

Modelling of ligand-protein binding

I. Computation of thermodynamic quantities

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Outline

- Molecular dynamics
- Sampling in molecular dynamics
- Calculation of thermodynamic quantities along the pathway
 - Techniques for calculating free energy:
 - Thermodynamic integration
 - Free energy perturbation
 - Potential of mean force
 - Non-equilibrium work
 - Enthalpy and entropy
 - Examples



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Molekular dynamics

2015.10.08

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Introduction

- Molecular dynamics – link between microscopic and macroscopic quantities
 - structure
 - dynamics
 - thermodynamics



Fnili_10_preSMD.mpg

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History

- Alder, B. J. and Wainwright, T. E.
J. Chem. Phys. **27**, 1208 (1957)

- McCammon, J. A., Gelin, B. R.,
and Karplus, M.
Nature (Lond.) **267**, 585 (1977)



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Basic terms

- Thermodynamic/Macroscopic state
 - The system is characterized by few macroscopic parameters; e.g.: T, P, N
- Microscopic state
 - The system is characterized by the positions and momenta of atoms (phase space).
- Ensembles
 - Microscopic states corresponding to a macroscopic state
- Molecular dynamics simulations
 - Generation of microscopic states of an ensemble as a function of time

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Thermodynamic ensembles

- Microcanonical – NVE (isolated system)
- Canonical – NVT (thermal equilibrium)
- Isotherm-izobar – NPT
- Grand canonical – μ VT (equilibrium with a reservoir of particles)

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Ergodic hypothesis

- Measurable quantities: ensemble average $\langle A \rangle_{ensemble}$
- Molecular dynamics: time average $\langle A \rangle_{time}$

$$\langle A \rangle_{time} = \langle A \rangle_{ensemble}$$

- „long enough” MD – appropriate sampling

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Force field

- Molecular mechanics
 - „classical“
 - simple, fast computations
 - includes parameters
 - Can be applied within the validity of the parameter space
 - Chemical reactions are typically outside the validity
- Quantum mechanics
 - accurate
 - time intensive computations

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Molecular mechanics

Atoms are pointlike objects with mass and interactions

$$E = E_{\text{str}} + E_{\text{bend}} + E_{\text{tors}} + E_{\text{vdw}} + E_{\text{el}} + E_{\text{cross}}$$

intramolecular

intermolecular

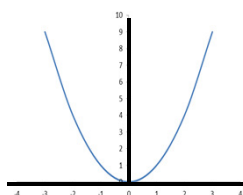
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Bond stretching energy

$$E_{\text{str}} = k(r - r_0)^2$$

$$F_{\text{str}} = -2k(r - r_0)$$



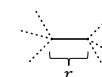
good approximation in the vicinity of r_0
 k and r_0 are atom dependent parameters

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Bond stretching energy - parameters

$$E_{\text{str}} = k(r - r_0)^2$$



general class	atom type ¹	description
hydrogen types		
	H	amide or imino hydrogen
	HC	explicit hydrogen attached to carbon
	HO	hydrogen on hydroxyl oxygen
	HS	hydrogen attached to sulfur
	HW	hydrogen in water
	H2	ditrino hydrogen in h2
	H3	hydrogen of lysine or arginine (positively charged)
all-atom carbon types²		
	C	sp ² carbonyl carbon and aromatic carbon with hydroxyl substituent in tyrosine
	CA	sp ² aromatic carbon in 5-membered ring with 1 substituent
	CB	sp ² aromatic carbon at junction between 5- and 6-membered rings
	CC	sp ² aromatic carbon in 5-membered ring with 1 substituent and next to a nitrogen
	CK	sp ² aromatic carbon in 5-membered ring between 2 nitrogens and bonded to 1 hydrogen (in purine)
	CM	sp ² same as Cj but one substituent
	CN	sp ² aromatic junction carbon in between 5- and 6-membered rings
	CQ	sp ² carbon in 6-membered ring of purine between 2 HC nitrogens and bonded to 1 hydrogen
	CR	sp ² aromatic carbon in 5-membered ring between 2 nitrogens and bonded to 1 H (in h2)
	CT	sp ³ carbon with 4 explicit substituents
	CV	sp ² aromatic carbon in 5-membered ring bonded to 1 H and bonded to an explicit hydrogen
	CW	sp ² aromatic carbon in 5-membered ring bonded to 1 H and bonded to an explicit hydrogen
	C*	sp ² aromatic carbon in 5-membered ring with 1 substituent

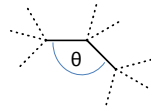
Bond Stretching Potential Parameters			
Bond	used for	K, kcal mol ⁻¹ Å ⁻²	R _{eq} , Å
CT-CT	BMT, EMT	310.0	1.526
CT-HI	BMT, EMT	340.0	1.090
CT-HC	BMT, EMT	340.0	1.090
CT-NA	BMT, EMT	337.0	1.473
CR-HS	BMT, EMT	367.0	1.080
CR-NA	BMT, EMT	477.0	1.343
CW-H4	BMT, EMT	367.0	1.080
CW-NA	BMT, EMT	427.0	1.381
CW-CW	BMT, EMT	549.0	1.350
AL-CI	TCF	116.1	2.170
P-F	PF ₅	260.3	1.646
NN-ON	NO ₂	300.0	1.260

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Bending energy

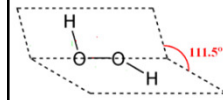
$$E_{bend} = k(\theta - \theta_0)^2$$



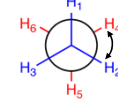
k and θ_0 are atom dependent parameters

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Torsional/dihedral angle energy



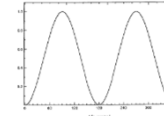
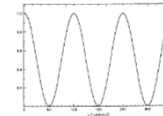
$$E_{tors} = \frac{V_n}{2} [1 + \cos(n\phi - \phi_0)]$$



V_n – barrier height
n – periodicity

Dihedral angle (atom types)				V_n , kcal/mol	n	ϕ_0	comments
C	CT1	NH1	C	0.2000	1	180.00	! backbone phi
NH1	C	CT1	NH1	0.6000	1	0.00	! backbone ksi
CT1	C	NH1	CT1	1.6000	1	0.00	! backbone omega
CA	CA	CA	CA	3.1000	2	180.00	! Phe side chain
H	OH1	CT2	CT1	0.4200	3	0.00	! Ser side chain

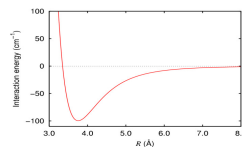
~15000 parameters



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van der Waals energy



short range: repulsive; $\exp(-r)$ or r^{-12} Pauli repulsion
middle range: attractive; r^{-6} dispersion
long range: disappears

$$E_{vdw} = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]$$

$$\sigma_{ij} = \frac{1}{2}(\sigma_i + \sigma_j)$$

$$\epsilon_{ij} = \sqrt{\epsilon_i \epsilon_j}$$

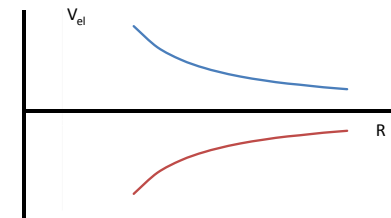
$$c * \exp\left(\frac{-r}{\sigma}\right)$$

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Electrostatic energy

$$V_{el} = \frac{q_i q_j}{\epsilon r_{ij}} \quad \text{Coulomb}$$



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MM parameters

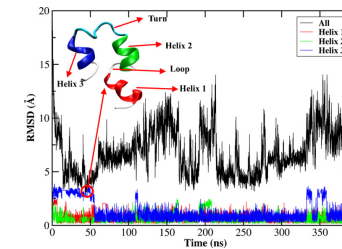
- Derivation
 - Quantum mechanical calculations
 - Experimental data
 - Extension based on analogy
- Validation by comparing computed and experimental data
 - Macromolecular structure
 - NMR data
 - Structure and energy of van der Waals complexes
- Error compensation; mutual interdependence of parameters

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Quality of MM force field

- Protein structure
- DNA, RNA structure
- Conformation of organic molecules
- Ligand-protein interactions
- Structure and interactions of lipids and membranes
- ...



RMSDs of backbone atoms
from the native structure
as a function of MD
simulation time

Duan J Mol Model 2014;20,2195

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Selected MM force fields

- Charmm (Chemistry at HARvard Macromolecular Mechanics)
- AMBER (Assisted Model Building with Energy Refinement)
- OPLS (Optimized Potentials for Liquid Simulations)
- GROMOS (GRONingen Molecular Simulation)
- MMFF (Merck Molecular Force Field)

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MD algorithm

Newtonian mechanics

$$r^N(r_1, r_2 \dots r_N) \quad p^N(p_1, p_2 \dots p_N)$$

$$U(\underline{r}) \quad K(\underline{p}) = \sum_i \frac{|p_i|^2}{2m_i}$$

$$H = K + U \quad \dot{r}_i = \frac{p_i}{m_i} \quad \dot{p}_i = f_i$$

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Verlet algorithm

Calculation of p_i and r_i at δt time steps

$$p_i(t), r_i(t) \rightarrow p_i(t + \delta t), r_i(t + \delta t) \rightarrow f_i(t)$$

$$p_i\left(t + \frac{1}{2}\delta t\right) = p_i(t) + \frac{1}{2}\delta t \cdot f_i(t)$$

$$r_i(t + \delta t) = r_i(t) + \frac{\delta t \cdot p_i\left(t + \frac{1}{2}\delta t\right)}{m_i} \rightarrow f_i(t + \delta t)$$

$$p_i(t + \delta t) = p_i\left(t + \frac{1}{2}\delta t\right) + \frac{1}{2}\delta t \cdot f_i(t + \delta t)$$

Typical δt for simulation of biochemical systems: 1-4 fs

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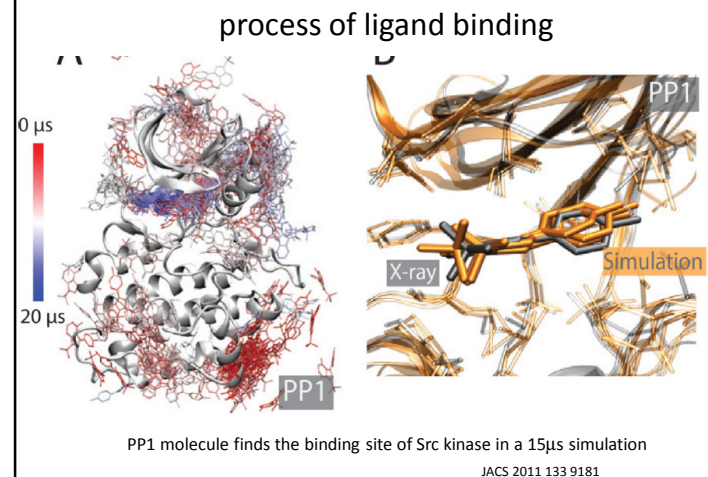
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Selected applications

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Application 1

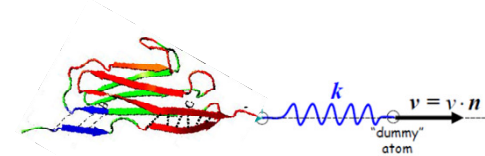


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Application 2

Steered MD

- Constant velocity pulling



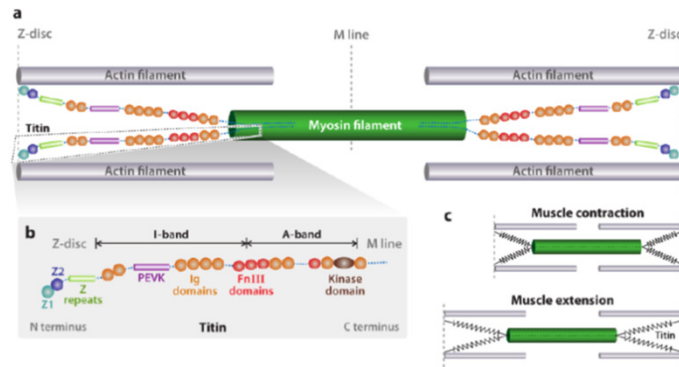
$$U = \frac{1}{2}k[v t - (\vec{r} - \vec{r}_0) \cdot \vec{n}]^2$$

- Constant force pulling

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Application 2

Titin structure and function



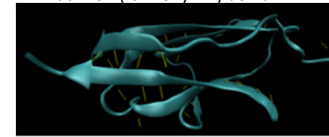
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Application 2

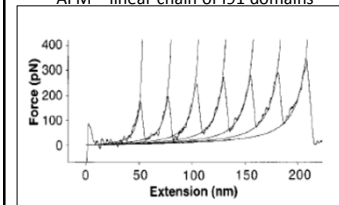
Unfolding and force

titin I91 (formerly I27) domain



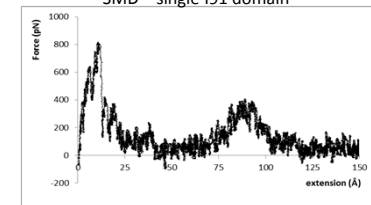
Constant velocity pulling

AFM – linear chain of I91 domains



Rief et al. (1997 Science 276 1109)

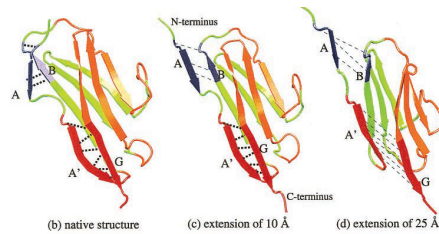
SMD – single I91 domain



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Application 2

Unfolding and structure

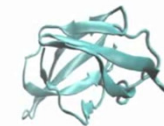
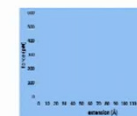


Lu, H., and Schulten, K. (2000). Biophys. J. 79, 51–65

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Application 2

Titin Fn domain unfolding mechanism

A78
 $v=1\text{Å/ns}$ 

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MD scope and limitation

- Scope
 - Structural study; structure refinement
 - Dynamics
 - conformations, ligand-protein binding, steered processes,...
 - Thermodynamics see later
 - Free energy changes
 - solvation, ligand-protein binding,...
- Limitations
 - Sampling see later
 - Accuracy of force field
 - Chemical reactions cannot be routinely studied

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MD - sampling

- Microstates appear according to Boltzmann distribution
 - $\exp\left(-\frac{E}{kT}\right)$
- Simulation time is limited by computational capacity
 - Time scale for proteins: $\sim \mu\text{s}$
- Rare events with high energy barrier cannot be straightforwardly simulated

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MD - Sampling

Time scale (s)	Amplitude (Å)	Description	# MD steps (step \sim fs)
10^{-15} - 10^{-12}	0.001-0.1	Bond stretching, bond angle deformation	1-1000
10^{-12} - 10^{-9}	0.1-10	Protein sidechain, loop and collective motions	10^3 - 10^6
10^{-9} - 10^{-6}	1-100	Folding of small proteins	10^6 - 10^9
10^{-6} - 10^{-1}	10-100	Protein folding, Ligand-protein binding	10^9 - 10^{14}

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Free energy - Sampling

$$F = -kT \ln \left[h^{-3N} \iint \exp\left(-\frac{E(r,p)}{kT}\right) dp dr \right] \quad (1) \text{ Formula for free energy}$$

Free energy calculation with MD sampling is problematic

phase space incomplete in (1)
 positive integral
 ln function increases monotonically
 negative contribution missing
F overestimated

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Free energy - Sampling

$$F = -kT \ln \left[h^{-3N} \iint \exp \left(-\frac{E}{kT} \right) dp dr \right] \quad (1) \text{ Formula for free energy}$$

$$F = -kT \ln \left[\int \exp \left(-\frac{E}{kT} \right) dr \right] + \left(\text{ideal gas kinetic energy} \right) \quad (2) \text{ Integrated by momenta}$$

$$F' = -kT \ln \left[\frac{\int \exp \left(-\frac{E}{kT} \right) dr}{\int \exp \left(-\frac{E}{kT} \right) \exp \left(+\frac{E}{kT} \right) dr} \right] \quad (3) \text{ Divided by volume integral}$$

$$F' = kT \ln \left[\frac{\int \exp \left(+\frac{E}{kT} \right) \exp \left(-\frac{E}{kT} \right) dr}{\int \exp \left(-\frac{E}{kT} \right) dr} \right] = kT \ln \left(\exp \left(\frac{E}{kT} \right) \right) \quad (4) \text{ Formulated as expected value}$$

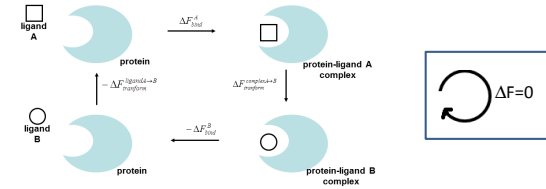
Terms with high E contribute to F significantly according to (4), but their sampling has a low probability

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Free energy difference

- Sampling issue hampers the calculation of F and $\Delta F = F_{\text{bound}} - F_{\text{free}}$
- Special techniques for calculating $\Delta F = F_B - F_A$ (A similar to B) for similar systems (see later)
- Thermodynamic cycle: binding free energy difference ($\Delta \Delta F$) of two similar ligands is obtained from the free energy difference of similar systems

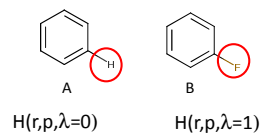


- $\Delta \Delta F = \Delta F_{\text{bind}}^A - \Delta F_{\text{bind}}^B = \Delta F_{\text{transform}}^{\text{complex A} \rightarrow \text{B}} - \Delta F_{\text{transform}}^{\text{ligand A} \rightarrow \text{B}}$
- „alchemical” transformations: $\Delta F_{\text{transform}}^{\text{complex A} \rightarrow \text{B}}$ and $\Delta F_{\text{transform}}^{\text{ligand A} \rightarrow \text{B}}$
 - 2 transformations to obtain $\Delta \Delta F$

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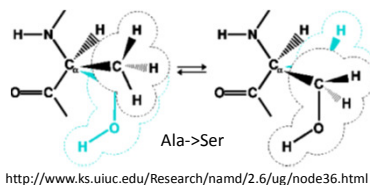
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Alchemical transformation- coupling parameter



$$H_\lambda = H(r, p, \lambda) = (1-\lambda) H_A + \lambda H_B$$

λ – coupling parameter
 H_λ may be other function of λ
 H_A, H_B may depend on λ



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MD techniques to calculate ΔF

- Thermodynamic integration (TI)
- Free energy perturbation (FEP)
- Potential of mean force (PMF)
- Non-equilibrium work (Jarzynski equation)

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Thermodynamic integration

$$\Delta F = F_B - F_A = F(\lambda=1) - F(\lambda=0) = \int_{\lambda=0}^{\lambda=1} F'(\lambda) d\lambda$$

$$F' = \frac{d}{d\lambda} [-kT \ln Z(\lambda)] = \left\langle \frac{\partial E}{\partial \lambda} \right\rangle$$

$$F' = \left\langle \frac{\partial E}{\partial \lambda} \right\rangle \rightarrow \frac{dF(x, \lambda)}{d\lambda} = \frac{d \left(-kT \ln \int e^{-\frac{E(x, \lambda)}{kT}} dx \right)}{d\lambda}$$

$$= -kT \frac{1}{\int e^{-\frac{E(x, \lambda)}{kT}} dx} \left(\int e^{-\frac{E(x, \lambda)}{kT}} \frac{\partial E(x, \lambda)}{\partial \lambda} dx \right) = \left\langle \frac{\partial E(x, \lambda)}{\partial \lambda} \right\rangle$$

E.g.: $E(x, \lambda) = (1-\lambda) E_A(x) + \lambda E_B(x)$;
 $dE/d\lambda = E_B - E_A$

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Thermodynamic integration

• simulation

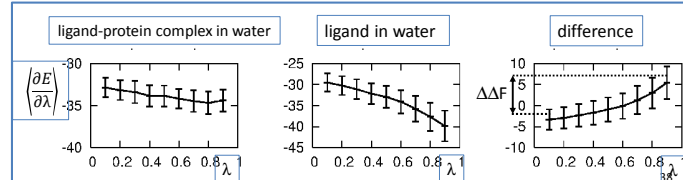
1. λ evolves in time
2. MD at several fixed λ value

– Calculation of $\left\langle \frac{\partial E}{\partial \lambda} \right\rangle$

- E.g.: $\frac{\partial E}{\partial \lambda} = E_B - E_A \rightarrow \langle E_B - E_A \rangle_\lambda$ depend on λ ; $\frac{\partial E}{\partial \lambda}$ may be more involved

– Numerical integration

$$\Delta F = \int_{\lambda=0}^{\lambda=1} \left\langle \frac{\partial E}{\partial \lambda} \right\rangle_\lambda d\lambda$$



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Free energy perturbation

$$F = -kT \ln \left[\int \exp \left(-\frac{E}{kT} \right) dr \right] \quad (1) \text{ Formula for free energy}$$

$$F_B - F_A = -kT \ln \left[\frac{\int \exp \left(-\frac{E_B}{kT} \right) dr}{\int \exp \left(-\frac{E_A}{kT} \right) dr} \right] \quad (2) \text{ Free energy difference for two systems}$$

$$F_B - F_A = -kT \ln \left[\frac{\int \exp \left(-\frac{E_A}{kT} \right) \exp \left(\frac{E_A}{kT} \right) \exp \left(-\frac{E_B}{kT} \right) dr}{\int \exp \left(-\frac{E_A}{kT} \right) dr} \right] \quad (3) 1 = \exp \left(-\frac{E_A}{kT} \right) \exp \left(\frac{E_A}{kT} \right)$$

$$F_B - F_A = -kT \ln \left[\frac{\int \exp \left(-\frac{E_A}{kT} \right) \exp \left(-\frac{\Delta E}{kT} \right) dr}{\int \exp \left(-\frac{E_A}{kT} \right) dr} \right] \quad (4) \Delta E = E_B - E_A$$

$$F_B - F_A = -kT \ln \left[\left\langle \exp \left(-\frac{\Delta E}{kT} \right) \right\rangle_A \right] \quad (5) \text{ Expectation value}$$

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Free energy perturbation

$$\Delta F = -kT \ln \left\langle \exp \left(-\frac{E_B - E_A}{kT} \right) \right\rangle_A$$

• A \rightarrow B may be divided into several intervals

A \rightarrow B
 small changes

$$\Delta F = \sum_i -kT \ln \left\langle \exp \left(-\frac{E(\lambda_{i+1}) - E(\lambda_i)}{kT} \right) \right\rangle_{\lambda_i}$$

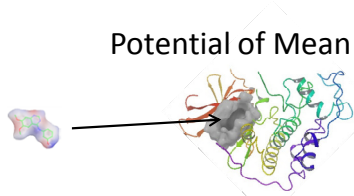
Simulation

- MD for system λ_i
- Calculation of $\exp \left(-\frac{E(\lambda_{i+1}) - E(\lambda_i)}{kT} \right)$

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Potential of Mean Force(PMF)



\underline{x} – intermolecular coordinates
 \underline{y} – intramolecular coordinates

$$F = -RT \ln \left[\int \exp \left(-\frac{E(\underline{x}, \underline{y})}{RT} \right) d\underline{x} d\underline{y} \right] \quad \text{Free energy}$$

$$F(\underline{x}) = -RT \ln \left[\int \exp \left(-\frac{E(\underline{x}, \underline{y})}{RT} \right) d\underline{y} \right] \quad \text{Potential of mean force}$$

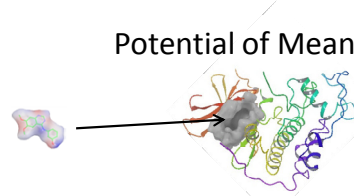
explanation

$$\frac{dF(\underline{x})}{d\underline{x}} = \frac{\int \frac{dE(\underline{x}, \underline{y})}{d\underline{x}} e^{-\frac{E(\underline{x}, \underline{y})}{RT}} d\underline{y}}{\int e^{-\frac{E(\underline{x}, \underline{y})}{RT}} d\underline{y}} = -\langle \varphi(\underline{x}) \rangle_{\underline{y}} \quad F - \text{potential}; \varphi - \text{force}$$

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Potential of Mean Force(PMF)



\underline{x} – intermolecular coordinates
 \underline{y} – intramolecular coordinates

Relation between probability ($P(\underline{x})$) and PMF ($F(\underline{x})$) of \underline{x}

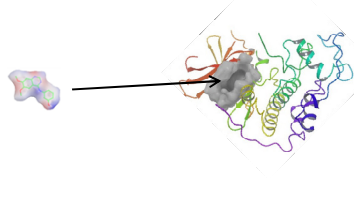
$$P(\underline{x}) = \int P(\underline{x}, \underline{y}) d\underline{y} = \frac{\int e^{-\frac{E(\underline{x}, \underline{y})}{RT}} d\underline{y}}{\int e^{-\frac{E(\underline{x}, \underline{y})}{RT}} d\underline{x} d\underline{y}} = \frac{e^{-\frac{F(\underline{x})}{RT}}}{\int e^{-\frac{F(\underline{x})}{RT}} d\underline{x}} \quad P(\underline{x}) - \underline{x} \text{ probability}$$

$$F(\underline{x}) - F_{Ref} = -RT \ln \frac{P(\underline{x})}{P(Ref)}$$

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Potential of Mean Force (PMF)



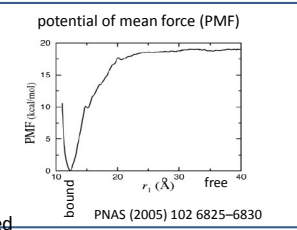
\underline{x} – intermolecular coordinates

Computation:
 $P(\underline{x})$ is calculated along \underline{x}

$$F(\underline{x}) - F_{Ref} = -RT \ln \frac{P(\underline{x})}{P(Ref)}$$

$$F(\underline{x}) = -RT \ln P(\underline{x}) + \text{const.}$$

Special sampling techniques needed
 Standard binding free energy can be calculated



potential of mean force (PMF)

PNAS (2005) 102 6825–6830

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Non-equilibrium work

$$\Delta F = F_2 - F_1 = -kT \ln \left\langle \exp \left(-\frac{W}{kT} \right) \right\rangle \quad (\text{Jarzynski})$$

- Expected value of work (W) obtained along non-equilibrium paths
- Fast transformation between the states is possible
- Appropriate sampling is challenging
- Current techniques are not superior to equilibrium methods

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Calculation of Enthalpy and Entropy

- ΔF can be calculated as the expected value of some function of energy differences
 - cf. TI and FEP
- ΔH , $T\Delta S$ can be calculated as the difference of the expected values of state functions
- ΔH , $T\Delta S$ can be calculated with significantly lower accuracy than ΔF

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Example – binding to lysozyme

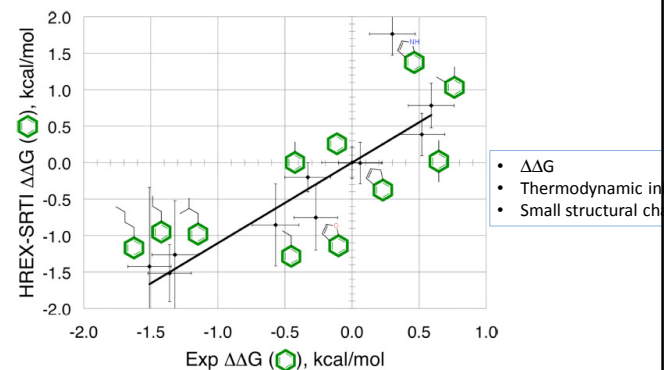


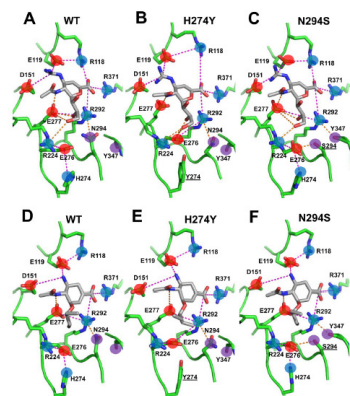
Figure 6. Comparison of the HREX-SRTI relative binding free energy predictions to experiment

J. Chem. Theor. Comput. 2011, 7 3001

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Example – neuraminidase inhibitors 1



- 2 ligands
- 3 proteins: wild type + 2 mutants

Figure 3. Representative structures for zanamivir (A, B and C) and oseltamivir (D, E and F) bound to WT and mutant NAs from the H5N1 H274Y and N294S mutations. Salt bridges and hydrogen bonds are depicted as magenta and orange dashed lines, respectively. Positively charged, negatively charged, and uncharged polar groups are noted as blue, red, and purple circles, respectively, and residues of interest are labeled. Mutual exclusions are indicated.

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Example – neuraminidase inhibitors 2

Table 1. Comparison of experimental $\Delta\Delta G$ in oseltamivir and zanamivir for three NA mutations with estimates obtained using different computational approaches.

Method	H274Y		N294S		Y252H		RMSE (RMSD), kcal/mol
	$\Delta\Delta G$, kcal/mol		$\Delta\Delta G$, kcal/mol		$\Delta\Delta G$, kcal/mol		
	zanamivir	oseltamivir	zanamivir	oseltamivir	zanamivir	oseltamivir	
Experimental ^a	0.4 (0.1)	3.3 (0.2)*	1.2 (0.1)*	2.6 (0.2)*	0.1 (0.2)	-1.4 (0.1)	N/A (0.2)
MM	-5.8 (7.4)	0.7 (7.0)	8.2 (7.7)	5.8 (6.2)	-0.1 (8.7)	-0.9 (7.4)	4.2 (7.4)
B3LYP	1.7 (2.9)	1.2 (3.0)	0.6 (2.0)	1.7 (1.9)	1.5 (1.7)	0.5 (1.5)	1.5 (2.2)
SRSA/HREX	1.3 (0.8)	4.1 (2.4)	2.3 (0.4)	2.2 (0.9)	0.6 (0.8)	0.7 (1.4)	1.1 (1.1)
MM-GBSA	6.2 (8.1)	0.9 (3.8)	5.7 (6.1)	-5.9 (3.6)	2.1 (2.9)	-1.9 (3.0)	4.8 (4.6)
MM-PBSA	8.4 (10.1)	3.0 (3.9)	5.8 (4.5)	-4.7 (3.2)	2.8 (3.1)	0.2 (2.6)	5.0 (4.6)
Cozzetta	-0.4 (0.5)	0.8 (0.4)	-0.4 (0.3)	0.3 (0.2)	-0.1 (0.4)	0.0 (0.0)	1.7 (0.3)

Values were derived from the data reported by Collins et al [10].

Standard deviations are shown in parentheses. Root mean squared error (RMSE) and the RMS Standard Deviation (RMSD) are provided.

*Indicates experimentally determined drug resistant mutation. 'N/A' stands for not applicable.

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- $\Delta\Delta G$; TI
 - Wild type/mutant
 - Experimental/calculated
 - (Standard deviation)
- Relative affinities toward various sequences are correctly predicted for both ligands
- Relative affinities of ligands toward a protein are not always predicted correctly

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Example – FKBP12-ligand

Standard binding free energy
Double decoupling
FEP
Free energy components

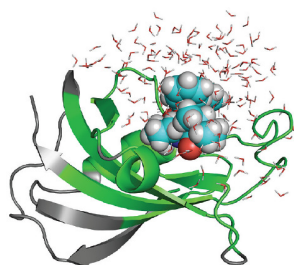


Figure 4. FKBP12 bound with ligand #8 studied previously.^{40,42} The gray parts are treated as a mean-field approximation with generalized solvent boundary potential.⁴⁰ See ref 42 for computational details.

$\Delta\Delta G_{\text{rep}}$	$\Delta\Delta G_{\text{dis}}$	$\Delta\Delta G_{\text{elec}}$	$\Delta\Delta G_{\text{c}}$	$\Delta\Delta G_{\text{t}}$	$\Delta\Delta G_{\text{r}}$	ΔG_{bind}^0	exptl
-1.1	-21.1	-3.7	6.9	3.4	5.4	-10.2	-10.9
			conf	transl	rot		

⁴⁹
J. Phys. Chem. B **2009**, *113*, 2234

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Summary

- Computational modelling of protein-ligand interactions – 1st part
 - MD based methods – potentially accurate
 - Major challenge: sampling
 - $\Delta\Delta F$ ($\Delta\Delta G$) can be calculated efficiently; „Alchemical” transformations
 - Techniques to calculate ΔF (between similar states)
 - Thermodynamic integration
 - Free energy perturbation
 - Potential of mean force
 - Non-equilibrium work
 - Non-routine applications; varying accuracy
 - Enthalpy and entropy can be calculated with lower accuracy

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