

Human Body as a signal source

Signal processing

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Human Body as signal source

Signals in medicine

Information content of signals

Signal detection - transducers

Explained through examples
there are endless possibilities

Signals in medicine

$$H = \sum p * \log_2 \frac{1}{p}$$

Information content in Bits

Signal is something which carries Information

Human body as signal source: everything which is a signal, and comes from the body

Here in the cartoon:

Information : Head or Tail?

Signal:

- Optical: we simply look at the coin, and see the image
- Digital: after encoding: 1/0



Transmitting information – information coding

in general

Information source

encoding ↓

Transmission channel

decoding ↓

Information receiver destination

an example

Which side is up?

encoding ↓ Sides : Head or Tail into Numbers: 1,0

Speech, waves in the air, sms

decoding ↓ 1,0 → head, tail

Decide who wins

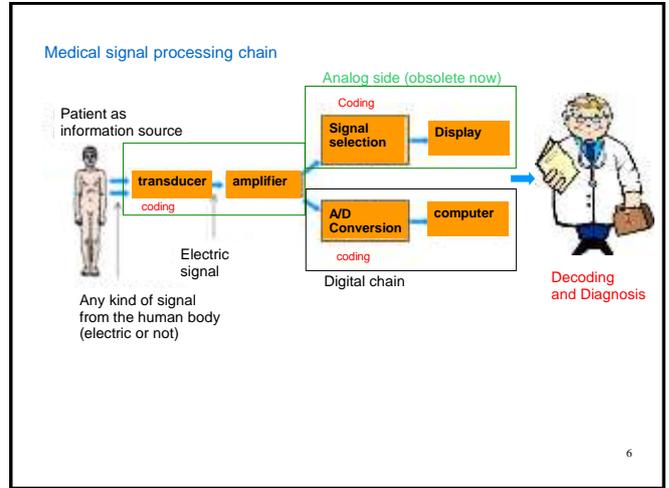
$$H = P_{tail} * \log_2 \frac{1}{P_{tail}} + P_{head} * \log_2 \frac{1}{P_{head}} = \frac{1}{2} * \log_2 \frac{1}{\frac{1}{2}} + \frac{1}{2} * \log_2 \frac{1}{\frac{1}{2}} = 1 \text{ [Bit]}$$

Signals in medicine
Signal is something which carries Information

Here in speech:

Information : „what we say“

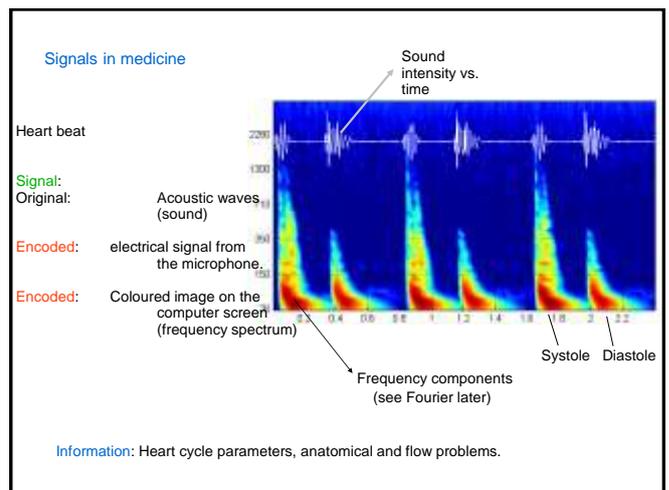
Signal:
- Audio: pressure wave the air
- encoding: electrical signal f Microph
- encoding: formal grammar
- decoding: electrical to Mechar (loudspeaker)
- decoding: natural language underst



Signals in medicine

Information: Heart cycle
ECG: Electro CardioGraphy

Signal:
Original: voltage across points (eg. two arms)
Encoding: None, But Filtering required
Removal of unwanted portion of the signal



Signals in medicine

PET: Positron Emission Tomography

Signal: γ -photons

Original: γ -photons

Encoded: electrical pulses from the detector.

Encoded: Coloured image on the computer screen

Information: Location of drug, labeling molecule, etc.

Signals in medicine

SPET-CT: Single Photon Emission Computed Tomography

Computer Tomography

Signal: γ -photons

Original: γ -photons

Encoded: electrical pulses From the detector.

Encoded: Coloured image

Information: Anatomy (X-ray) Label (disease, etc)

Signals in medicine

Heart beat

Signal: Cell types and count in unit volume

Original: Cell types and count in unit volume

Encoded: electrical signal from the cell sorter.

Encoded: Areas under the histogram

Information: Blood composition

LYMPH%	16.2	%
MXD %	6.7	%
NEUT%	77.1	%
LYMPH#	1.2×10^9	/ μ l
HXD #	0.5×10^9	/ μ l
NEUT#	5.8×10^9	/ μ l

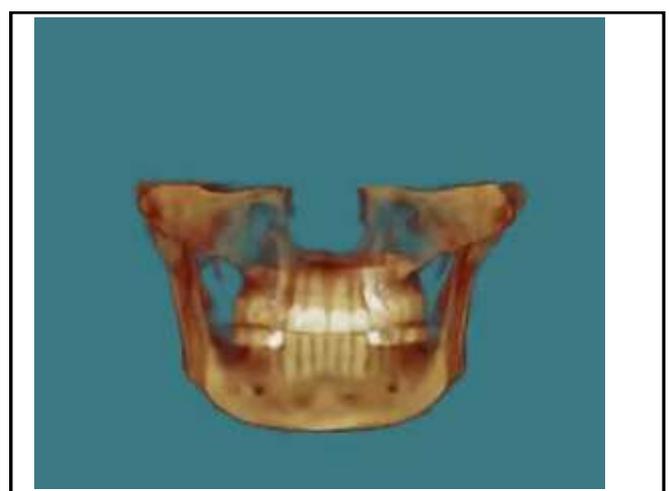
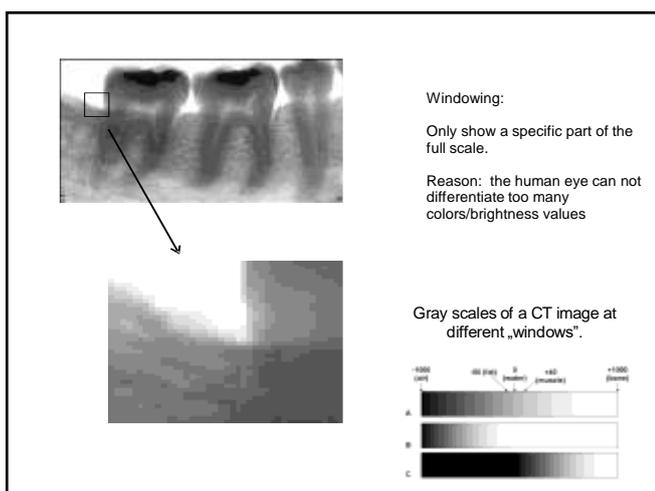
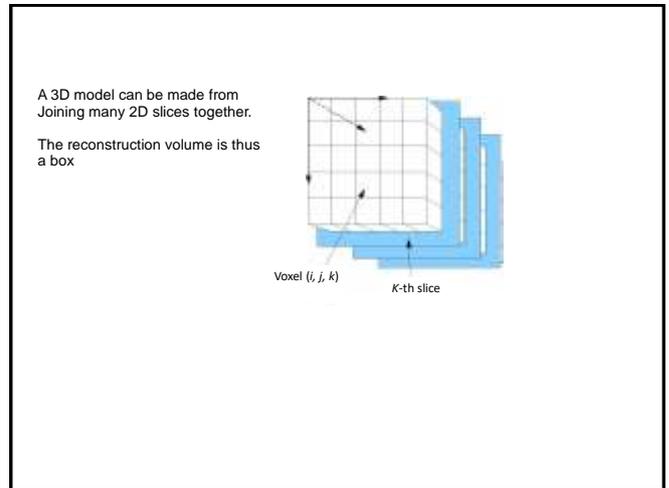
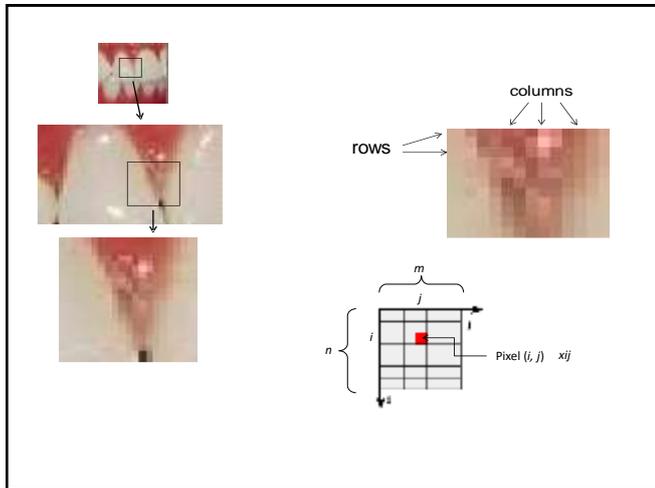
Basics of medical imaging:

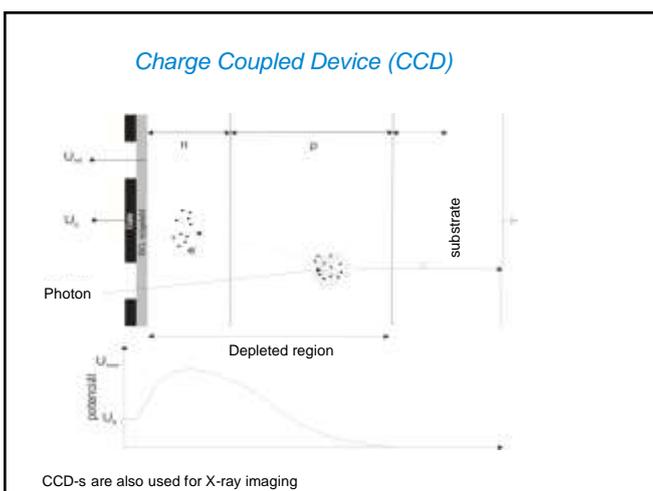
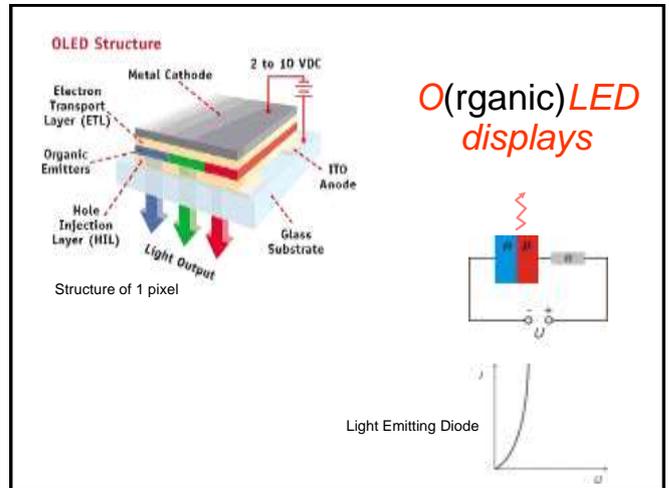
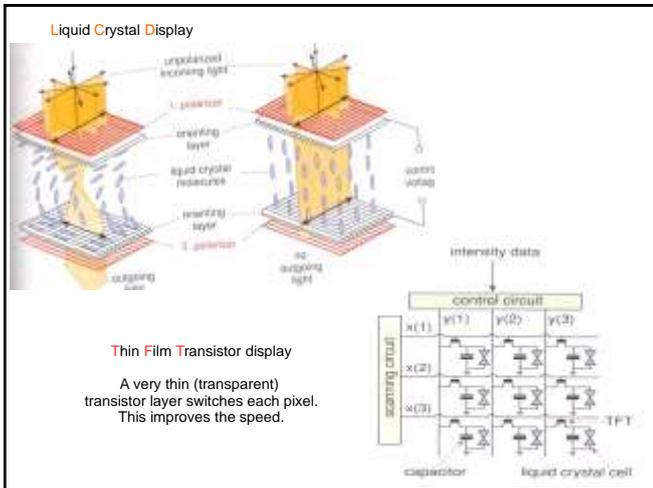
Pixel

Voxel

Image

Tomogram





Signal processing

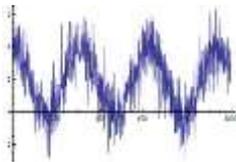
Types of signals

Electric signals – analog signal chain
(amplifier, frequency response, Fourier theorem)

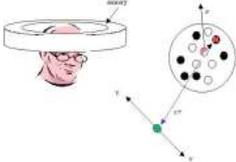
Digital signal processing (DSP)

Types of signals

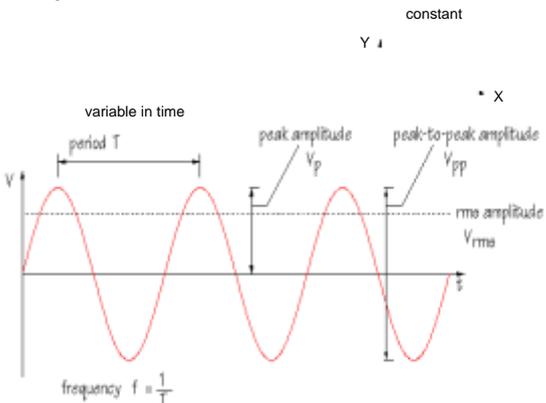
Electric

Not electric

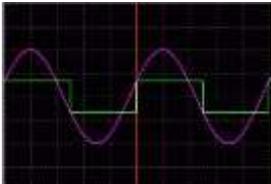



Types of signals



Types of signals

Periodic

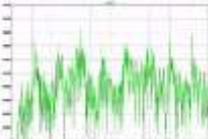


Not periodic

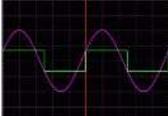


Types of signals

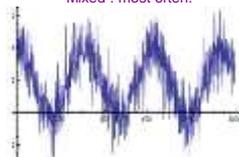
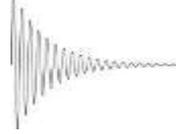
Random



Deterministic



Mixed : most often!

Types of signals

Continuous

Pulses

Types of signals

Analog

Theoretically unlimited resolution in time and magnitude (measurement system limit only)

Digital

1 0 0 1 0 1 1 1 0 0 1 0 0 0 1 0 1

Unipolar Coding ('1' = +V, '0' = 0V)

Digital: represented with numbers

Finite resolution

Digital signals are a form of **encoding**: digital to electrical to electrical to digital

Information content of signals

Analog signals – infinite information content?

Do we really need **unlimited** resolution?

Do we even **have** unlimited resolution in real-life analog signals?

Theoretically unlimited resolution in time and magnitude (measurement system limit only)

No!

We always have a real signal as:

$$S = \text{Information} + \text{Noise}$$

Information + Noise

Information content of signals

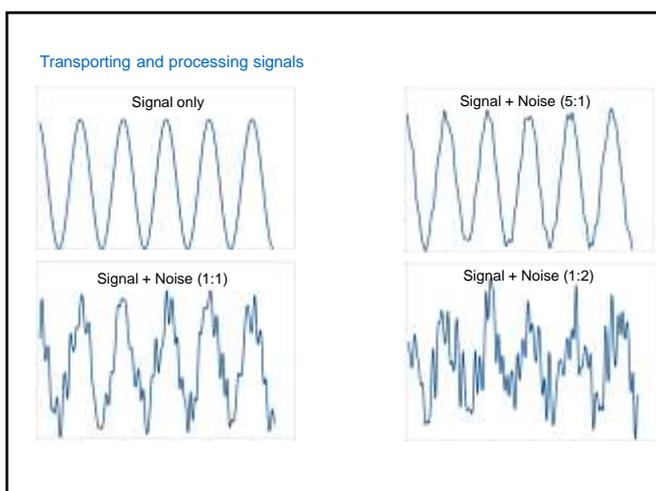
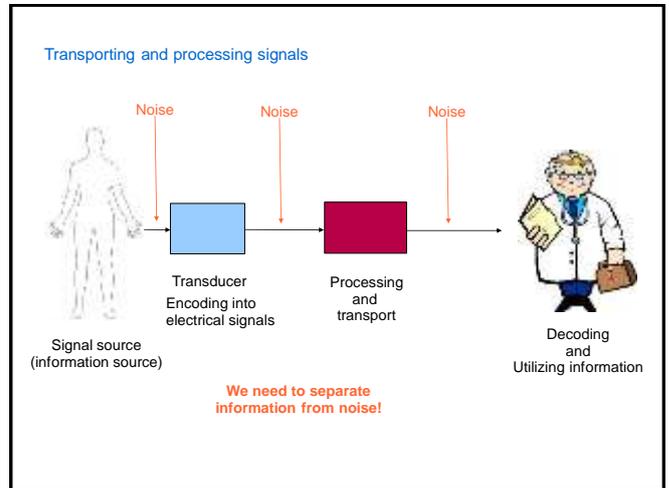
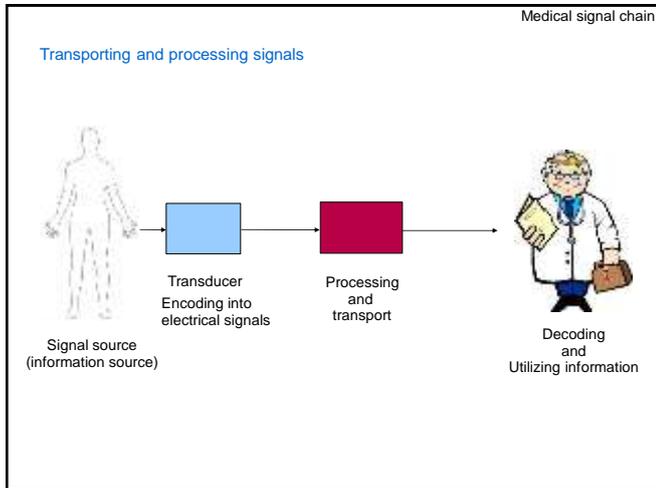
Analog signals – infinite information content?

We have Information + Noise

Goal: **Preserve and transport information** without increasing the noise content.

Information $U = A_{inf} \cdot \cos(\omega t + \phi)$

+ Noise $\text{Noise}(t) = A_{noise} \cdot \text{Random}(t)$



Transporting and processing signals

Amplifiers

Task: amplify signal, without addition of noise
(only transport information)
Combat noise in the chain: Amplify the signal at the beginning!

In real-life no amplifier is ideal, they always distort the signal

We need to characterize amplifiers, and other signal-transporting / processing elements of the signal chain.

Analysis of amplifiers

The technique is applicable to any transport/coding

Basic analysis: amplifier gain

$P = U \cdot I = U^2 / R$

$n = 10 \log \frac{P_{output}}{P_{input}} \quad [dB]$

U _{out} /U _{in}	P _{out} /P _{in}	dB
1,414	2	3
2	4	6
2,818	8	9
3,16	10	10
10	20	13
100	100	20
1000=10 ³	1000=10 ³	30
1000=10 ³	10000=10 ⁴	40
1000=10 ³	1000=10 ³	60

$\frac{P_2}{P_1} = 10 \log \frac{dB}{10}$

$\frac{P_2}{P_1} = 2 = 10 \log \frac{dB}{10}$

Analysis of amplifiers - complex signals

Fourier theorem: Any arbitrary (periodic) signal can be split into sine/cosine functions with varying frequency and amplitude OR from a set of such functions it can be recovered

$$Signal(t) \leftrightarrow \sum_i A_i \sin(\omega_i t) + B_i \cos(\omega_i t)$$

Where in the case of periodic signals $\omega_i = k \cdot f$, $f = 1/T$ and $k = 1, 2, 3, 4, 5, \dots$

Base frequency overtones

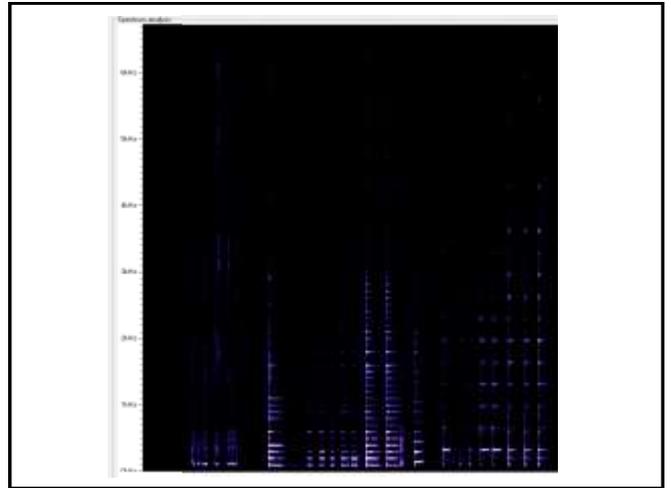
Analysis of amplifiers - Fourier theorem $Signal(t) \leftrightarrow \sum_i A_i \sin(\omega_i t) + B_i \cos(\omega_i t)$

The screenshot shows a software interface with two columns of plots. Each column contains a time-domain waveform (sine wave and a more complex periodic wave) and its corresponding frequency spectrum. The spectrum shows discrete peaks at the component frequencies. A red box highlights a section of the interface with text in Chinese.

Analysis of amplifiers - Fourier theorem $Signal(t) \leftrightarrow \sum_i A_i \sin(\omega_i t) + B_i \cos(\omega_i t)$

The screenshot shows a software interface with two columns of plots. Each column contains a time-domain waveform (sine wave and a more complex periodic wave) and its corresponding frequency spectrum. The spectrum shows discrete peaks at the component frequencies.

Analysis of amplifiers - Fourier theorem $Signal(t) \leftrightarrow \sum A_i \sin(\omega_i t) + B_i \cos(\omega_i t)$
 Non-periodic signals: Fourier transform $F(\omega) = \frac{1}{\sqrt{(2\pi)}} \int_{-\infty}^{+\infty} f(t) e^{j\omega t} dt$



Analysis of amplifiers - Fourier theorem $Signal(t) \leftrightarrow \sum A_i \sin(\omega_i t) + B_i \cos(\omega_i t)$
 Non-periodic signals: Fourier transform $F(\omega) = \frac{1}{\sqrt{(2\pi)}} \int_{-\infty}^{+\infty} f(t) e^{j\omega t} dt$

Insheer
 Penny Whistle
 Traditional Air

Analysis of amplifiers - Fourier theorem $Signal(t) \leftrightarrow \sum A_i \sin(\omega_i t) + B_i \cos(\omega_i t)$
 Non-periodic signals: Fourier transform $F(\omega) = \frac{1}{\sqrt{(2\pi)}} \int_{-\infty}^{+\infty} f(t) e^{j\omega t} dt$

Analysis of amplifiers - Fourier theorem $Signal(t) \leftarrow \sum A_i \sin(\omega_i t) + B_i \cos(\omega_i t)$

Non-periodic signals: Fourier transform $F(\omega) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{+\infty} f(t) e^{i\omega t} dt$

Any signal is just a representation of information

We can have many pictures of the same

Time-based (more conventional)

or

Frequency-based (useful, but a bit abstract)

Fourier-transform is the „art of engineering“ (Picasso: La Crucifixion)



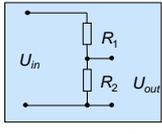
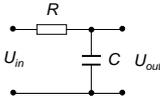
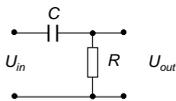

Analysis of amplifiers - Transfer function of filters

Low-pass filter $n(\text{dB})$ vs $\log f$

High-pass filter $n(\text{dB})$ vs $\log f$

$U_{\text{output}} = U_{\text{input}} \cdot \frac{R_2}{R_1 + R_2}$

Substitute one R with C

Analysis of amplifiers - Transfer function of filters

Low-pass filter $n(\text{dB})$ vs $\log f$

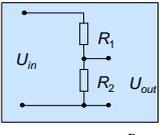
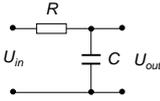
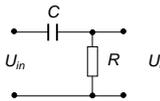
High-pass filter $n(\text{dB})$ vs $\log f$

$U_{\text{output}} = U_{\text{input}} \cdot \frac{R_2}{R_1 + R_2}$

Substitute one R with C $R_C = \frac{1}{C\omega}$

$U_{\text{out}} = \frac{1}{\sqrt{1 + R^2 C^2 \omega^2}} U_{\text{input}}$

$U_{\text{out}} = \frac{RC\omega}{\sqrt{1 + R^2 C^2 \omega^2}} U_{\text{input}}$

Analysis of amplifiers - Transfer function of amplifiers

Input U_1 → Amplifier → Output U_2

$n(\text{dB})$ vs $\log f (\text{Hz})$

Ideal amplifier n_{max}

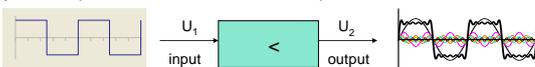
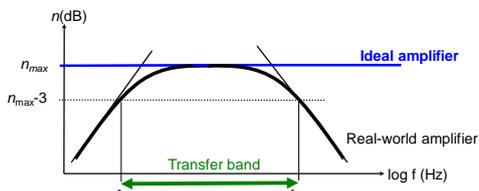
Real-world amplifier $n_{\text{max}} - 3$

Transfer band f_l to f_u

Amplifiers are not ideal, they have input and output capacitance, etc.

The output signal may *not* contain all frequency components!

Distortion, information loss / alteration

Analysis of amplifiers - Transfer function of amplifiers

Feedback in amplifiers
Modification of **gain** and **Transfer function**

Summation point

Amplifier gain

Gain with feedback circuit

$\beta > 0$: positive feedback
 $\beta < 0$: negative feedback
 $A\beta = 1$: oscillator (output without input signal: signal generator)

Analysis of amplifiers - Transfer function of amplifiers

Gain Bandwidth Product

Gain · Bandwidth = constant

The available power to the amplifier can either be put to use as:

high signal gain over a limited bandwidth
 or
 limited gain over a wide bandwidth.

Analysis of amplifiers - Transfer function of amplifiers

Frequency range of the signal must match the bandwidth!
 Information preservation = spectrum preservation

Analysis of amplifiers - Transfer function of amplifiers

During analog signal transport at every stage noise will be added! → degradation

Just transport that part of the spectrum which contains the information!

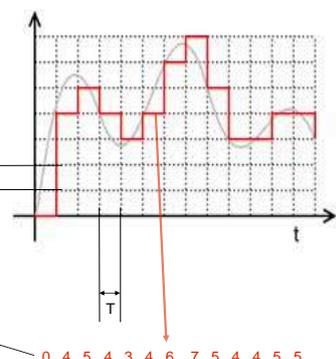
Digital signals – A/D conversion (ADC)

The analog signal can be represented by numbers:
 We measure the signal every T seconds, and transmit the result only.

Measurement accuracy (how many bits)

Digital signals are discrete in time and in value

Numbers can be transported / stored or processed losslessly!

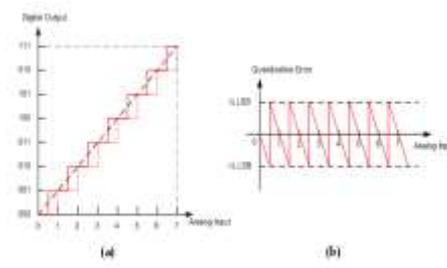


0 4 5 4 4 3 4 4 6 7 5 4 4 5 5...

Digital signals - Quantization

Digital signals are discrete in time and in value

What happens to the original parts between? They get lost!

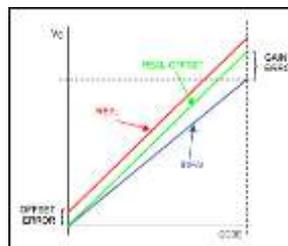


(a) (b)

Digital signals – Restoration (DAC)

Recovery of analog signals:
 Digital to analog converter

This is easily realized to be near-ideal
 Many-bits, fast DAC-s are cheap



Pitfalls to avoid



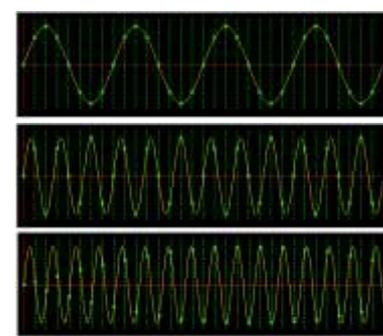
Digital signals – Sampling of sine waves

For non-sine signals: „first apply Fourier, then sample each sine“

f = 1000 Hz
 fs = 8000 Hz
 No problem

f = 3000 Hz
 fs = 8000 Hz
 Still no problem

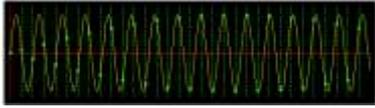
f = 3900 Hz
 fs = 8000 Hz
 Still no problem



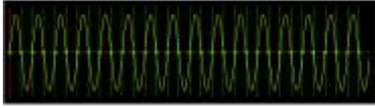
Digital signals – Sampling of sine waves

For non-sine signals: „first apply Fourier, then sample each sine“

$f = 3900\text{ Hz}$
 $f_s = 8000\text{ Hz}$
 Still no problem



$f = 4000\text{ Hz}$
 $f_s = 8000\text{ Hz}$
 Signal lost!



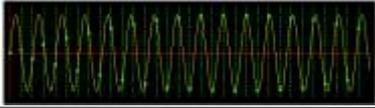
Nyquist theorem: sampling frequency must be at least 2x the frequency of the sine

Digital signals – Nyquist

Nyquist theorem: sampling frequency must be at least 2x the frequency of the sine

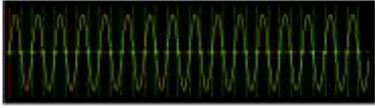
good

$f = 3900\text{ Hz}$
 $f_s = 8000\text{ Hz}$
 Still no problem

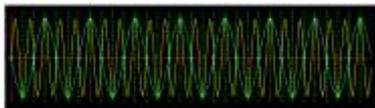


bad

$f = 4000\text{ Hz}$
 $f_s = 8000\text{ Hz}$
 Signal lost!



$f = 6000\text{ Hz}$
 $f_s = 8000\text{ Hz}$
 Signal lost!
 Aliasing



Aliased sine appears instead of the real input

