spring force equals the external force.
3. When the external force is quenched, the contraction of the spring is slowed down by the dashpot.

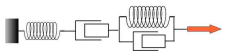
10

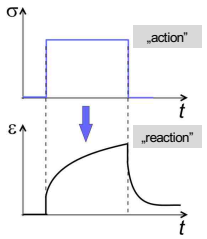
Standard linear modell





Burgers-modell





11

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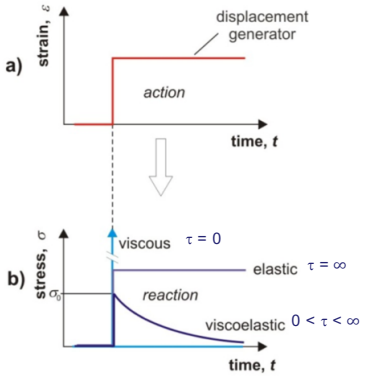
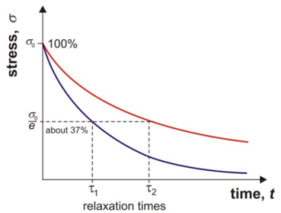
1./a Stress-relaxation in viscoelastic system

Decrease in stress while strain remains constant

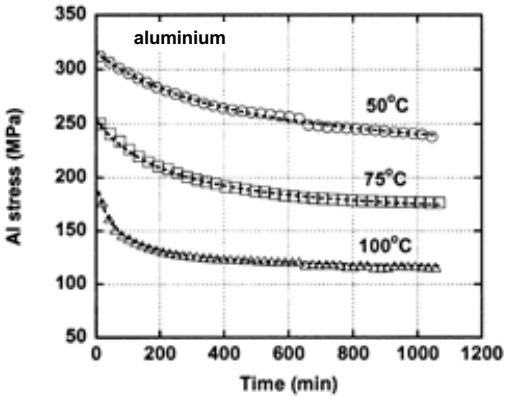




$$\sigma = \sigma_0 \cdot e^{-\frac{t}{\tau}}$$

$$\tau = \frac{\eta}{G} \qquad G = \frac{E}{2(1+\mu)}$$

12



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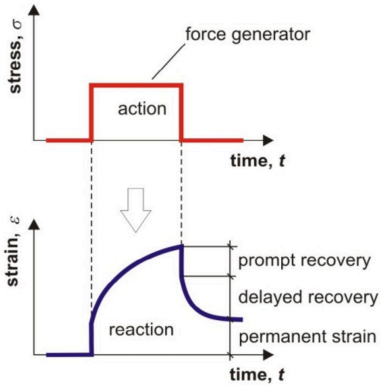
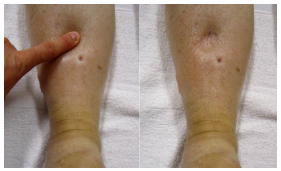
1./b Shape relaxation (recovery)

Recovery of shape after the stress is quenched.





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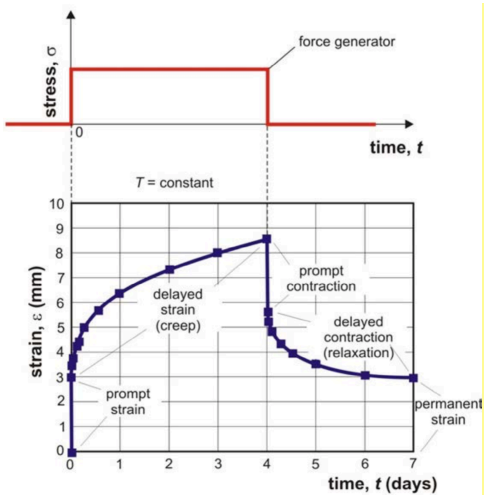
bone cement



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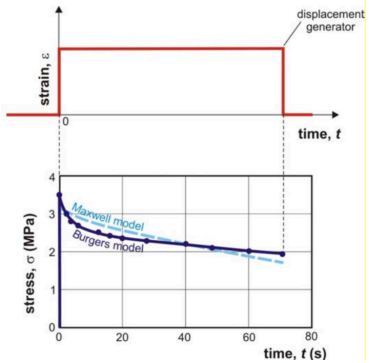
film made of miofibrillar proteins:



16

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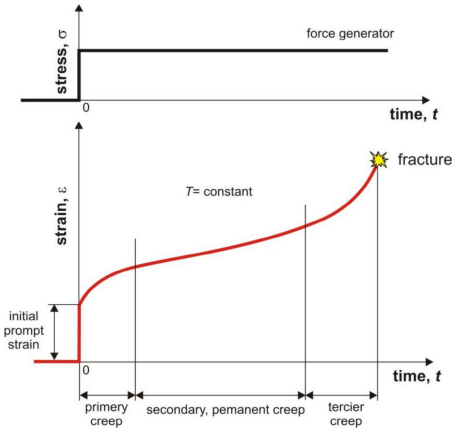
2. Creep

Continuously increasing strain upon constant long-time stress.

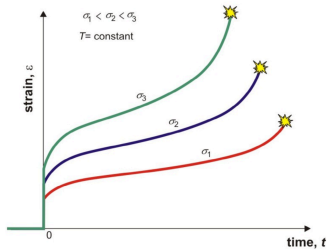


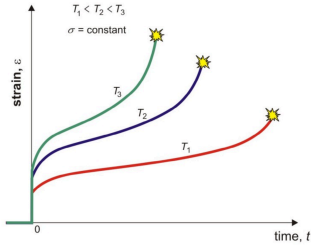
Modell: ? — Maxwell
— Burgers

$1–10^7$ s !!

17

17





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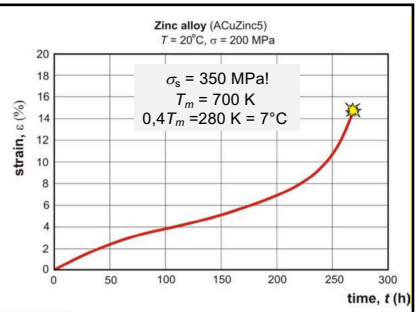
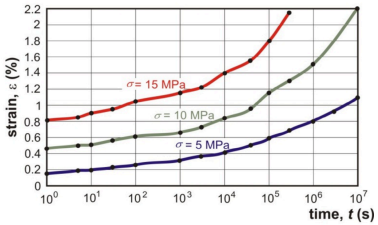
Effect of temperature on creep!. in case of metals it is signifficant if:
$0{,}4T_m < T$



Polypropilene:



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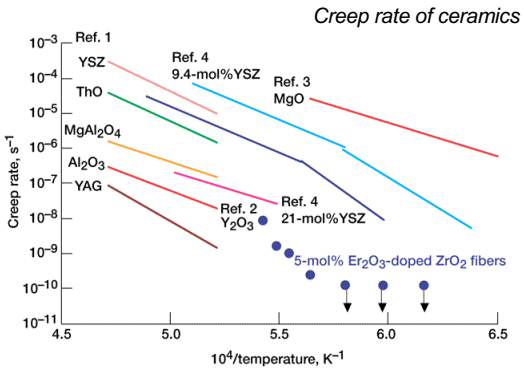

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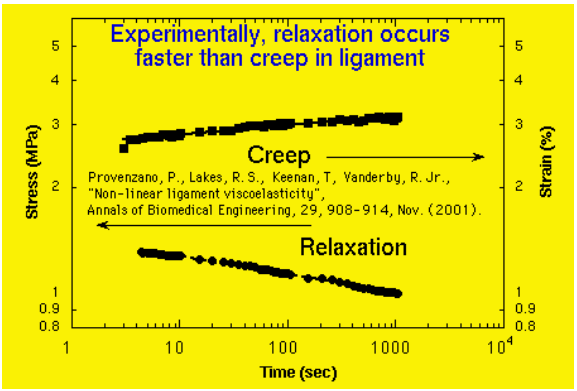

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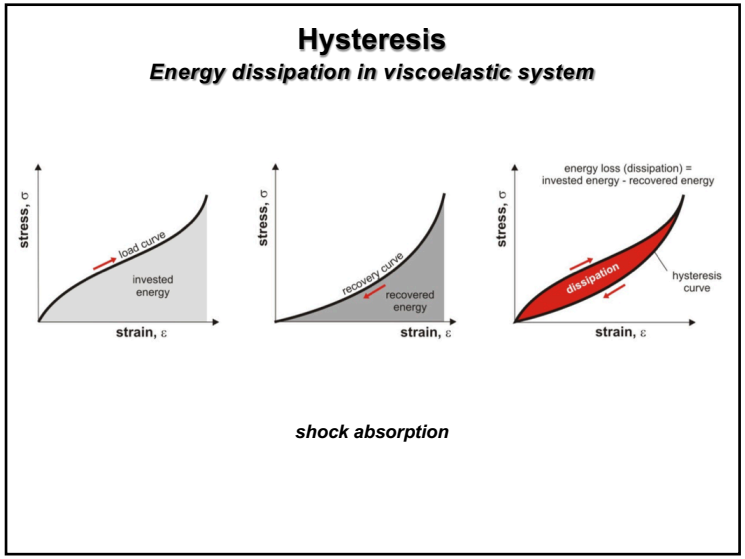

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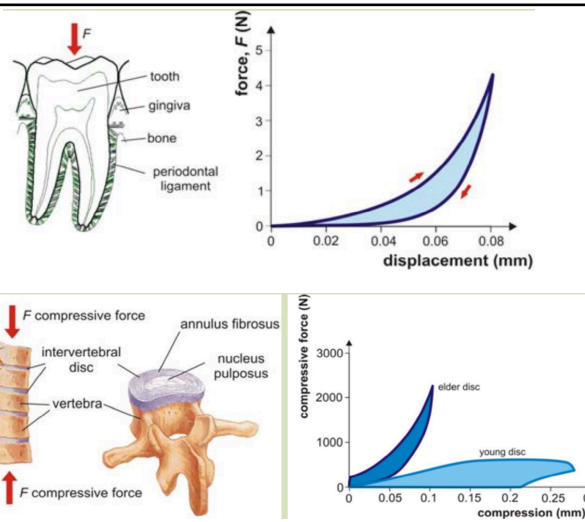

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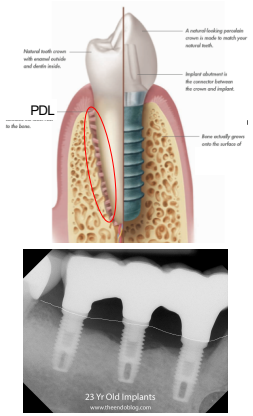
Example II: Implant vs. Natural tooth?

The difference is the periodontal ligament (PDL)!



Absence of PDL results in:
loss of masticatory force perception
loss of viscoelastic dampening
loss of force sensory mechanism
no implant movement

Implant is in direct contact with bone tissue

⇩

Increased compressive stress during mastication

⇩

Bone loss (0.2 mm /year)
Loss of gingival height

Implants ⟺ Root canal treatment

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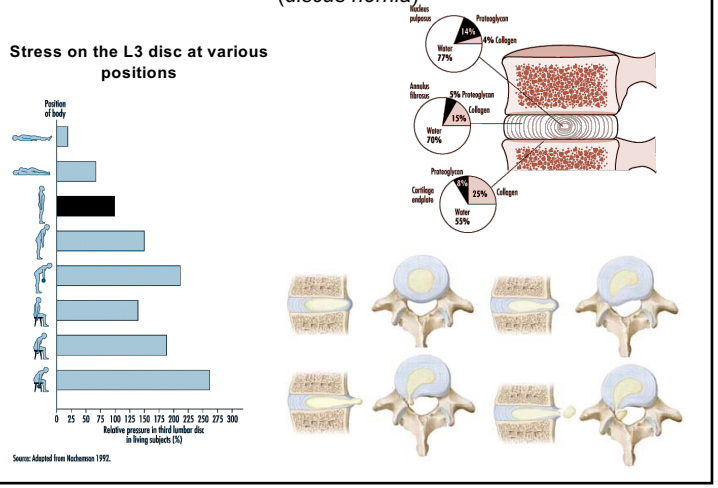
Example I: Consequence of mechanical stress on intervertebral discs
(*discus hernia*)



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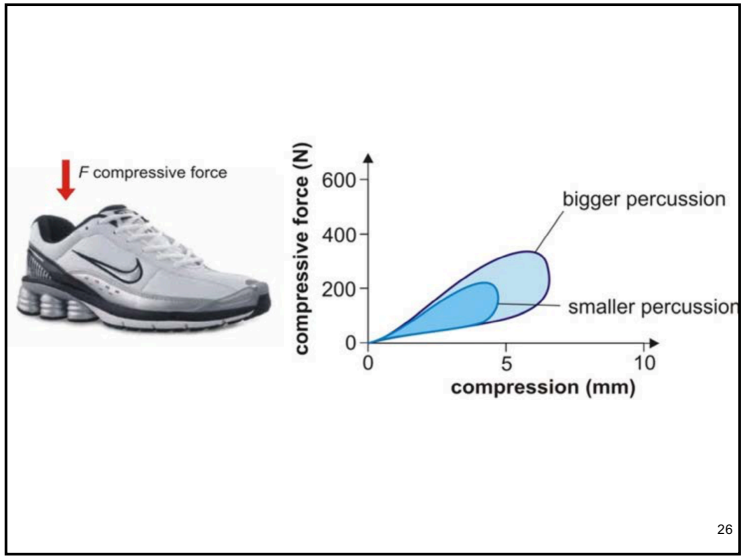

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