

# X-ray – CAT-scan

Principles of X-ray diagnostics,  
Computer Assisted Tomography

# Repetition, definitions

1. Define the X-ray radiation!
2. What processes lead to the attenuation of X-ray radiation?
3. What is the extent of the decay?

# Decay I.

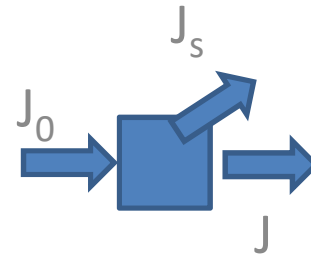
$$J = J_0 e^{-\mu \cdot x}$$

!!!Scattering:

$J_s$ : scattered intensity

elastic scattering

Compton scattering

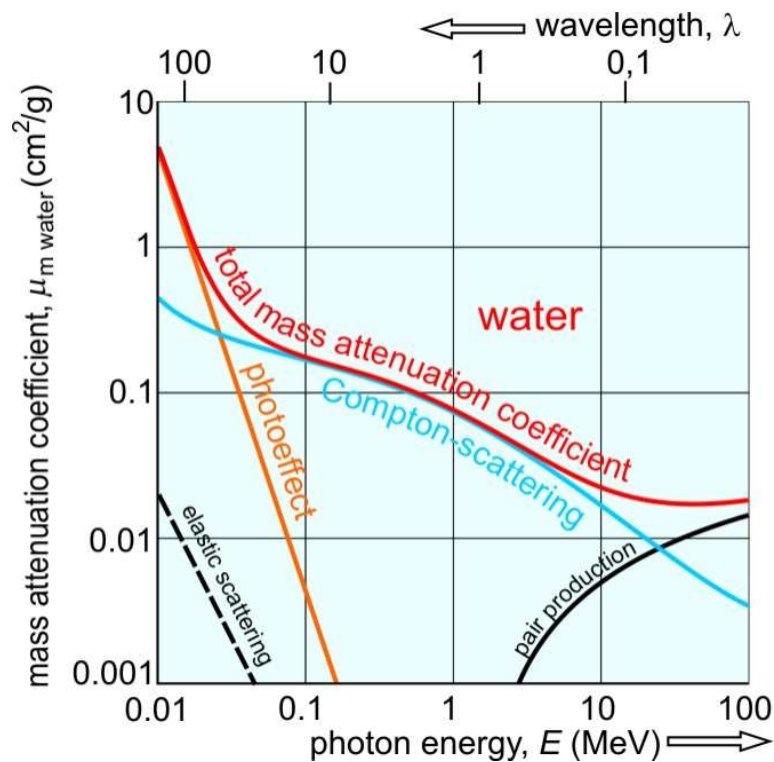


# Decay II.

$$J = J_0 e^{-\mu \cdot x}$$

$\mu$  depends on:

- Atomic number (Z), density ( $\mu = \mu_m \rho$ )  
together: electron density: probability of absorption effects
- energy

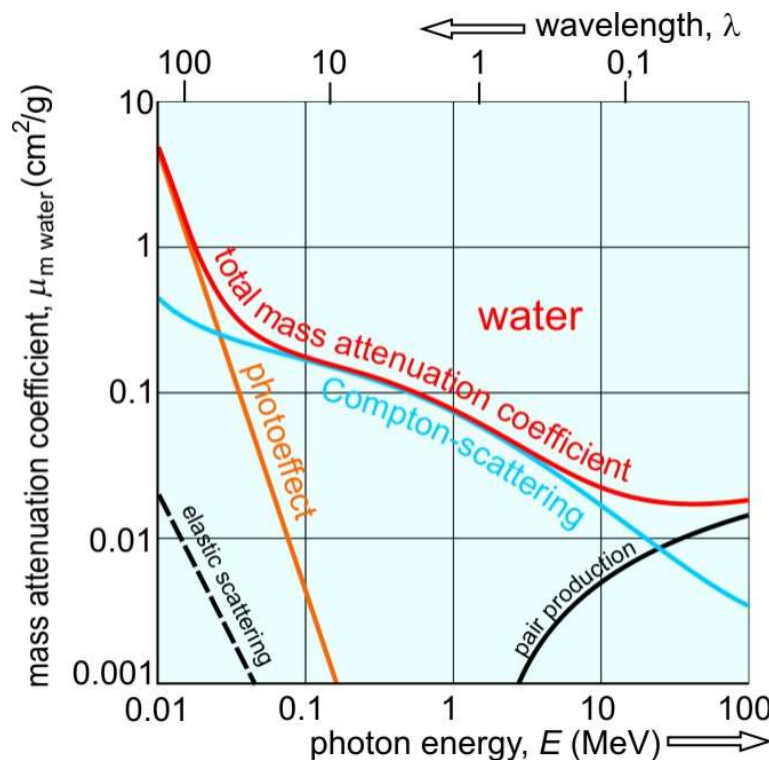


# Decay III.

$$J = J_0 e^{-\mu \cdot x}$$

$\mu$  depends on:

- Atomic number (Z), density ( $\mu = \mu_m \cdot \rho$ )  
together: electron density: probability of absorption effects
- energy



!!!NOT independent:

Absorption process	$\mu_m$ depends on Z	$\mu_m$ depends on fotonenergy (E)
elastic scattering (more probable at lower E)	$\mu_m \sim Z^2$	$\mu_m \sim 1/E^2 \sim \lambda^2$
fototeffect (more probable at lower E)	$\mu_m \sim Z^3$	$\mu_m \sim 1/E^3 \sim \lambda^3$
Compton scattering (more probable at higher E)	$\sim \text{indep.}$	$\sim \lambda$

(+complication: continous E spectra)

# Aim: Imaging

Basis:

Transmission (Absorbance) method:

the extent of absorption in a known “place” :

Gathered information:

usually morphological

rarely functional (DSA, lung movement)

Type of image:

usually static

rarely dynamic

1. X-ray image: 2D „summation” image
2. CT (CAT-scan) image: 3D

# X-ray Image

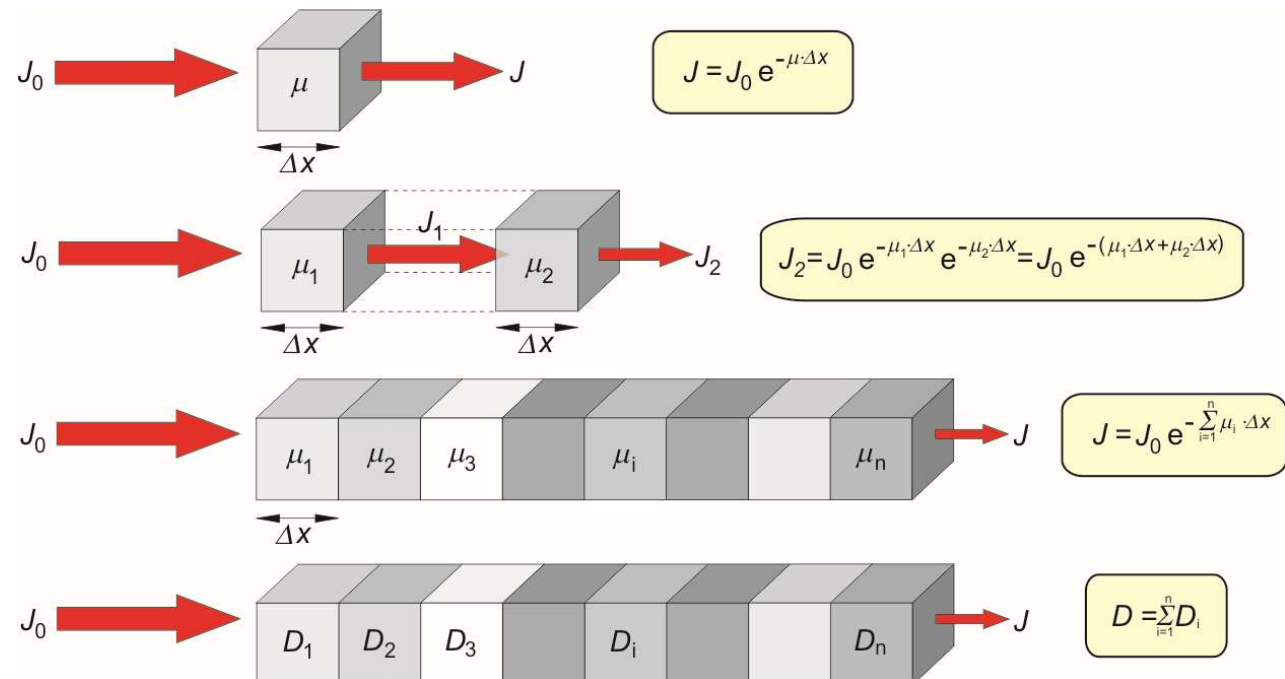
## 1. 2D – summation image:

$$J = J_0 e^{-(\mu_1 \Delta x + \mu_2 \Delta x + \dots \mu_n \Delta x)} = J_0 e^{-\sum_{i=1}^n \mu_i \Delta x}$$

Let us introduce the concept of **elementary density**,  $D_i = \mu_i \Delta x \cdot \lg e$ . Then, the total density of the examined body part becomes:

$$D = \lg \frac{J_0}{J} = \sum_{i=1}^n D_i$$

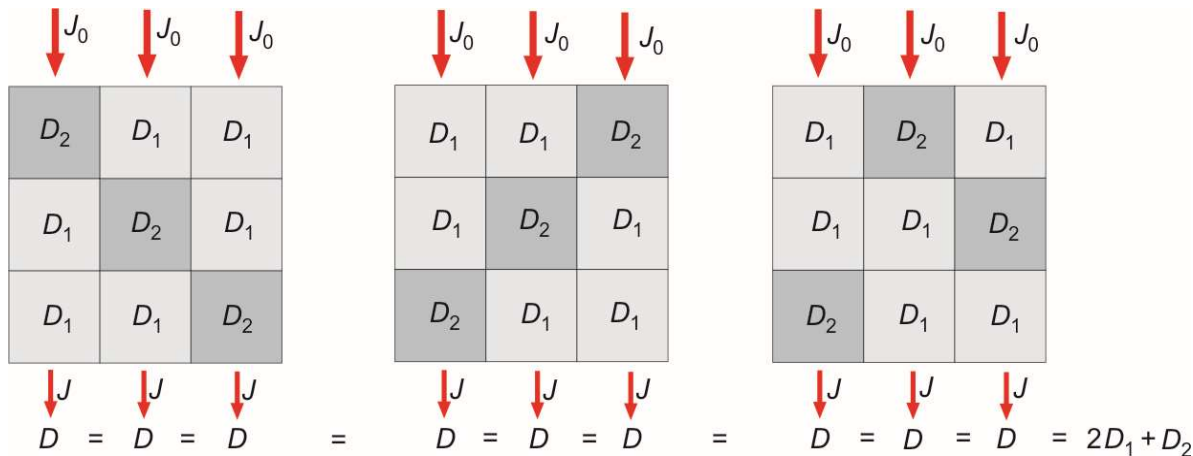
*Concept and properties of one element (pixel) of the summation image*



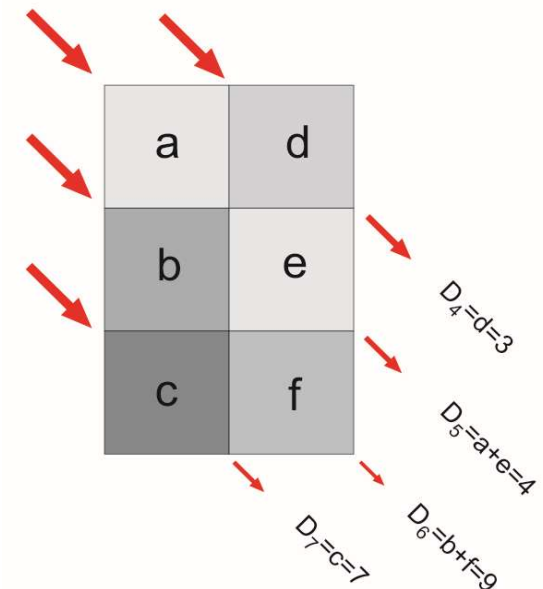
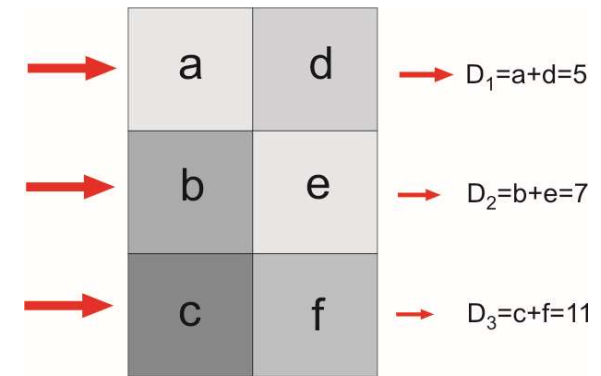
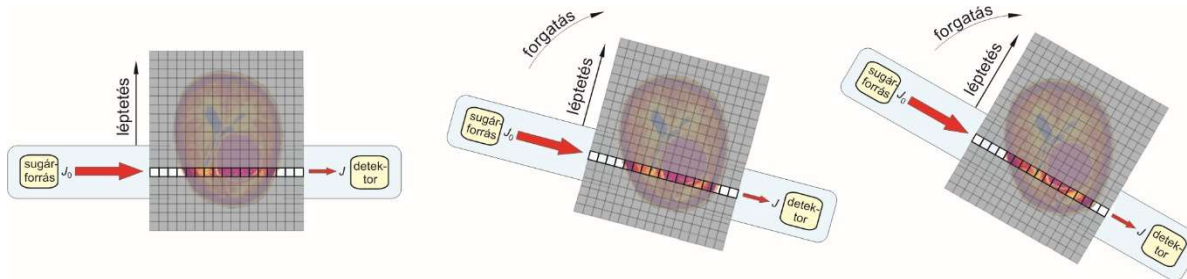
# CT Image

## 2. CT kép

*Elementary densities of the image projected on top of each other cannot be revealed by measurement from one direction only. In all the 3 cases the same summation image is obtained.*



*Elementary densities can be calculated from the summation data*





# Demonstration measurement

❖ 16\_CAT-SCAN - Summation image and 3D reconstruction.mp4

# Model measurement

❖ 17\_CAT-SCAN - Measurement with a phantom.mp4

# Lab report

❖ see excel file

# The Image

What is needed to separate two points in an image?

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❖ 21\_CAT-SCAN - demonstration of the DSA principle.mp4

# The image

What is needed to separate two points in an image?

- contrast difference: X-ray density for X-ray and CT
- resolution

the quality of image depends on too:

- Signal/noise ratio
  - noise: external noise+ internal noise
  - + scattering! (elastic and Compton)