

Physical basis of dental material science

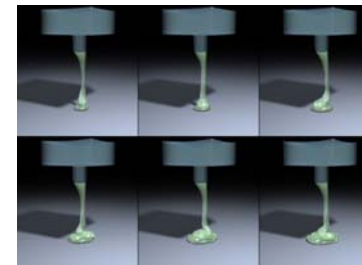
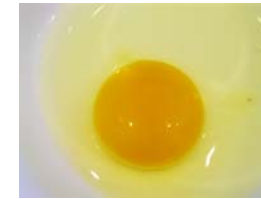
9.

Mechanical properties 3.

1

Viscoelasticity:

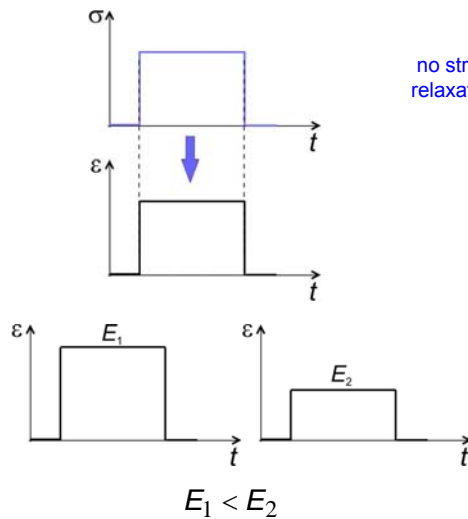
materials that exhibit both viscous and elastic characteristics when undergoing deformation.



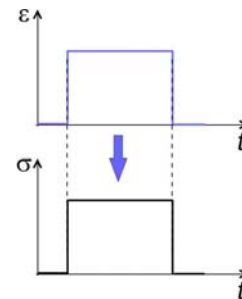
2

Ideal elastic body

Constant force (stress)



Constant deformation



no stress relaxation!

Hooke's law: $\sigma = E\varepsilon$
 $\sigma_{\text{shear}} = G\gamma$

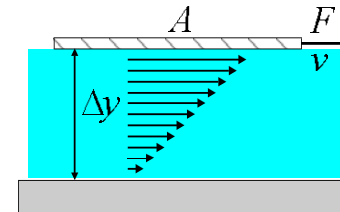
Model:



3

Viscosity (η):

measure of the resistance of a fluid which is being deformed by either shear stress or tensile stress.



A: surface
 F: force
 Δy : layer thickness
 v: speed

Newton's friction law:

$$F_s = \eta \cdot A \cdot \frac{\Delta v}{\Delta y}$$

viscosity (internal friction coefficient)

$$[\eta] = \text{Pa} \cdot \text{s}$$

velocity gradient

$$\frac{F_s}{A} = \eta \cdot \frac{\Delta v}{\Delta y}$$

$$\sigma_{\text{shear}} = \eta g_{\text{speed}}$$

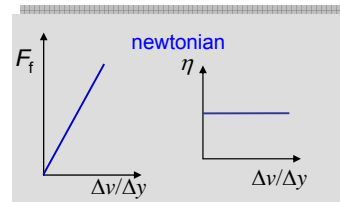
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e.g. at 20 °C:

material	air	water	blood (37°)	glycerine
η (mPa·s)	0.019	1	2–8	1490

Normal (or newtonian) fluid:

The viscosity depends only on the temperature (independent from e.g. velocity gradient or speed of flow).



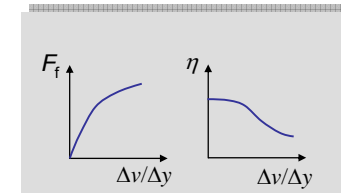
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Anomalous (or non-newtonian) fluids:

The viscosity depends on the **velocity gradient**.

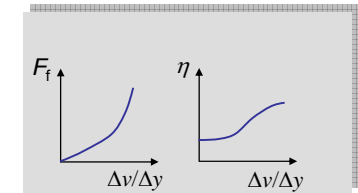
Pseudoplastic:

Viscosity decreases with the rate of shear.

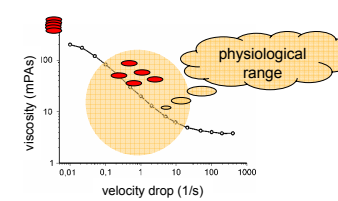


Dilatant:

Viscosity increases with the rate of shear.

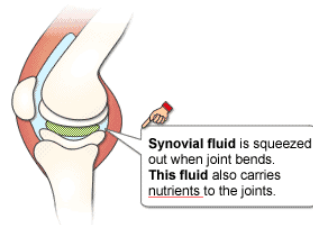
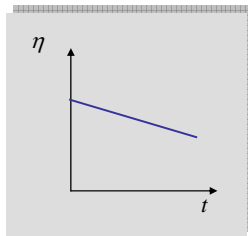


blood

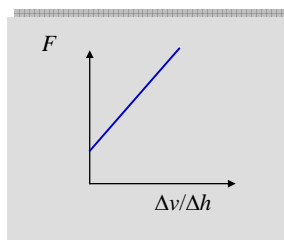


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Tixotropy: normally viscous, but becomes flow if stressed.



Bingham-fluid: behaves as a rigid body at low stresses but flows as a viscous fluid at high stress.



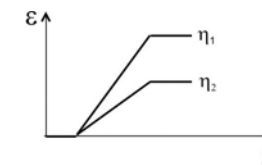
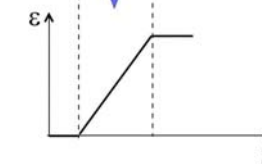
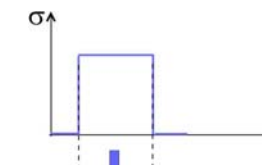
Tooth-paste



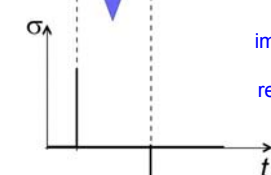
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Ideal viscous body

Deformation in the case of constant force (stress).



Constant deformation



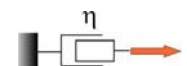
immediate stress relaxation

Newton's law:

$$\sigma_{\text{shear}} = \eta g_{\text{speed}}$$

Model:

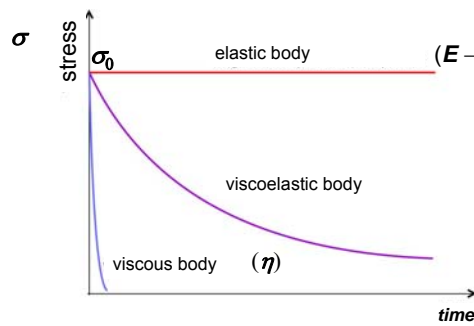
Newtonian dumper
dashpot



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Viscoelasticity:

After instant deformation:



Hooke's law
 $\sigma = E\varepsilon$
 $\sigma_{\text{shear}} = G\gamma$

Stress relaxation:

$$\sigma = \sigma_0 e^{-\frac{t}{t_{\text{rel}}}}$$

$$t_{\text{rel}} = \frac{\eta}{G}$$

relaxation time

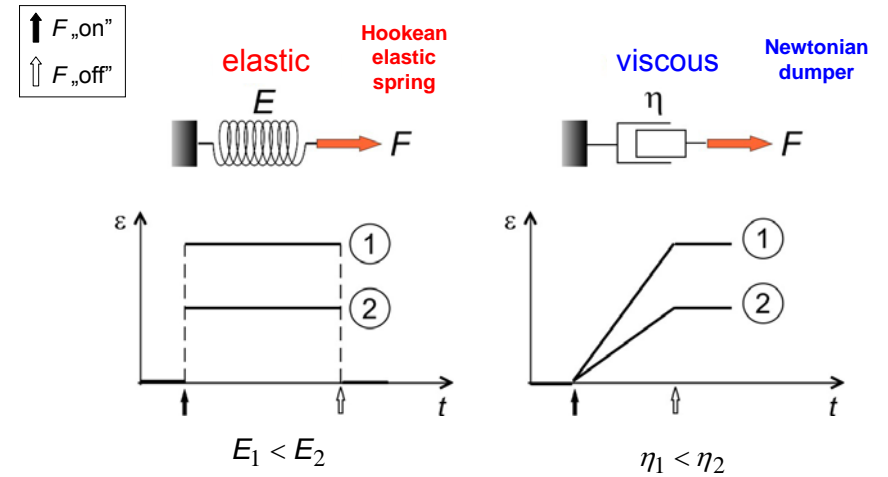
Newton's law
 $\sigma_{\text{shear}} = \eta \dot{\gamma}_{\text{speed}}$



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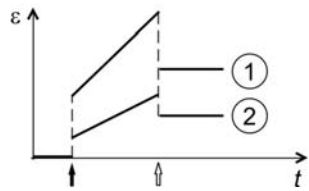
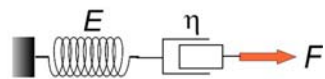
Changing deformation in the case of constant force

Models:



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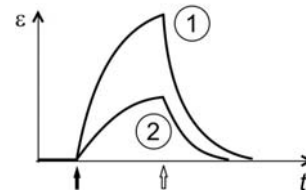
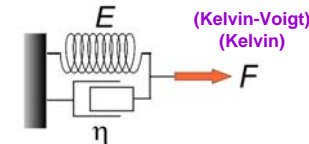
viscoelastic - Maxwell



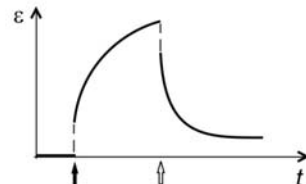
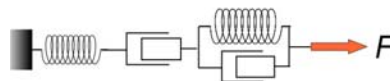
$$E_1 < E_2$$

$$\eta_1 < \eta_2$$

viscoelastic - Voigt



viscoelastic - Burgers



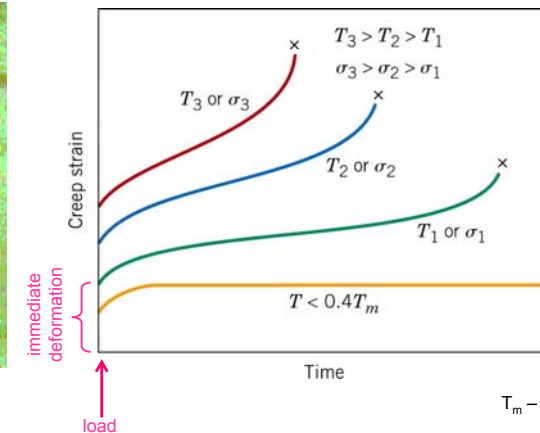
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Creep:

is the slow change in the dimensions of a material due to prolonged stress.



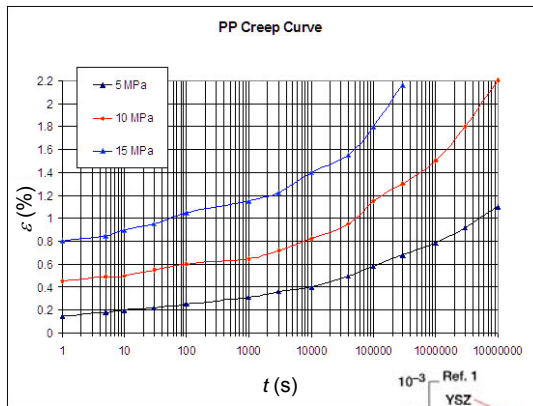
1–10⁷ s !!



temperature!
 e.g. metals
 $0.4T_0 < T$

Modell: ? — Maxwell

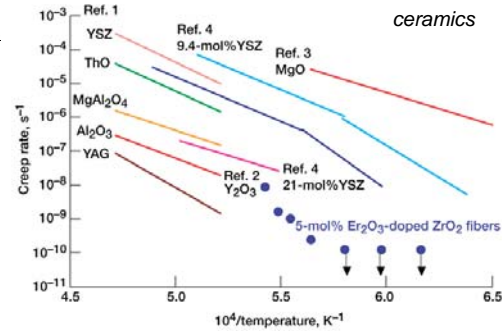
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Polipropilene (PP)

ε — creep strain

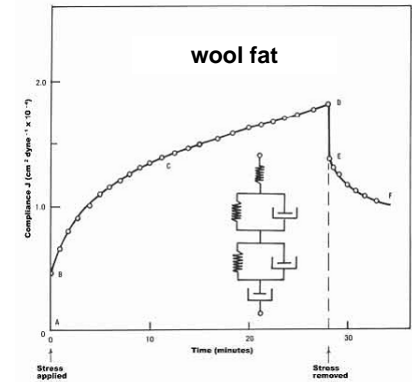
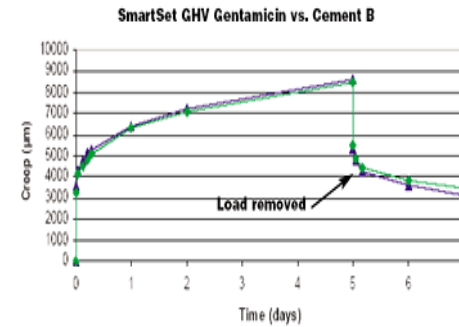
$\frac{\Delta \varepsilon}{\Delta t}$ creep rate



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Relaxation (recovery)

Rearrangement after stress removed.



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Relaxation

Decreasing of the inner stress in the case of constant deformation.



aluminium

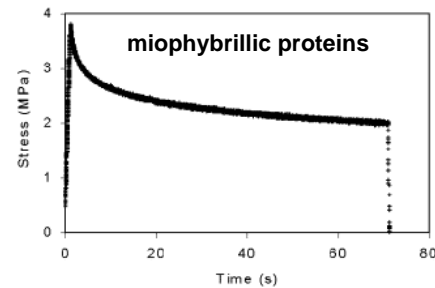
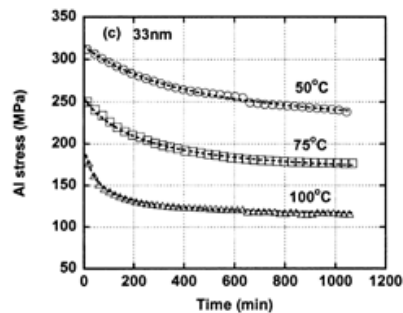
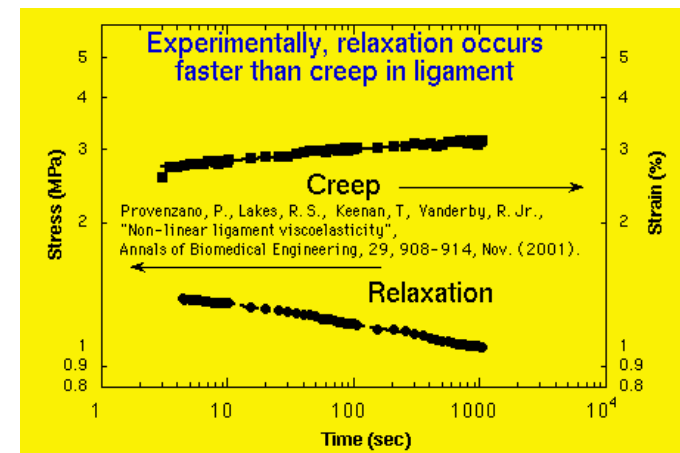


FIGURE 4. Original data of stress vs. time obtained by relaxation tests with films of MPNT.

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Fatigue:

structural damage that occurs when a material is subjected to cyclic loading.

(The nominal maximum stress values are less than the ultimate tensile stress limit)



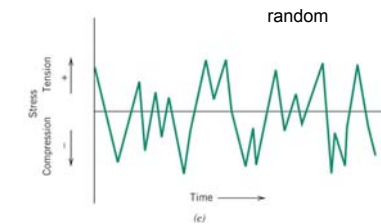
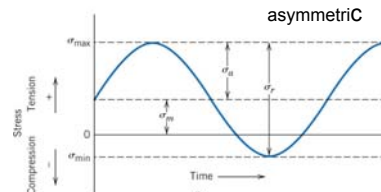
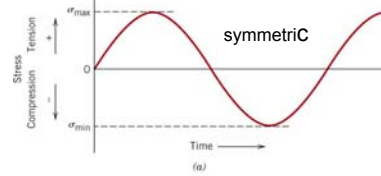
Long, repeated load

→ structural changes

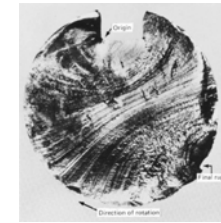
→ strength decreases

cracks!

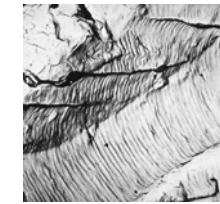
type of loads:



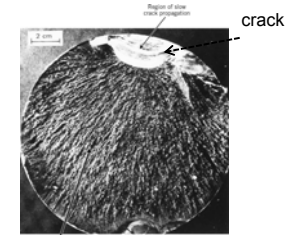
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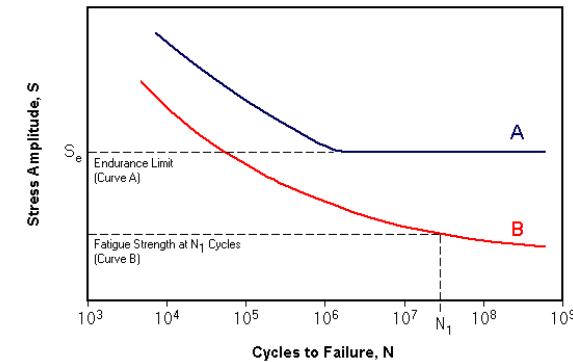
(fracture structure in rotating steel)



(fatigue striation in Al)



rapid failure



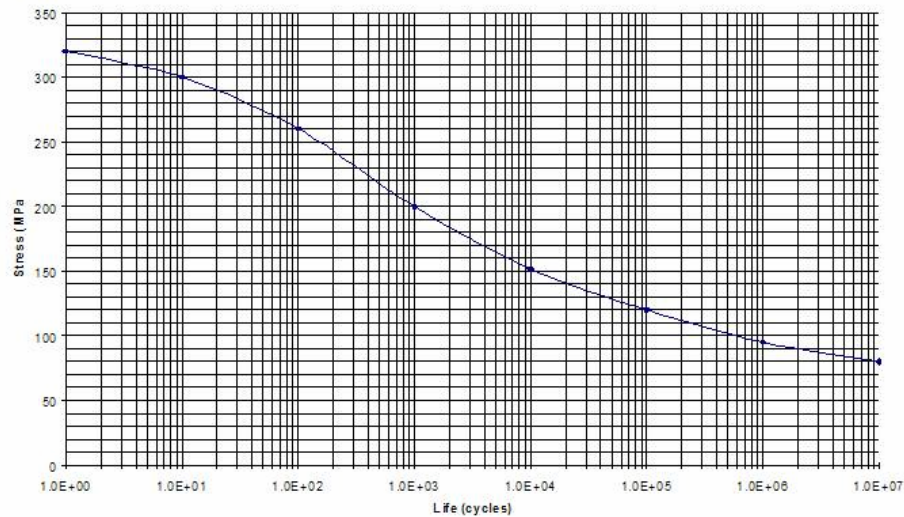
Fatigue S-N curve:

e.g. steel, titanium, ...

e.g. aluminium, copper, ...

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S-N CURVE FOR BRITTLE ALUMINUM WITH A UTS OF 320 MPa

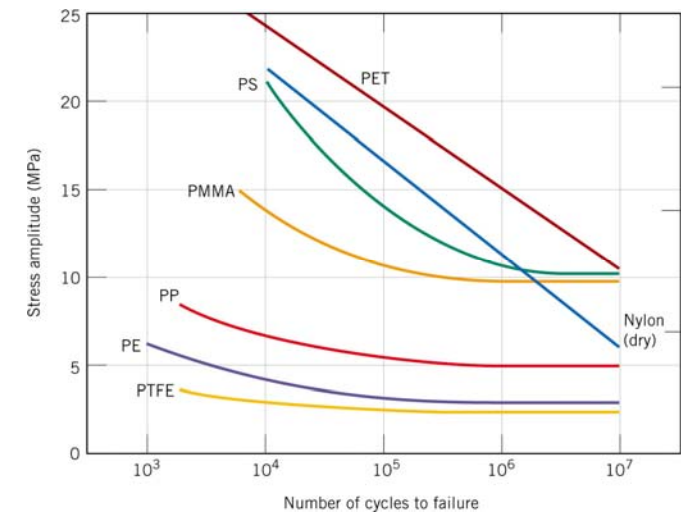


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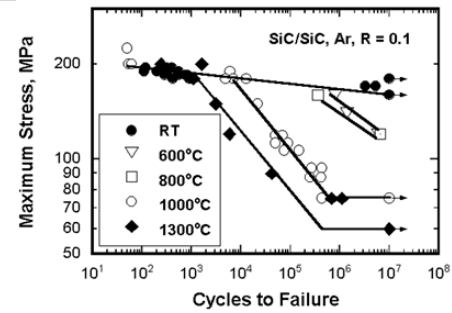
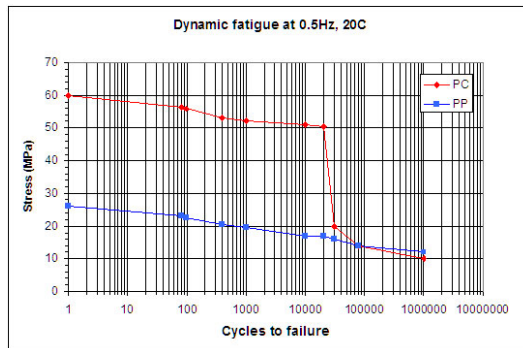
polymers

PET: Polyethylene terephthalate
PS: Polystyrene
PMMA: Poly(methyl methacrylate)

PP: Polyethylene terephthalate
PE: Polyethylene
PTFE: Polytetrafluoroethylene



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Abrasion (loss of tooth structure by mechanical forces)



Hardness!

(e.g. hardness of enamel)

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