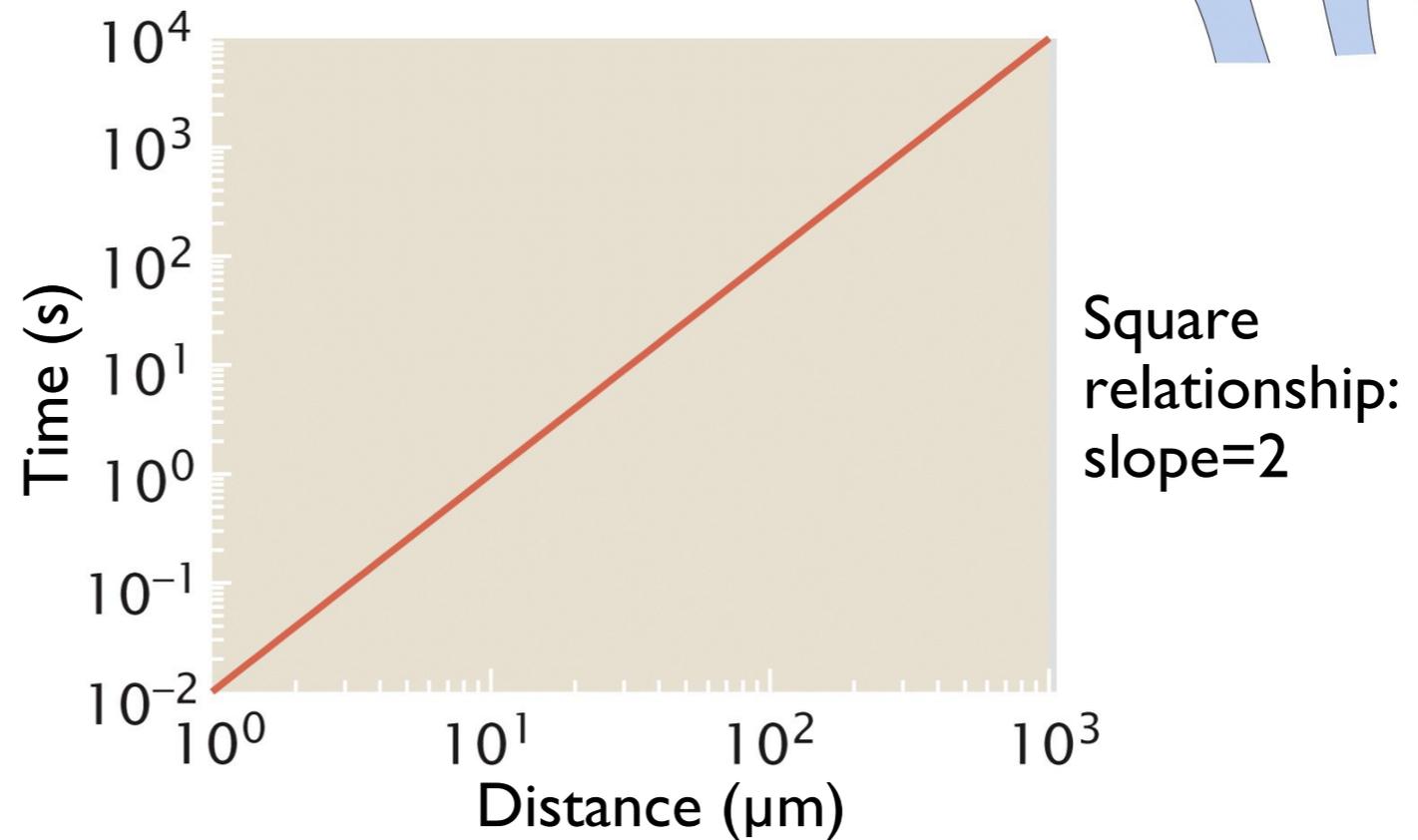
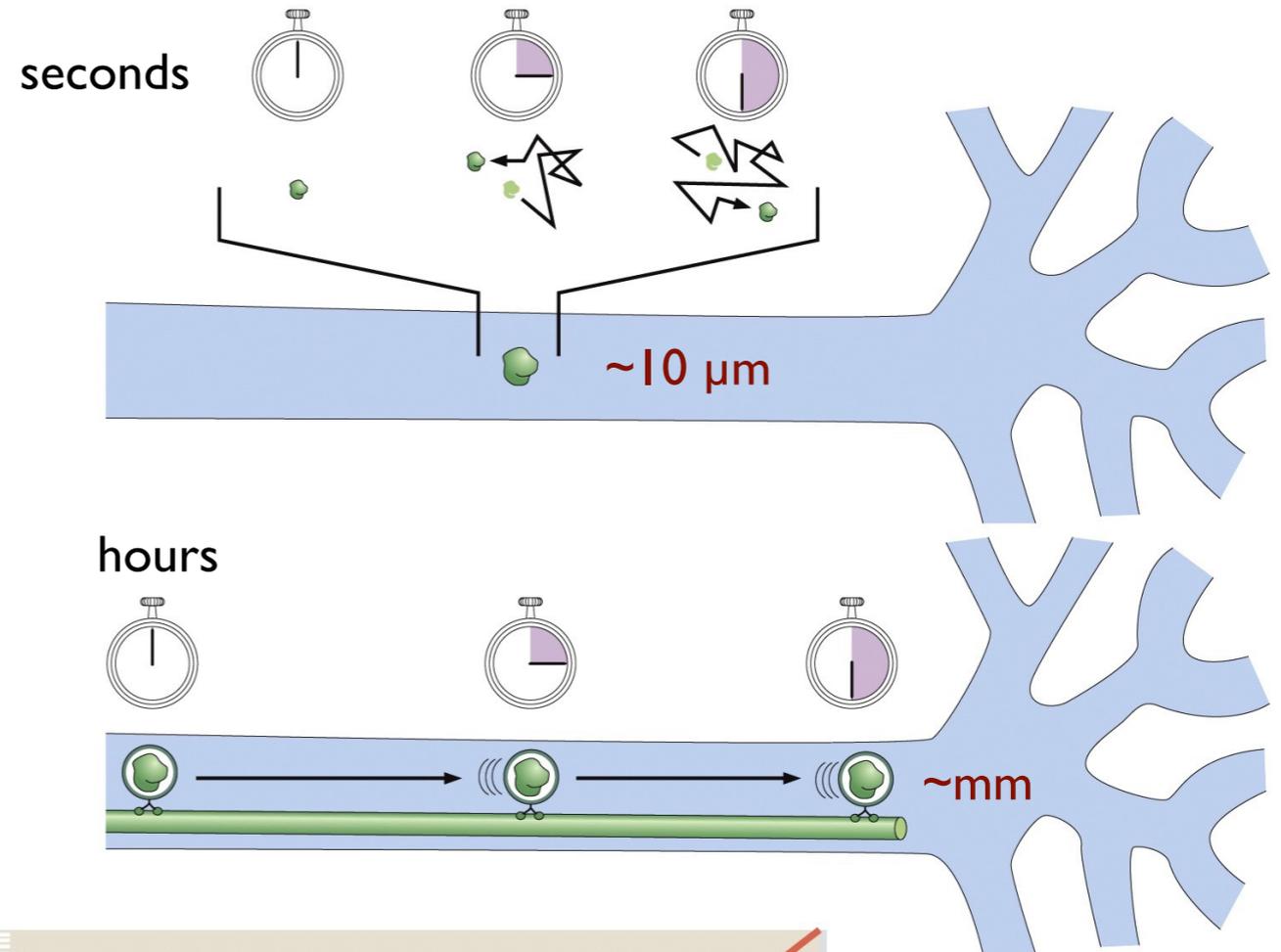
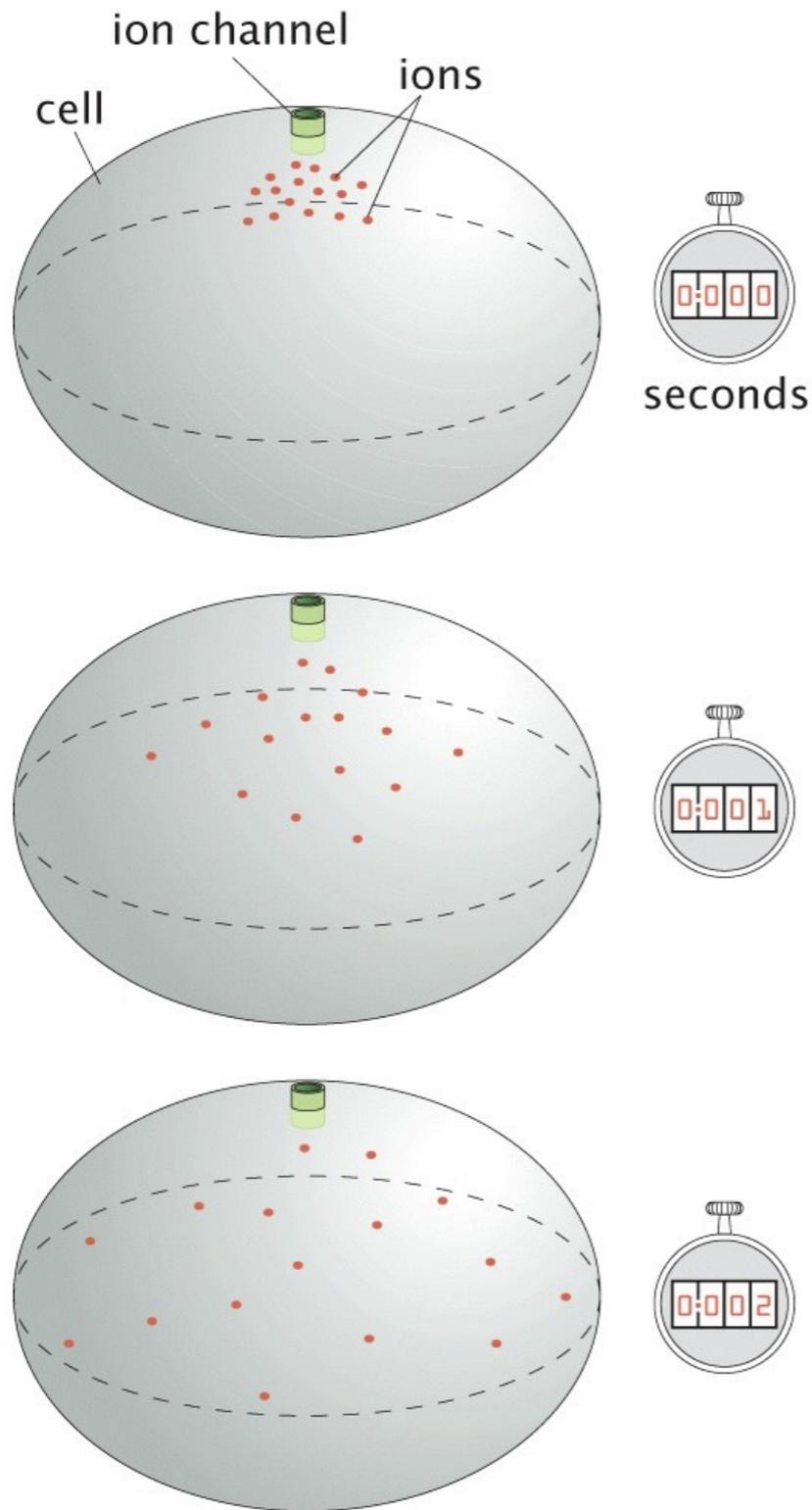


FLOW OF FLUIDS AND GASES

BLOOD AS FLUID

MIKLÓS KELLERMAYER

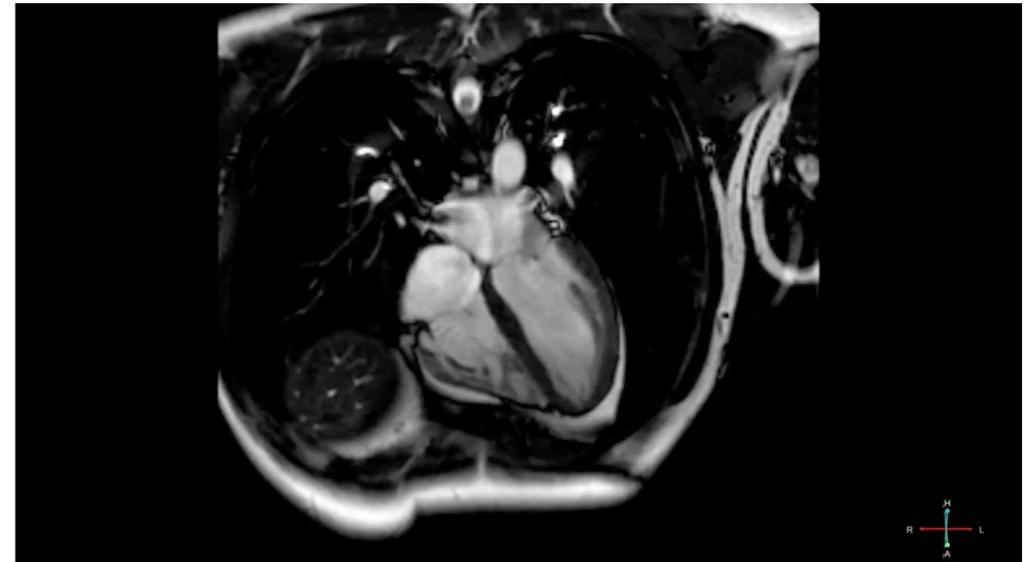
Diffusion is rapid only across small distances



Importance of the physics of fluids

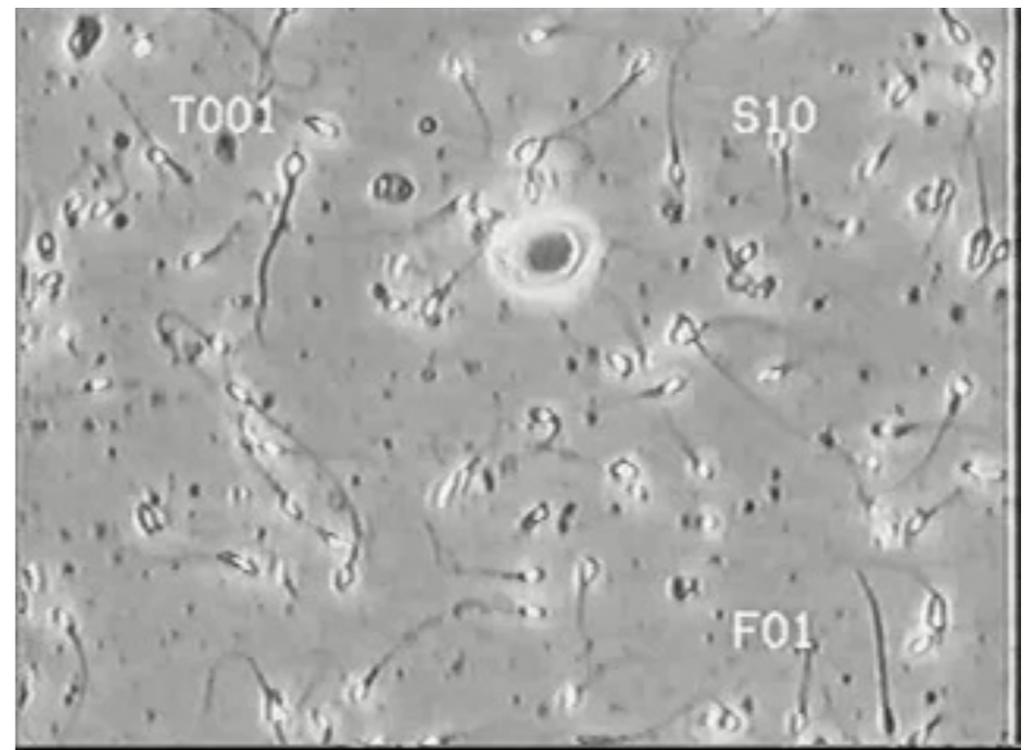
I. Hemodynamics

E.g.: What are the characteristics of blood flow in the circulatory system?
(similarly: flow of gases in respiratory system)



II. Motion in viscous fluids

E.g.: What is the force exerted by a single spermatoocyte during its motion?



N.B.: gases - in contrast to fluids - are compressible.
However, in the physiologically relevant range of pressure differences (~ 100 Pa), the changes in their volume/density are negligible.

Flow of fluids and gases

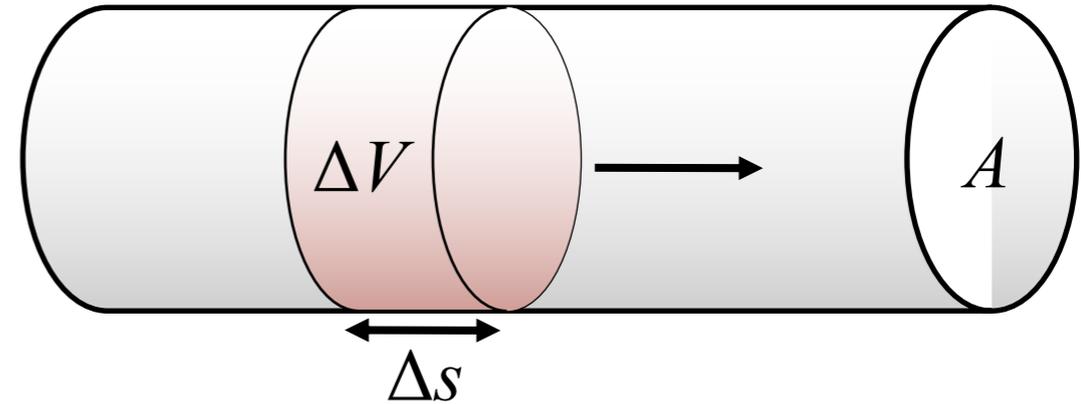
Physical properties of blood

- Basic principles
- Types of fluids
- Types of fluid flow
- Laws of fluid flow
- Blood as a fluid;
determinants of
blood viscosity

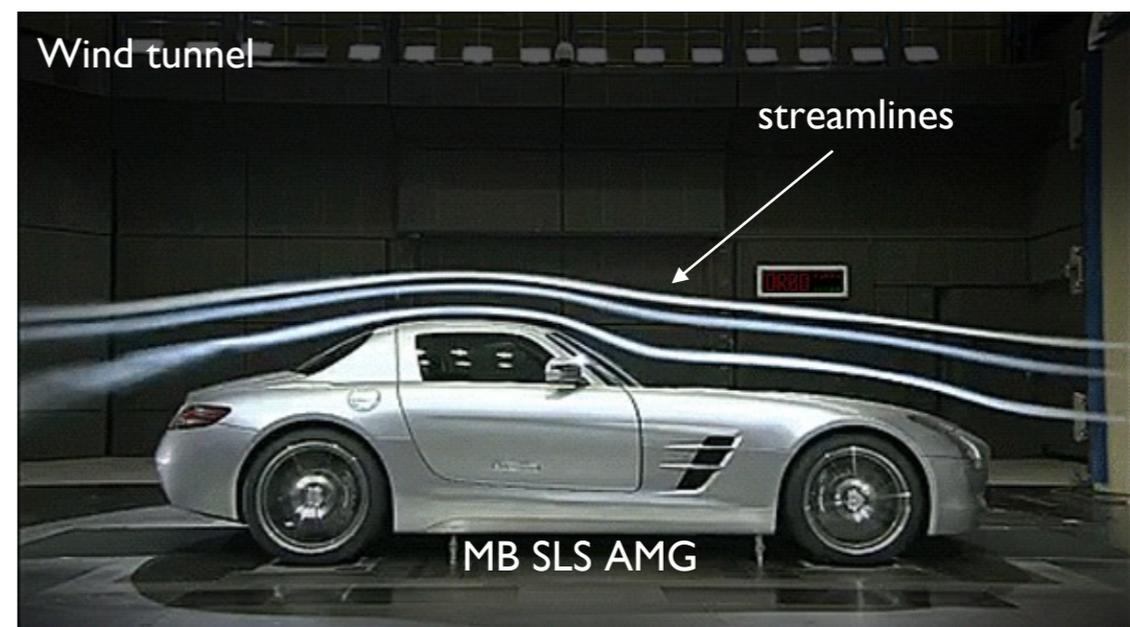
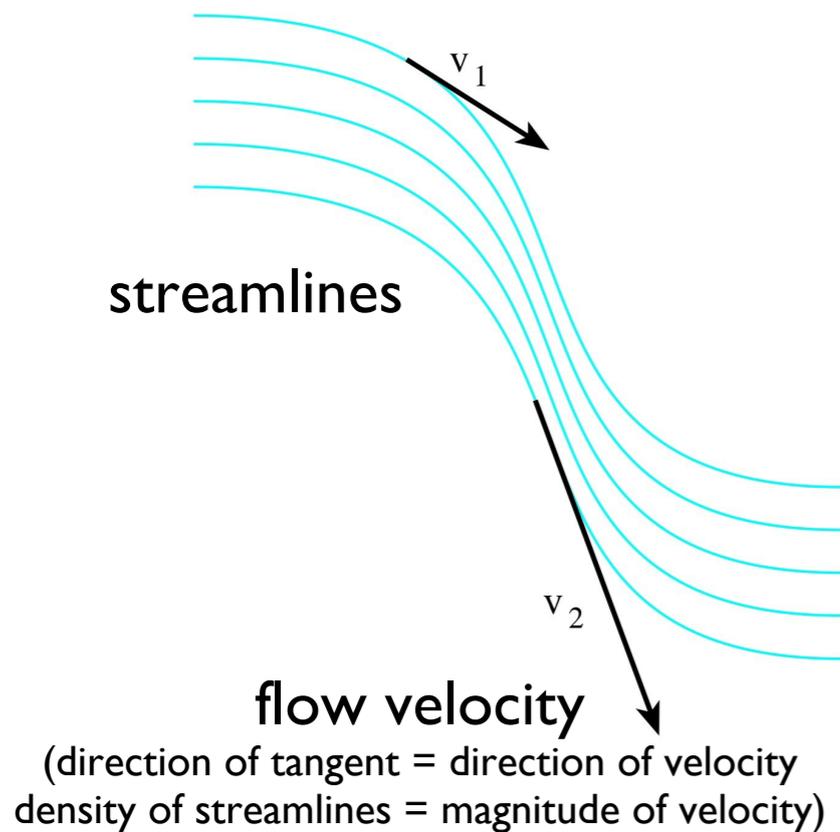
Basic principles I.

Volumetric flow rate (I_V):

$$I_V = \frac{\Delta V}{\Delta t} = A \frac{\Delta s}{\Delta t} = A \bar{v}$$



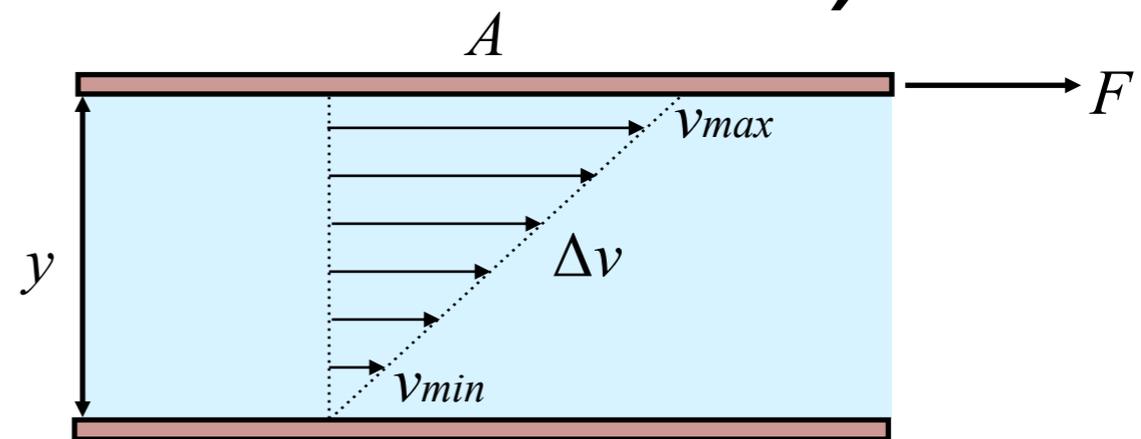
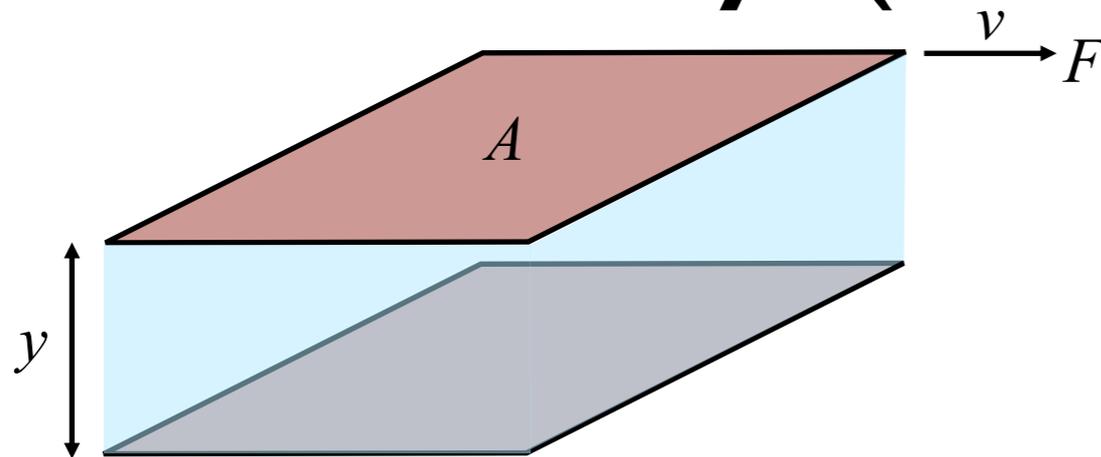
Average velocity: $\bar{v} = \frac{I_V}{A}$



Flow can be made visible

Basic principles II.

Viscosity (internal friction)



- F = shear force
- A = area of fluid layer
- η = viscosity
- v = flow velocity
- y = distance between fluid layers
- F/A = shear stress (τ)
- $\Delta v/\Delta y$ = velocity gradient (D)

$$\frac{F}{A} = \eta \frac{\Delta v}{\Delta y} \quad (\text{Newton's friction law})$$

$$\eta = \frac{\tau}{D}$$

Units of viscosity: $1 \text{ Pas} = 1 \frac{\text{Ns}}{\text{m}^2} = 10 \text{ P} (\text{poise})$

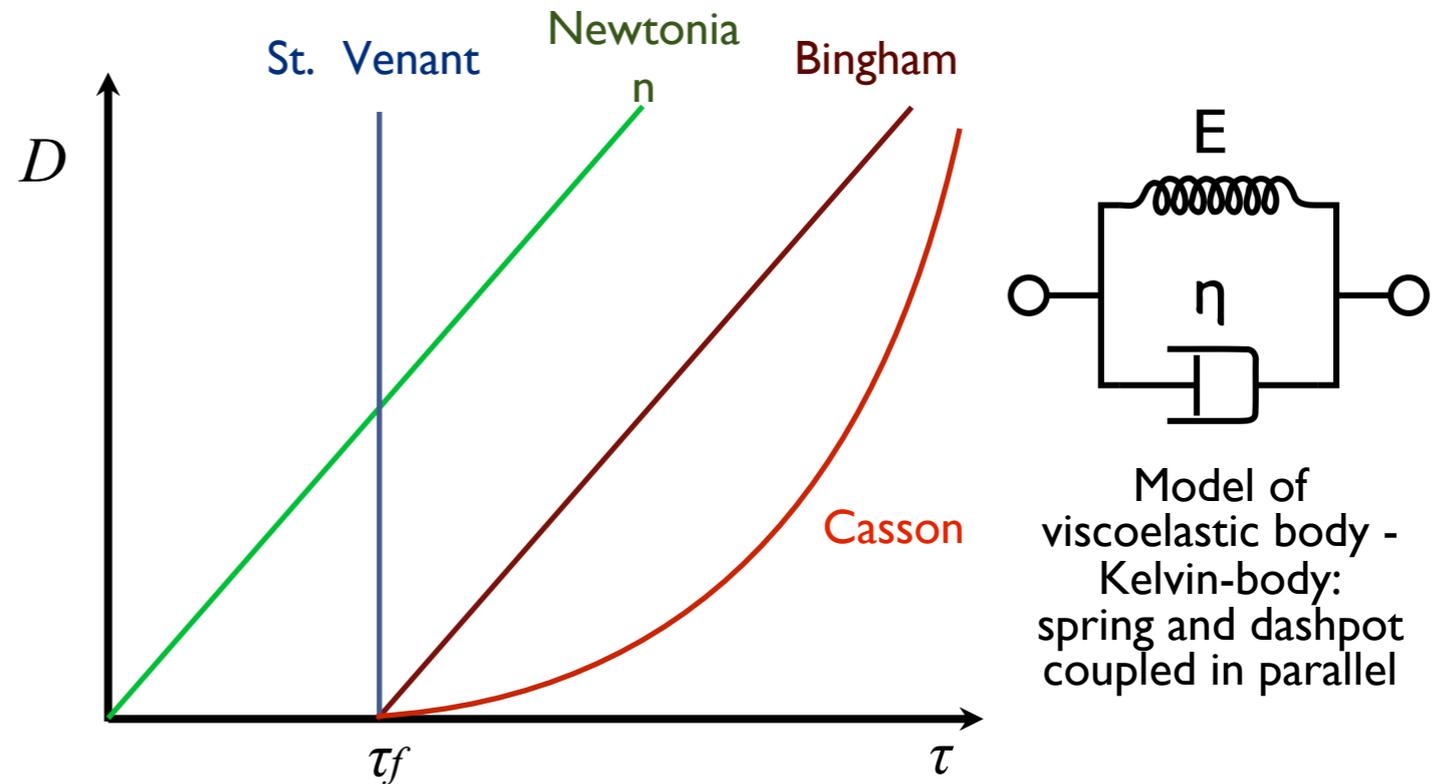
Viscosity of distilled water (25 °C): 1 mPas (1 centipoise)

N.B.: in gases: $\eta \sim T$
Momentum exchange between particles acts against the gliding of layers past one another.

fluids: $\eta \sim e^{E/k_B T}$
Viscosity decreases with the increase in the relative concentration of vacancies.

Types of fluids

Relationship between velocity gradient and shear stress in **real** fluids



1. Ideal

frictionless, incompressible
 $\rho = \text{constant}$, $\eta = 0$

2. Non-ideal (real)

a. Newtonian (viscous)

η independent of shear stress

b. Non-newtonian (anomalous)

η changes with shear stress

- $\tau_f = \text{flow threshold}$
- Viscoelastic materials: combination of viscous and elastic properties (e.g., solution of polymers, macromolecules)
- Stress-relaxation: decay of stress in rapidly deformed viscoelastic body.
- Blood is a non-newtonian fluid; it displays viscoelastic properties.

Types of fluid flow

1. Stationary

Volumetric flow rate stays constant (parameters characterizing flow remain unchanged).

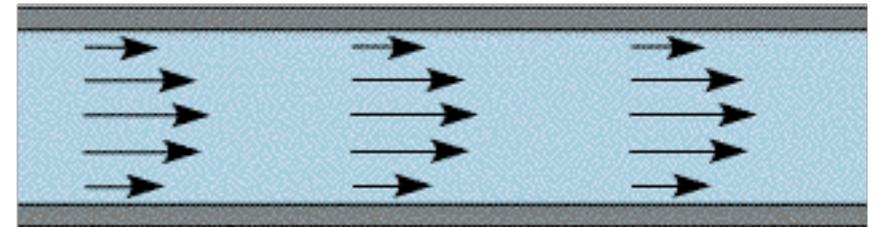
2. Laminar

Fluid layers do not mix.

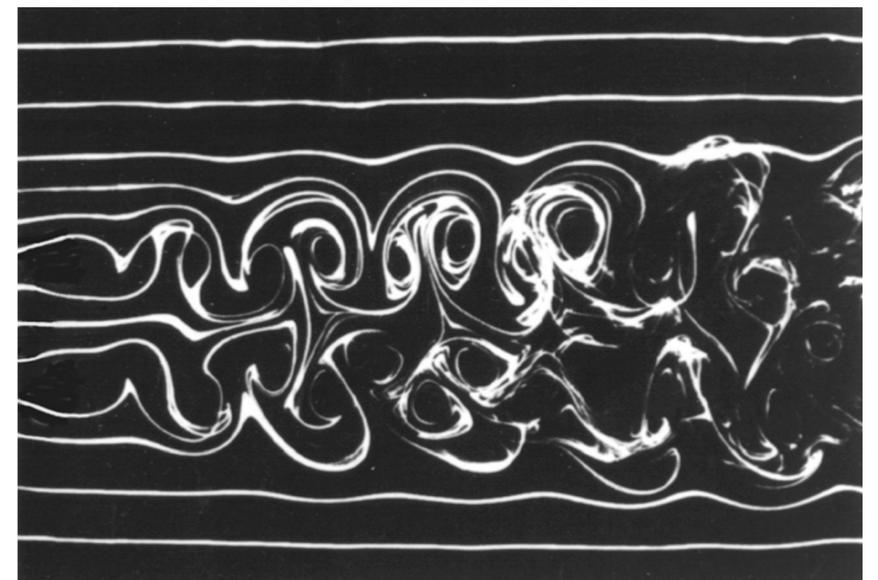
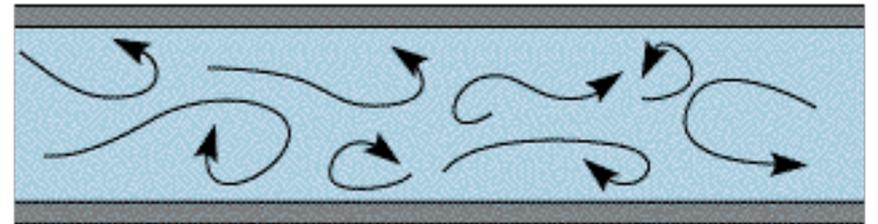
3. Turbulent

Fluid layers mix.

laminar flow



turbulent flow



Reynolds number (Re):

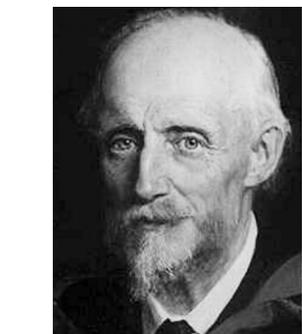
$$Re = \frac{vr\rho}{\eta}$$

v = flow rate (m/s)

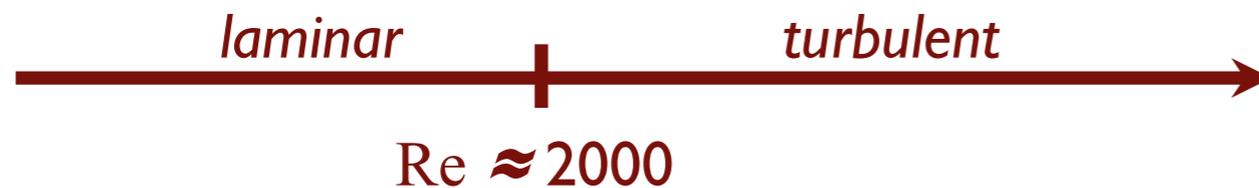
r = tube radius (m)

ρ = density of fluid (kg/m³)

η = viscosity (Ns/m²)



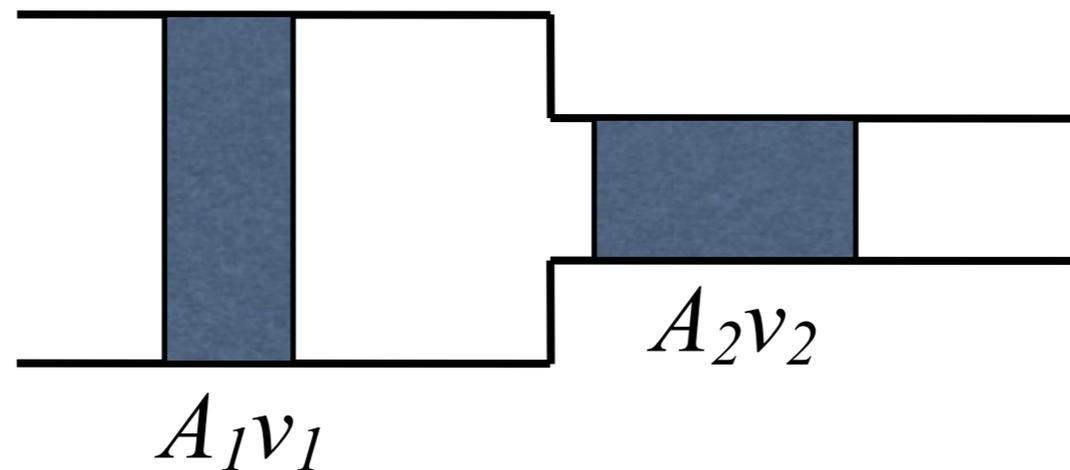
Osborne Reynolds
(1842-1912)



"When I meet God, I am going to ask him two questions: Why relativity? And why turbulence? I really believe he will have an answer for the first." (Werner Heisenberg)

Laws of flow in ideal fluids I.

Continuity equation:
volumetric flow rate is constant



$$A_1 v_1 = A_2 v_2 = \text{constant}$$

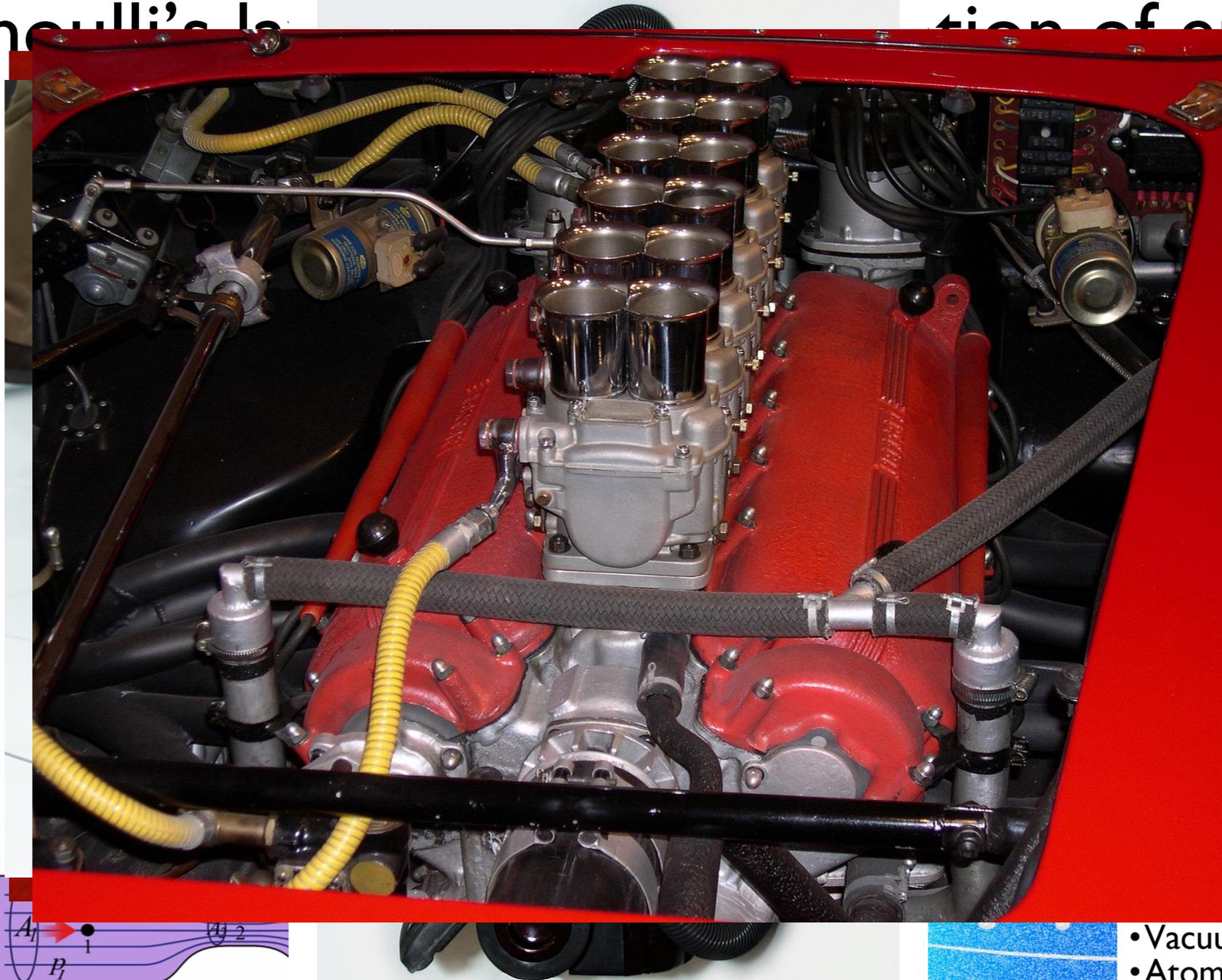
A = cross-sectional area
 v = flow velocity

Laws of flow in ideal fluids II.

Bernoulli's law Conservation of energy



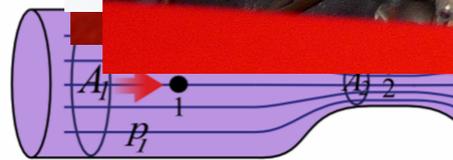
Daniel Bernoulli
(1700-1782)



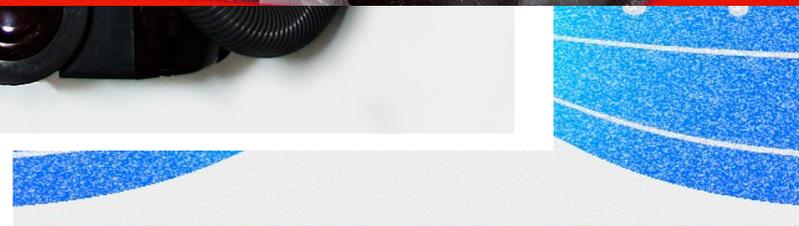
pressure
dynamic pressure
static pressure



Giovanni Battista
Venturi
(1746-1822)



Static pressure drops at the
tube narrowing



Venturi tube

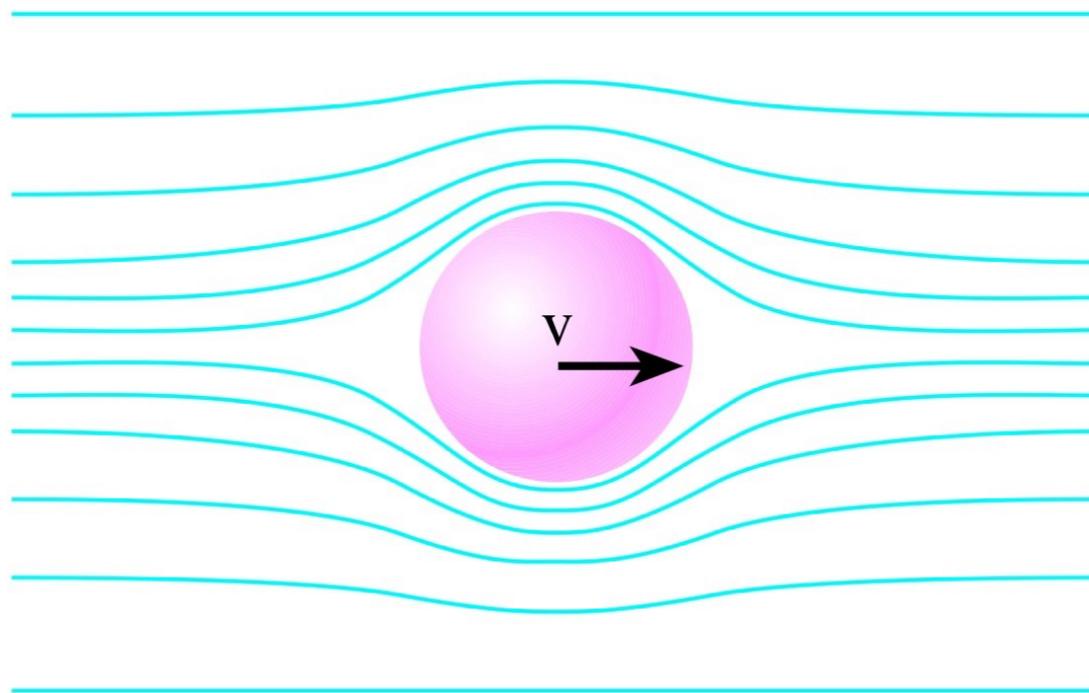
- Pulsic pulse (*pulsus* *tenuis*) in aorta insufficiency
- Vacuum pump
- Bunsen-burner
- Volumetric flow rate
- Vacuum cleaner
- Atomizer, spray, carburetor
- Leadpipe and barrel of wind instruments
- Diffuser

Laws of flow in viscous fluids I.

Stokes' law



Georg Gabriel Stokes
(1819-1903)



$$F = \gamma v = 6r\pi\eta v$$

F = force

γ = drag coefficient (shape factor)

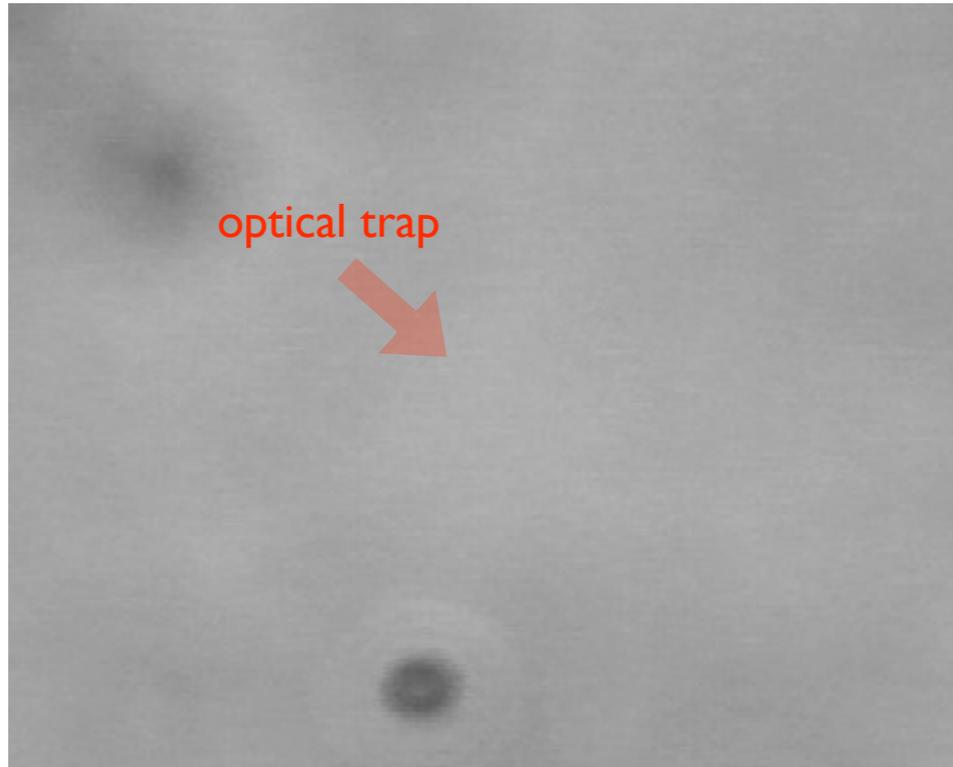
v = flow rate

r = radius of sphere

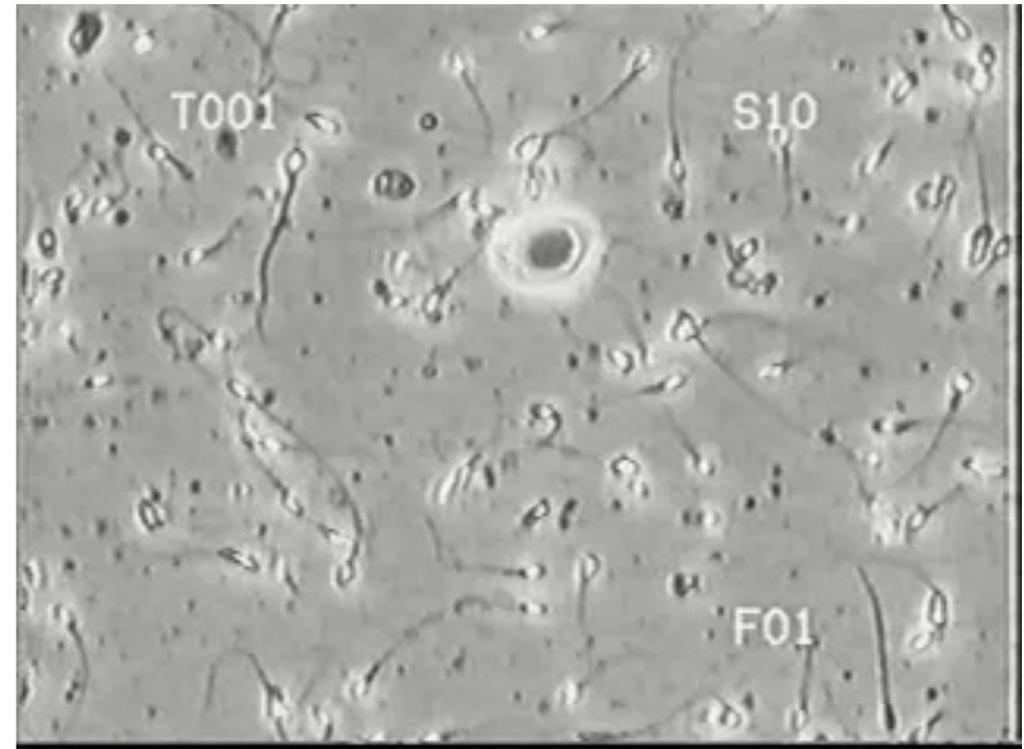
η = viscosity

Stokes force

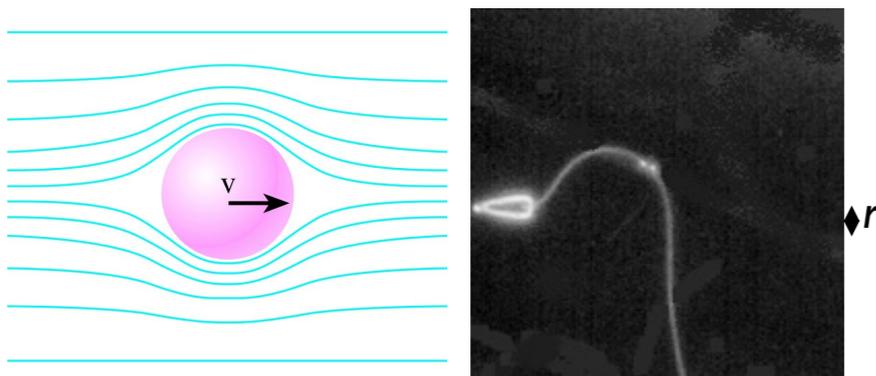
Hydrodynamic drag force (Stokes force): $F = \gamma = 6r\pi\eta v$



Affects stationary objects in moving fluid
(microbead captured in optical trap)



Affects objects moving in stationary fluid
(moving spermatozoa)



$r = 1.6 \mu\text{m} = 1.6 \times 10^{-6} \text{ m}$
 $v = 50 \mu\text{m/s} = 5 \times 10^{-5} \text{ m/s}$
 $\eta = 10^{-3} \text{ Pas}$

How much force is exerted by a single spermatozoa during its movement?

$$\gamma = 6r\pi\eta = 6 \cdot 1.6 \times 10^{-6} \cdot \pi \cdot 10^{-3} = 3 \times 10^{-8} \text{ N s/m}$$

$$F = \gamma = 3 \times 10^{-8} \text{ N s/m} \cdot 5 \times 10^{-5} \text{ m/s} = 1.5 \times 10^{-12} \text{ N} = \boxed{1.5 \text{ pN}}$$

Laws of flow in viscous fluids II.

Hagen-Poiseuille's law



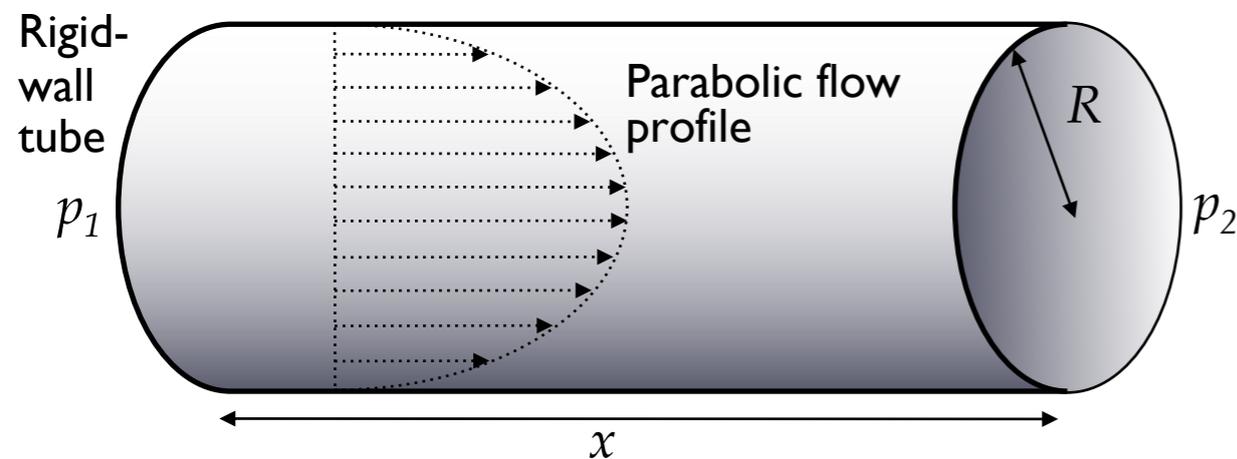
G.H.L. Hagen
(1797-1884)



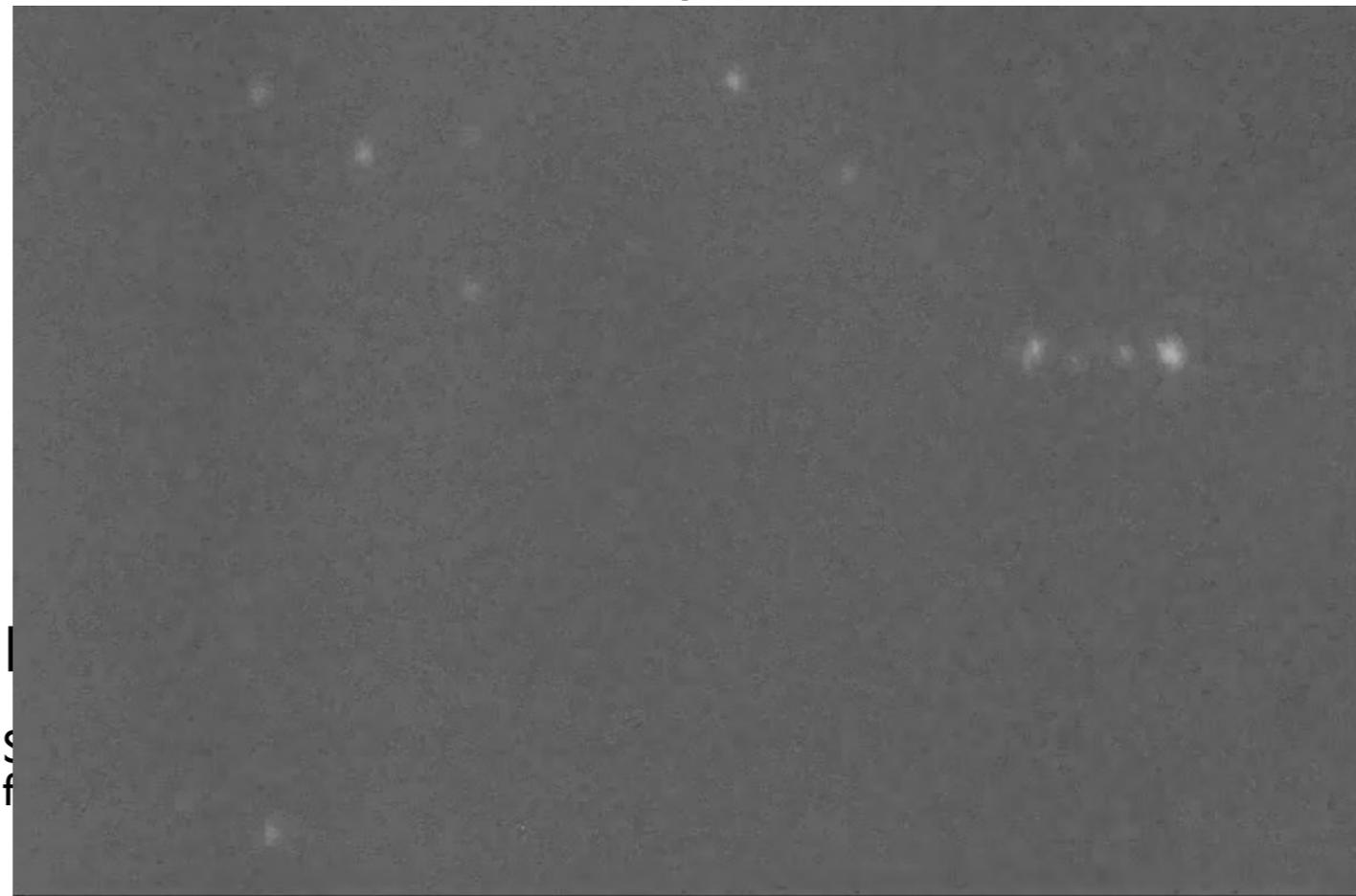
J.-L.-M. Poiseuille
(1799-1869)

| Thermodynamic current | Relevant intensive variable (its difference maintains current) | Current density | Physical law |
|-----------------------|--|--|------------------|
| Volumetric flow | Pressure (p) | $J_v = -\frac{R^2}{8\eta} \frac{\Delta p}{\Delta x}$ | Hagen-Poiseuille |

$$J_v = \frac{V}{tA} = \frac{R^2}{8\eta} \frac{\Delta p}{\Delta x}$$

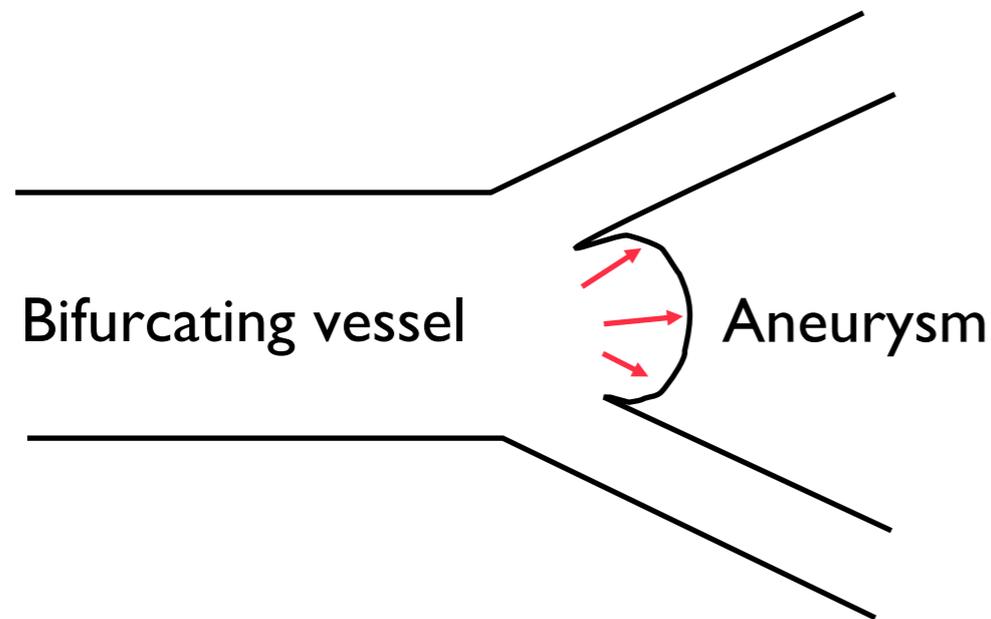


- V = volume
- t = time
- R = tube radius
- η = viscosity
- p = pressure
- x = tube length
- $V/t = I_v$ = volumetric flow rate
- $\Delta p/\Delta x$ = pressure gradient, maintained by $p_2 - p_1$ (negative!)
- A = cross-sectional area of tube
- I_v = volumetric flow rate



Medical significance of fluid flow

Bernoulli's law:



Formation of aneurysm (pathological expansion of blood vessel):

- Expansion of vessel: diameter increases
- Flow rate decreases, according to continuity equation
- Static pressure increases due to Bernoulli's law
- Aneurysm pregradates - positive feedback mechanism leading to catastrophe

Hagen-Poiseuille's law:

$$\frac{V}{t} = \frac{R^4 \pi \Delta p}{8\eta \Delta x}$$

Flow intensity, hence the delivered oxygen quantity, may be **drastically reduced** in certain pathological conditions:

- constriction of blood vessels (e.g., diabetes, B \ddot{u} rger's disease)
- change in blood viscosity (e.g., fever, anaemia)
- Reduction of vessel diameter by half leads to a reduction of volumetric flow by 1/16!

Blood as a fluid

| | | |
|--|----------------------------|-----------------------------|
| 55-60% of body mass is water 42 kg (70 kg body mass) | | |
| 2/3 intracellular 28 kg | 1/3 extracellular 14 kg | |
| | 1/3 plasma 4-5 kg | 2/3 intersticium 9-10 kg |

Blood: Average volume: 5 l
Average viscosity: 5 mPas
Average density: 1.05 g/cm³
Composition: 40-45 % corpuscular, 55-60 % plasma

Determinants of blood viscosity

I. Hematocrit (*htc*, ϕ):

$$htc = \frac{V_{cells}}{V_{total}}$$

Normal range: 0.4-0.5.

Viscosity of blood as suspension
(in the physiologically relevant *htc* range):

$$\lg \eta_s = A + B\phi$$

η_s =suspension viscosity

A, B=empirical constants

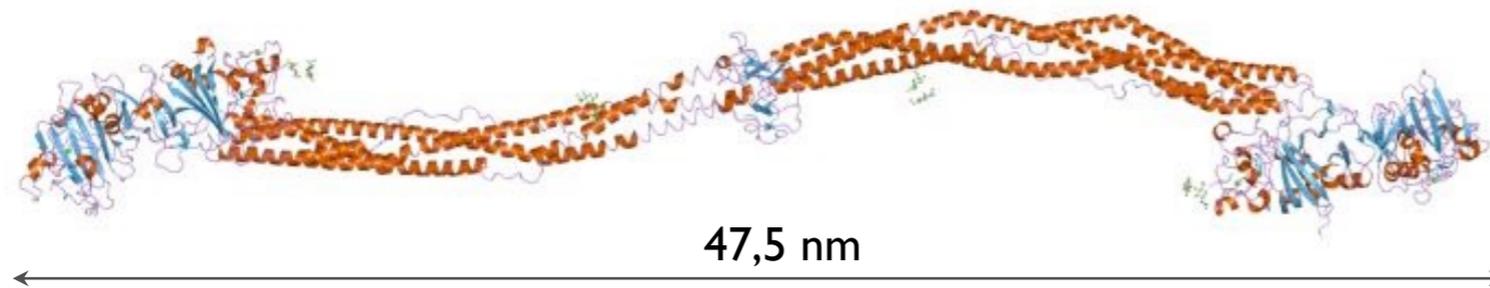
Determinants of blood viscosity

2. Plasma viscosity

- Depends on plasma proteins.
- In *paraproteinaemias* (e.g. myeloma multiplex or plasmocytoma) the concentration of immunoglobulins is high, leading to increased viscosity.

| Plasma protein | Normal concentration | % ratio | Function |
|-----------------------|-----------------------------|----------------|---|
| Albumin | 35-50 g/l | 55% | maintenance of colloind osmotic pressure, transport |
| Globulins | 20-25 g/l | 38% | Part of the immune system |
| Fibrinogen | 2-4.5 g/l | 7% | Blood coagulation |

Fibrinogen, fibrin

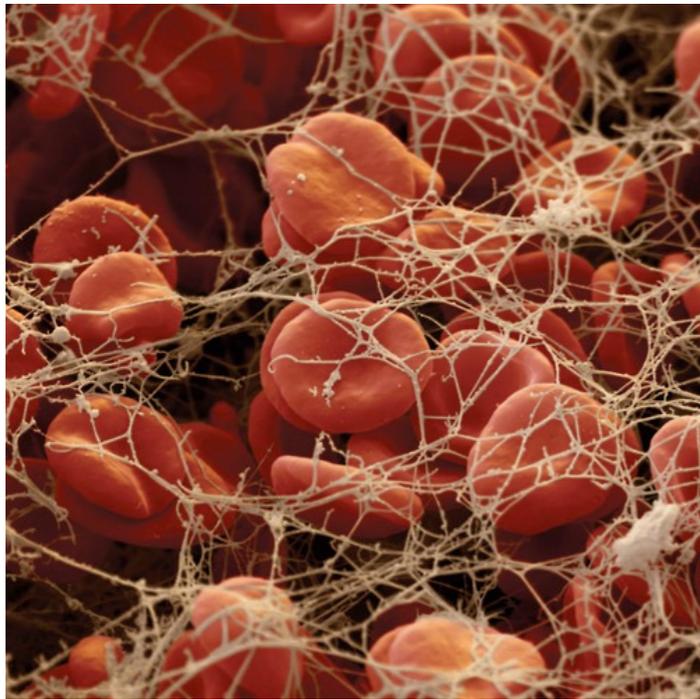


Fibrinogen:

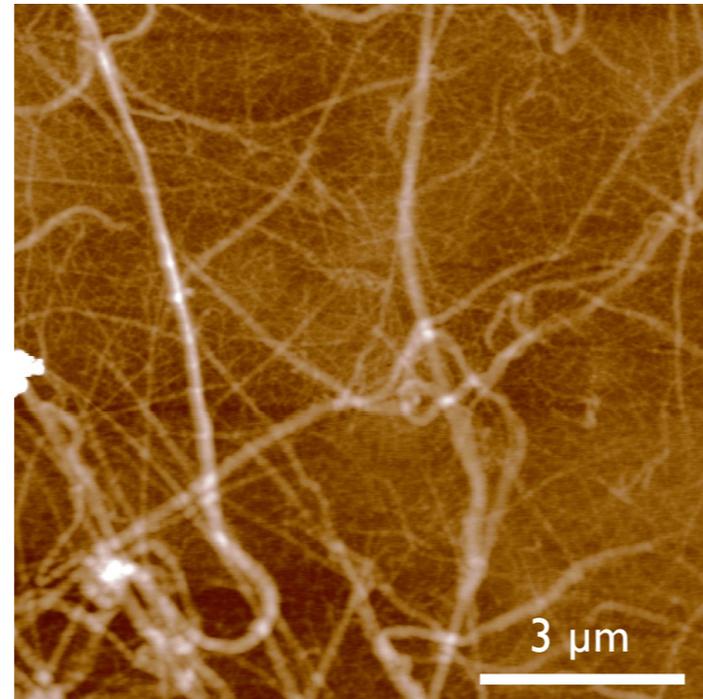
MW = 340.000 Da

In plasma: 2-4 g/l \approx **10 μ M**

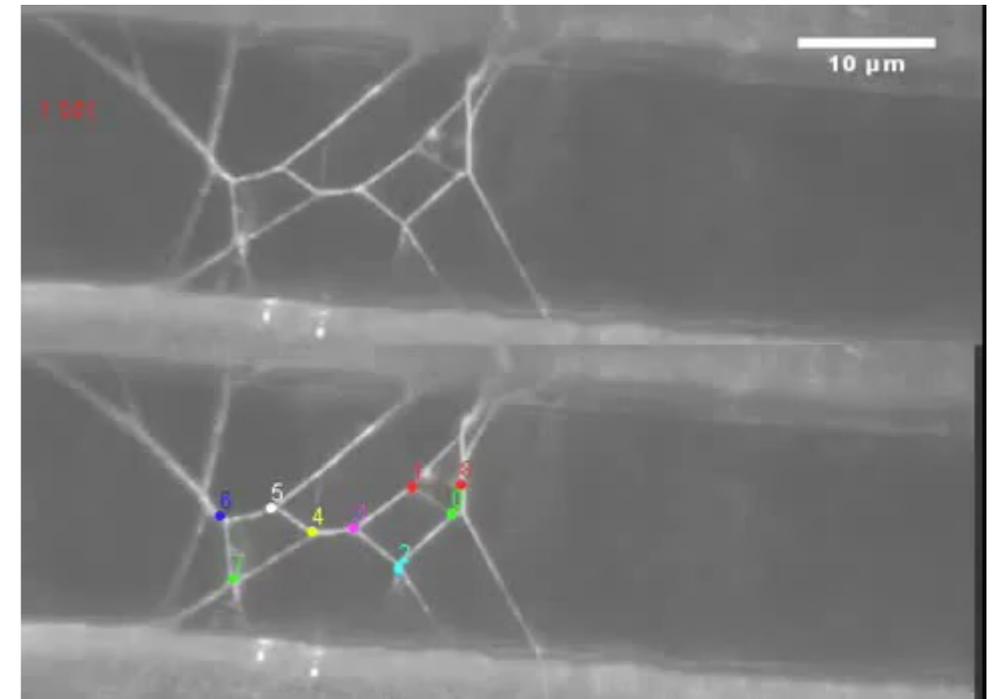
Average nearest-neighbor distance \approx **55 nm**



Red blood cells in fibrin meshwork



Fibrin polymerized in vitro (AFM)

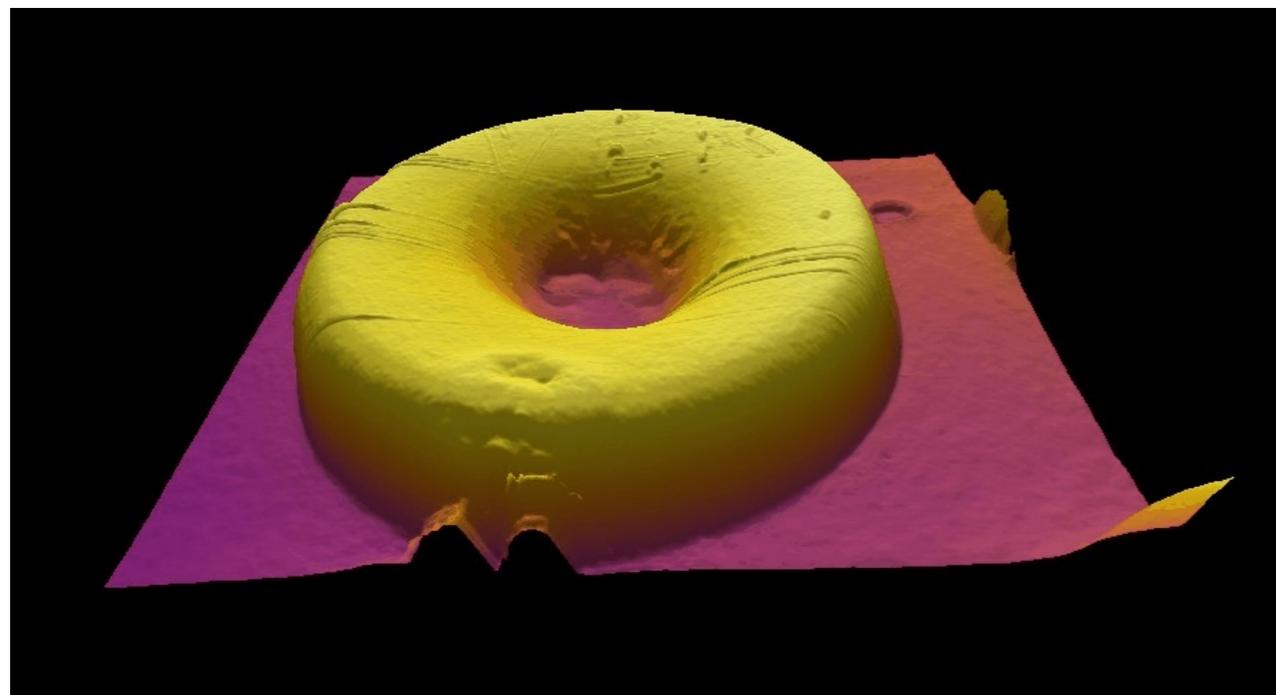


Extensibility of fluorescently labeled fibrin fibrils

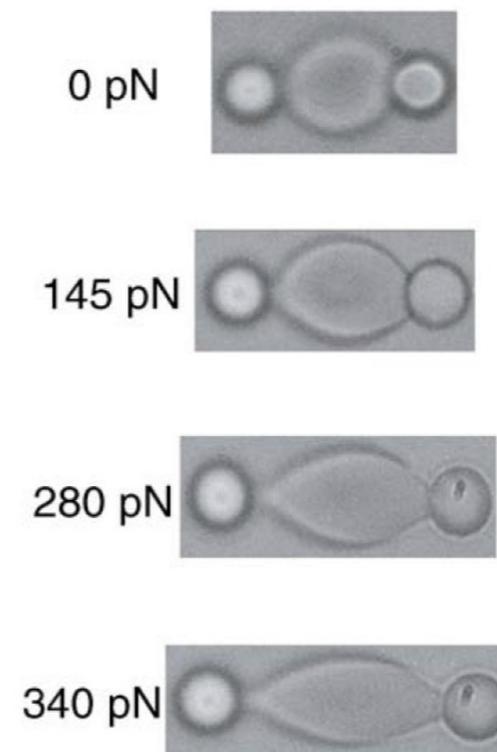
Determinants of blood viscosity

3. *Plasticity of red blood cells*

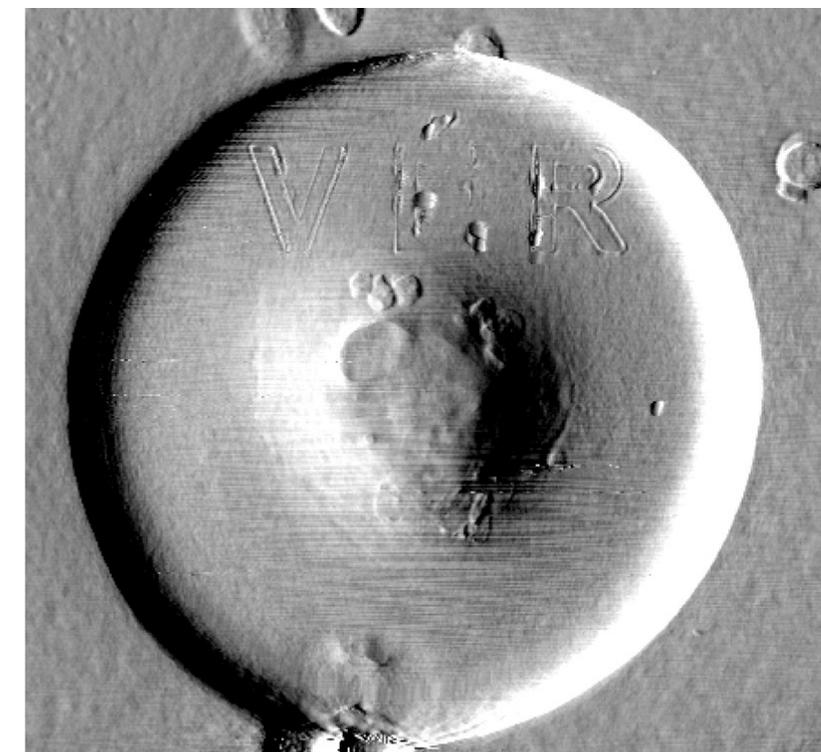
- 65% suspension of blood-cell-size particles is rock hard.
- By contrast, a 95% blood suspension is fluid, with viscosity of ~ 20 mPas!
- Deformation of red blood cells: droplet, parachute, arrowhead shapes.



Disc-shaped cell with 7-11 μm diameter



Deformation of a RBC with optical tweezers



Fixed RBC maintaining impression (AFM)

Determinants of blood viscosity

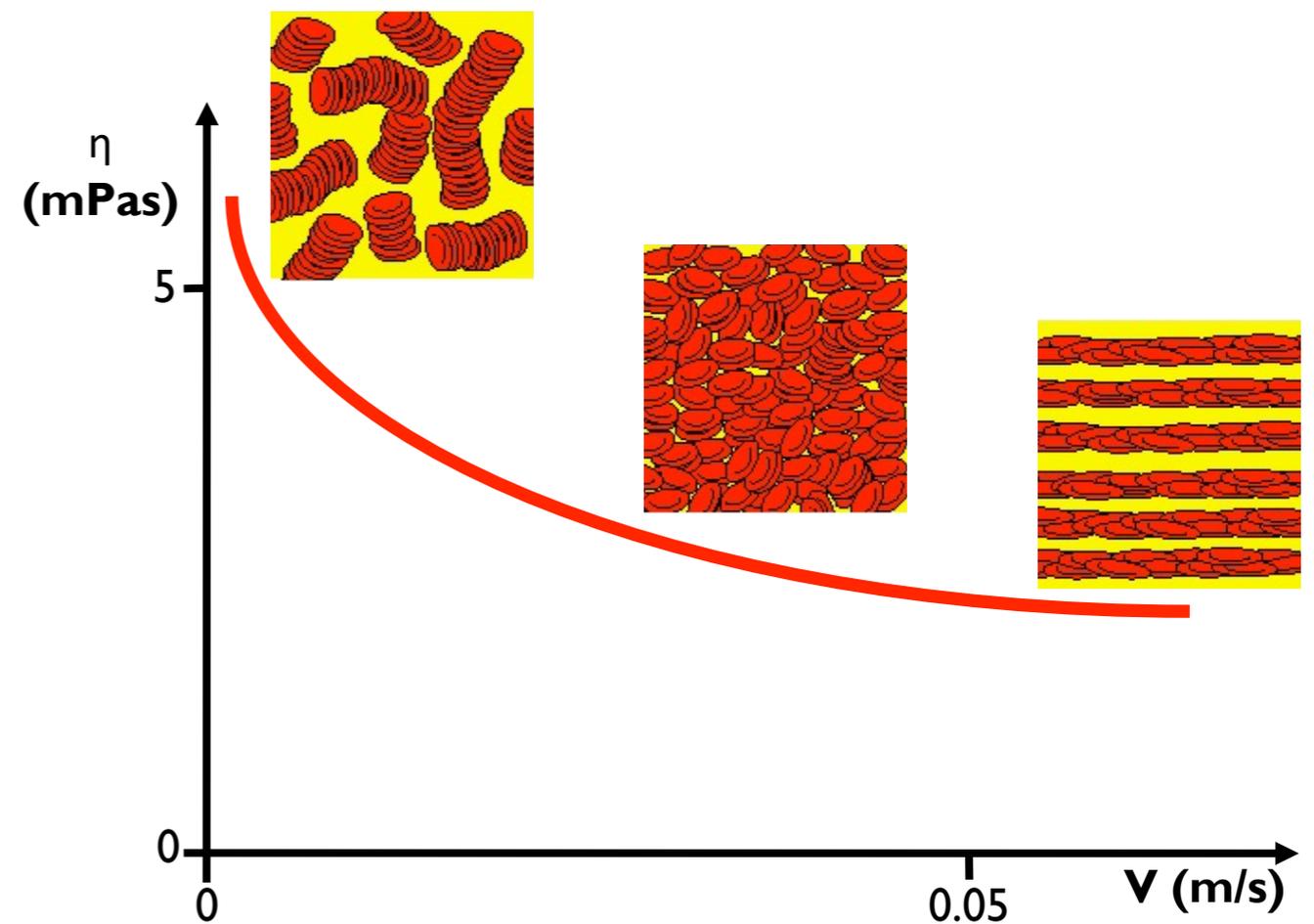
4. Aggregation of red blood cells

- Stack or rouleaux formation.
- More pronounced at low flow rates



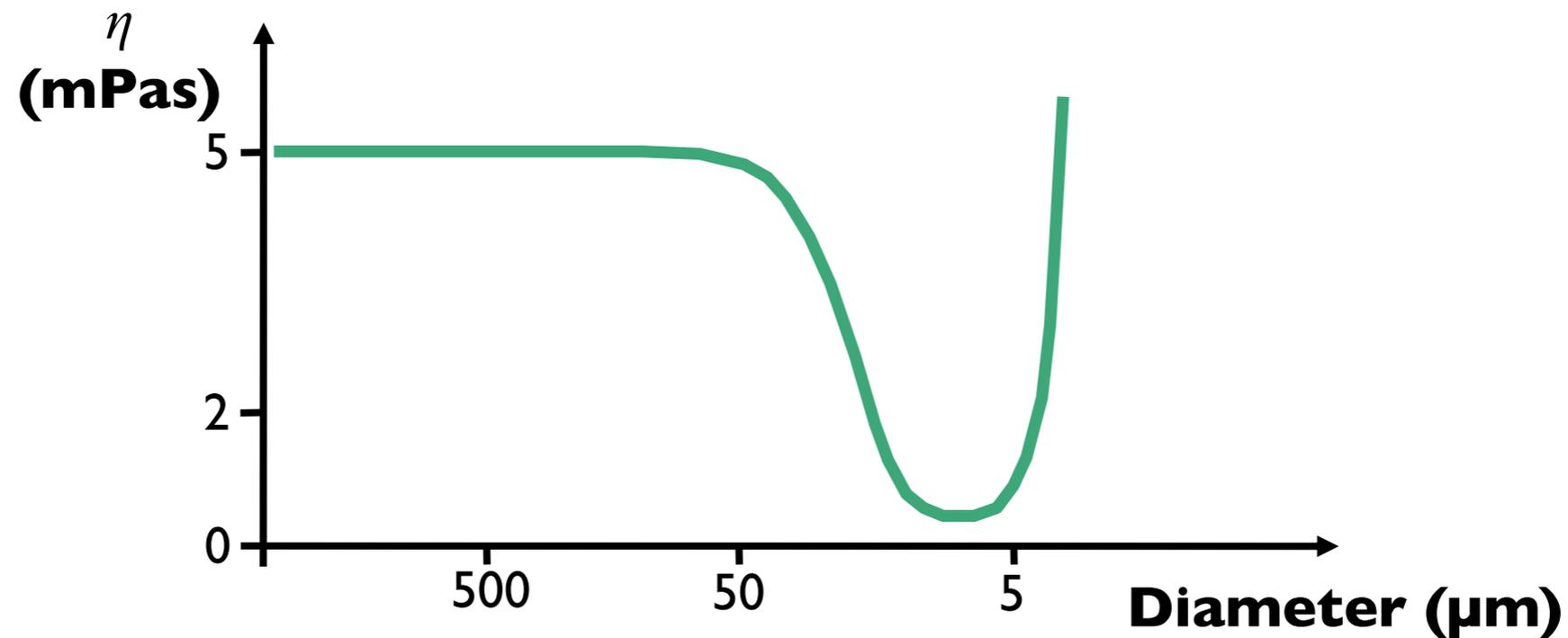
Rouleaux (stack)

5. Flow rate, velocity gradient



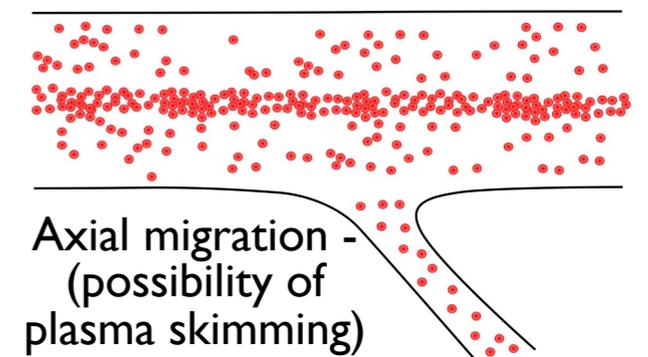
Determinants of blood viscosity

6. Blood vessel diameter



N.B.:

- With a decrease of vessel diameter, the anomalous (non-newtonian) behavior of blood becomes more pronounced.
- *Axial migration*: the red blood cells line up in the axis of the vessel (Bernoulli's law). In the axis the velocity gradient decreases, and near the vessel wall it increases. Increase in velocity gradient decreases apparent viscosity (Fåhræus-Lindquist effect).



Feedback



<https://feedback.semmelweis.hu/feedback/pre-show-qr.php?type=feedback&qr=LGOXIBXNJ84TD66N>