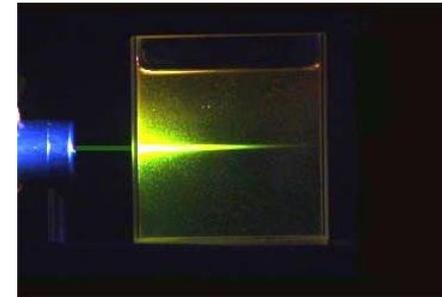


LEFTOVER FROM LECTURE 1: RADIATION ATTENUATION

MIKLÓS KELLERMAYER

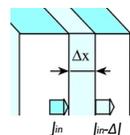
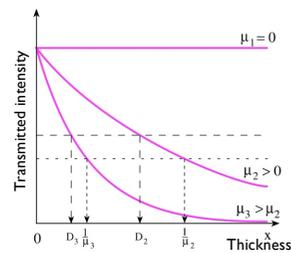
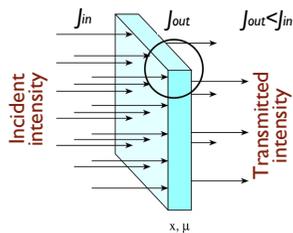
As radiation travels through matter, its intensity decreases



(Radiation that exits is weaker than the one that enters)

Is there a simple, general law to describe this phenomenon?

General radiation attenuation law



A given quantity (J) and its change (ΔJ) are proportional:

$$\Delta J = -\mu \Delta x J_{in}$$

Exponential function:

$$J_{out} = J_{in} e^{-\mu x}$$

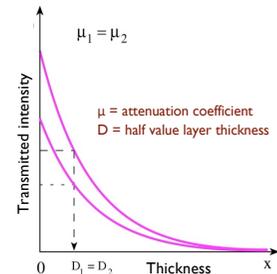
$$J = J_0 e^{-\mu x}$$

Properties of ΔJ :

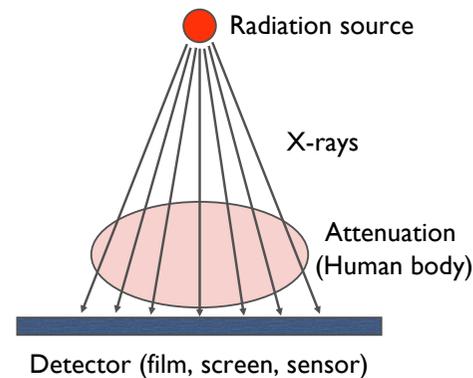
$$\Delta J \sim J_{in}$$

$$\Delta J \sim \Delta x$$

$$\Delta J \sim \mu$$



Medical relevance



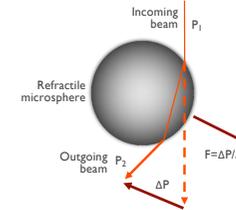
Chest x-ray

LEFTOVER FROM LECTURE 2: LIGHT REFRACTION

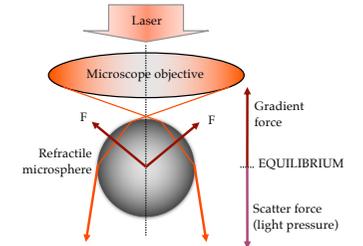
MIKLÓS KELLERMAYER

Manipulating objects with refraction

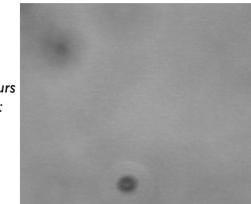
Refraction is accompanied by photonic momentum change (ΔP)
(Theory later):



Refractile particles may be **captured** with photonic forces:

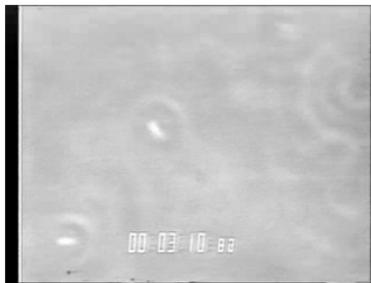


In the **optical trap** a momentum change occurs between the photons and the trapped particle:



3 μm latex (polystyrene) microspheres in the optical trap

Even cells can be captured with the optical trap



Trapping of bacterial cells

Tying a knot on a molecular filament by using optical trap

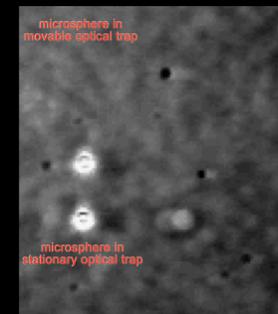
Actin filament

DNA



Phase contrast image

Fluorescence image



Fluorescence image

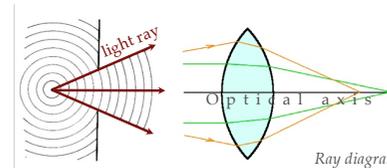
WAVE OPTICS

MIKLÓS KELLERMAYER

GEOMETRIC OPTICS AND WAVE OPTICS

Geometric optics

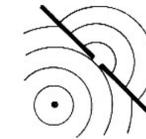
If light propagates through a slit much larger than its wavelength, then the spreading of the wavefront (phase) may be simplified into a line ("light ray").



- Optical (light) ray ("light beam"): abstraction, mathematical line.
- Arrows represent the direction of energy propagation.
- Optical axis: line connecting the midpoint of optical components (e.g., lenses).
- Principle of reversibility: the direction of energy propagation (arrows) may be reversed.

Wave optics

If light propagates through a slit comparable or smaller than its wavelength, then its wave properties must be taken into account.



Important parameters of the propagating wave:

- Period (T)
- Frequency ($f=1/T$)
- Velocity (v, c)
- Wavelength (λ): distance covered in a period:

$$\lambda = cT = \frac{c}{f}$$

Speed of propagation of light in *vacuum*: $c=2,99792458 \times 10^8 \text{ ms}^{-1}$

In *optically denser media* the speed of propagation is reduced (c_1). This may be expressed with the *absolute refractive index* (n_1):

$$n_1 = \frac{c}{c_1}$$

Wave: propagating oscillation

What is an oscillation?

Example:
Tacoma Narrows Bridge



- Tacoma Narrows Bridge ("Gallopin' Gertie")**
- ("Gertie the Dinosaur" (1914), cartoon, Winsor McCay)
 - Opening: July 1, 1940.
 - During wind (50-70 km/h): oscillation for hours
 - Oscillation amplitude initially 0.5 m, then, after snapping of a suspension cable, up to 9 m!
 - Collapse: November 7, 1940.

(Explanation of the effect)



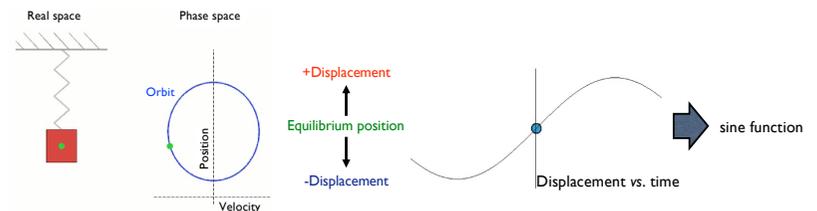
Kármán vortex street



Theodore von Kármán
1881-1963

Harmonic oscillation

Restoring force acts on a system displaced out of equilibrium (e.g., mass on a spring).



$$y = R \sin \varphi$$

Because $\phi = \omega t$: $y = R \sin(\omega t)$

If the initial phase angle (ϕ_0) differs from 0: $y = R \sin(\omega t + \phi_0)$

Because angular velocity (ω) is the full circular orbit (2π) per period (T): $y = R \sin\left(\frac{2\pi}{T} t + \phi_0\right)$

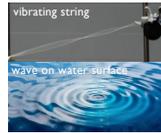
Important parameters of the propagating wave:

- Period (T)
- Frequency ($f=1/T$)
- Velocity (v, c)
- Wavelength (λ): distance covered in a period:

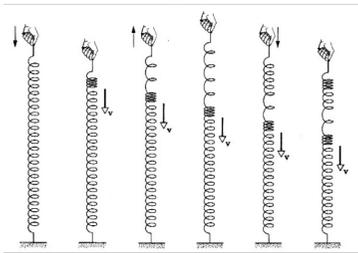
$$\lambda = cT = \frac{c}{f}$$

Types of waves

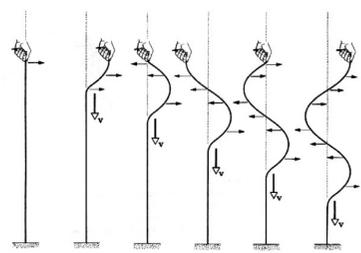
- According to **source**:
 1. Mechanical: elastic deformation propagating through elastic medium
 2. Electromagnetic: electric disturbance propagating through space (vacuum)
- According to **propagation dimension**:
 1. One-dimensional (rope)
 2. Surface waves (pond)
 3. Spatial waves (sound)
- According to **relative direction of oscillation and propagation**:



1. Longitudinal



2. Transverse



Wave phenomena I.

Diffraction

Huygens-Fresnel principle:
every point of a wavefront is the source of further waves

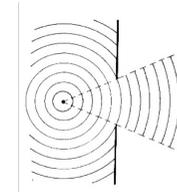


Christiaan Huygens (1629-1695)

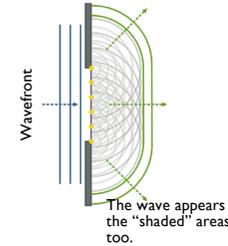


Augustin-Jean Fresnel (1788-1827)

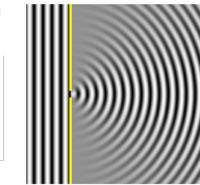
Slit much greater than the wavelength (λ)



Slit much smaller than wavelength (λ)

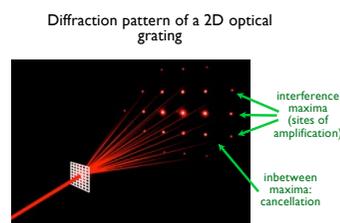
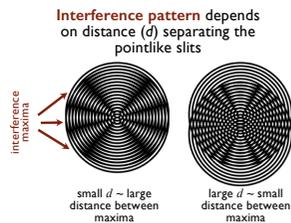
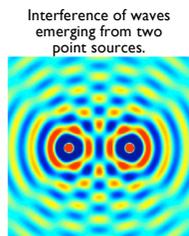
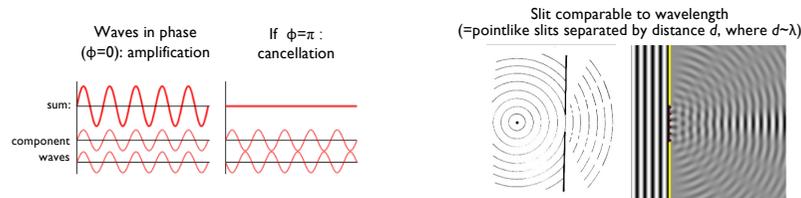


The wave appears in the "shaded" areas, too.



Wave phenomena II. interference

Principle of superposition



Wave phenomena III. Polarization

Polarization

- **Polarization**: oscillation is oriented in some preferred direction
- **Birefringence** is related to polarization: anisotropic propagation velocity
- Only **transverse** waves can be polarized.



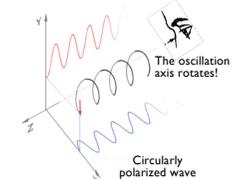
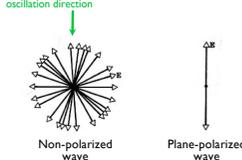
Polarization of Mechanical waves



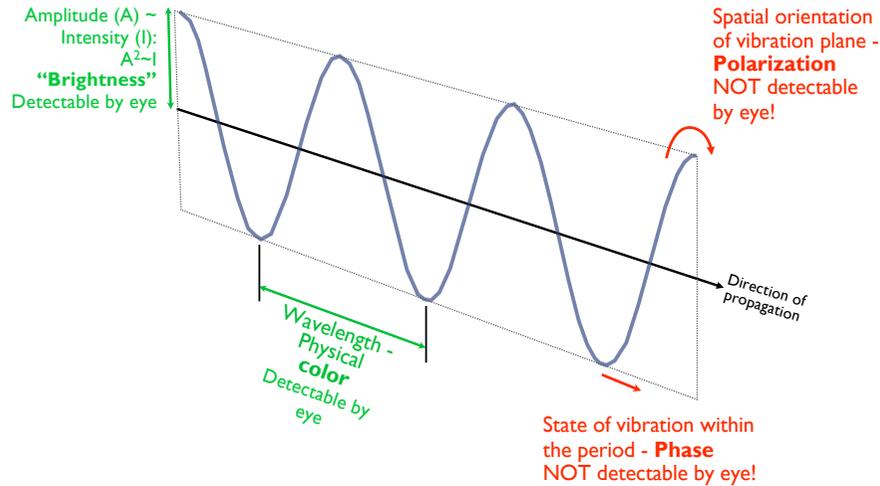
Polarization of Electromagnetic waves



Polarization can be understood by observing the head-on view of the wave:

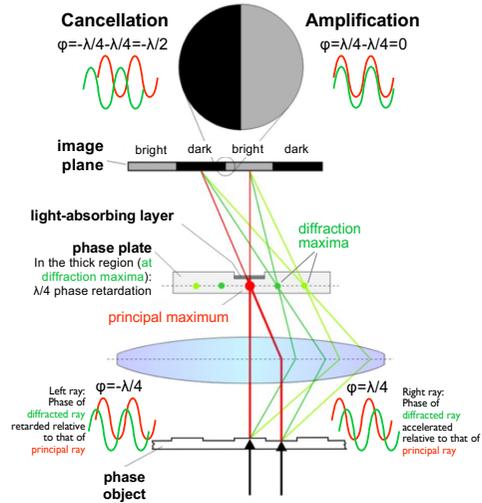


Detectable parameters of the light wave



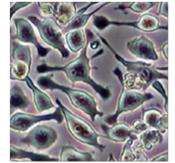
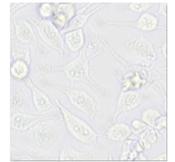
Origin and nature of wave: next week!

Phase, phase contrast microscopy



- Phase: shows the state of vibration within the entire period (2π).
- Expressed with the phase angle (ϕ).
- Phase difference between waves: phase shift (retardation or acceleration)

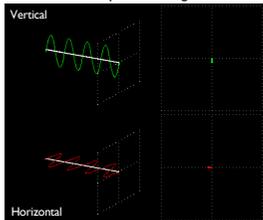
Live (unstained) cells



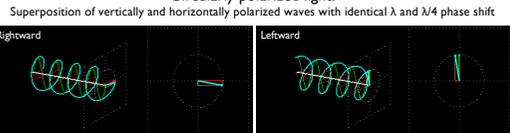
Polarized light and its interactions

Direction of the vibration (electric or magnetic field) has preferred orientation

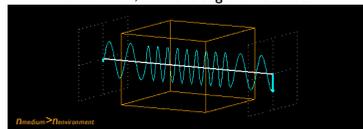
Plane-polarized light



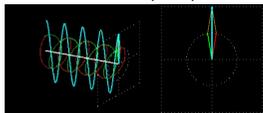
Circularly polarized light:



Light decelerates in optically dense medium; because its frequency is constant, its wavelength is reduced.

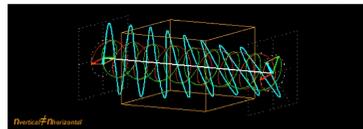


Superposition of a right- and leftward circularly polarized wave results in plane-polarized light.



Orientation of polarization plane depends on the relative phase of the two circularly polarized waves

In an anisotropic* medium a phase shift occurs between the circularly polarized components: the polarization plane of the emerging wave **rotates**.

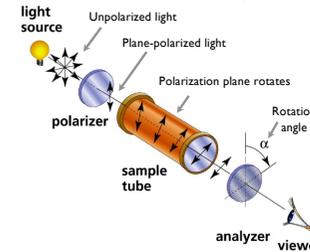


*Anisotropy (birefringence): refractive index (~light speed) is orientation dependent (i.e., in different directions within the sample, light propagates with different speeds).

Movies - http://cddemo.sziolab.org/index_hu.html

Applications of polarization

Polarimetry



Rotation angle depends on the concentration (c) of the optically active* material:

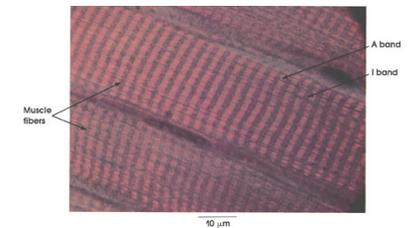
$$\alpha = [\alpha]_D^{20} \cdot c \cdot l$$

$[\alpha]$ = specific angle of rotation ("20": room temperature; "D": emission spectral line of Na $\lambda = 589$ nm)
 l = length of sample tube

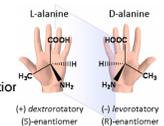
*Optically active material: contains **chiral** (mirror-symmetric) molecules that rotate the plane of polarization

Polarization microscopy

Cross-striated skeletal muscle in the polarization microscope



- A-band: anisotropic (birefringent) region (contains myosin helically ordered myosin molecules)
- I-band: isotropic region



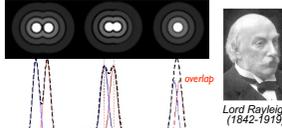
Resolution of the human eye I.

Diffraction limit

Because of diffraction: image of a point object is an Airy disk



Rayleigh criterion: objects may be resolved if their corresponding Airy disks do not overlap



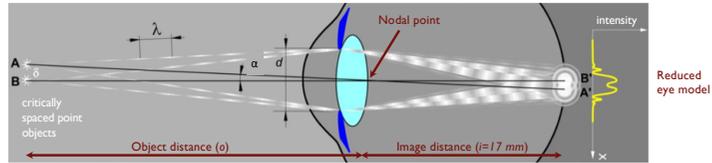
Smallest resolved distance has a limit (Abbe equation):

$$d = \frac{0.61\lambda}{n \sin \alpha}$$

λ = wavelength
 n = refractive index of medium
 α = angle between axis and outermost ray



Diffraction limit of the human eye



Limiting visual angle: $\alpha_H = 1.22 \frac{\lambda}{d}$ Smallest angle of view at which two closely spaced objects may be resolved. At average wavelength (550 nm) and pupil diameter (4 mm): **0.6'** (angular minutes)

Resolution of the human eye II.

Biological limit: receptor cell density

Object	Image on receptors	Sensed image
Two widely spaced points	Two distinct clusters of receptor cells	Two distinct points
Two closely spaced points	Two overlapping clusters of receptor cells	One blurred point
Two very closely spaced points	One large cluster of receptor cells	One blurred point

- Condition of resolution: at least one inactivated receptor cell falls in between two activated ones. The limiting angle of view under this condition is $(\alpha_B) \approx 0.8'$
- The diffraction and biological limits of the human eye are **comparable!**

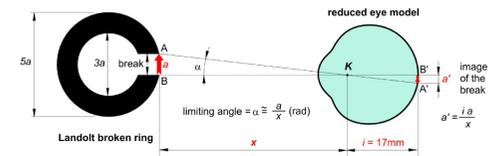
Visual Acuity ("visus", vision):

$$visual_acuity = \frac{1'}{\alpha}$$

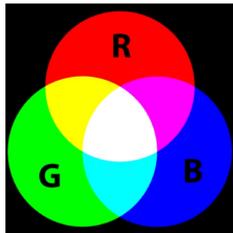
α = experimental (measured) visual angle

Average visual angle in healthy humans: $1'$ (= 100% vision)

Measurement of visual acuity



Color coding, color vision



Additive color coding

Any color may be generated by mixing three basic colors (R=red, G=green, B=blue) with varying weighing factors.

$$X = rR + gG + bB$$

In the human eye:

- 3 different color-sensitive receptors.
- Each receptor absorbs in different regions of the visible spectrum (R=64%, G=32%, B=2%).

Absorption spectra of the human color-sensitive receptors (cones)

